

RECEIVED: November 16, 2010

REVISED: December 6, 2010

ACCEPTED: December 8, 2010

PUBLISHED: December 27, 2010

Colored resonant signals at the LHC: largest rate and simplest topology

Tao Han, Ian Lewis and Zhen Liu

Department of Physics, 1150 University Avenue, University of Wisconsin, Madison, WI 53706, U.S.A.

E-mail: than@hep.wisc.edu, ilewis@wisc.edu, zliu57@wisc.edu

ABSTRACT: We study the colored resonance production at the LHC in a most general approach. We classify the possible colored resonances based on group theory decomposition, and construct their effective interactions with light partons. The production cross section from annihilation of valence quarks or gluons may be on the order of 400 – 1000 pb at LHC energies for a mass of 1 TeV with nominal couplings, leading to the largest production rates for new physics at the TeV scale, and simplest event topology with dijet final states. We apply the new dijet data from the LHC experiments to put bounds on various possible colored resonant states. The current bounds range from 0.9 to 2.7 TeV. The formulation is readily applicable for future searches including other decay modes.

KEYWORDS: Jets, Beyond Standard Model, Phenomenological Models, Hadronic Colliders

Contents

1	Introduction	1
2	Classification of resonant particles in hadronic collisions	2
3	Parton-resonance interactions	3
3.1	$\mathbf{3} \otimes \mathbf{3}$	4
3.2	$\mathbf{3} \otimes \mathbf{8}$	5
3.3	$\mathbf{8} \otimes \mathbf{8}$	6
3.4	$\mathbf{3} \otimes \bar{\mathbf{3}}$	7
4	Resonance production at the LHC	8
4.1	Quark-quark annihilation	10
4.2	Quark-gluon annihilation	12
4.3	Gluon-gluon annihilation	13
4.4	Quark-antiquark annihilation	14
5	Bounds from the LHC Dijet spectrum	16
6	Conclusion	19
A	Clebsch-Gordan coefficients	20
B	Feynman rules	21

1 Introduction

With the first crop of data being released, the CERN Large Hadron Collider (LHC) is already pushing the energy frontier and taking the field of high energy physics to a new era. While much of the attention for new physics discovery has centered on theories associated with electroweak symmetry breaking, most initial states at hadron colliders are composed of colored particles. Hence, any new colored resonances will be produced with favorable rates at the LHC since their couplings may be typically of the strength of the strong-interaction.

Beyond the Standard Model (SM), there are many possible exotic colored states that can be produced at the LHC. Besides being phenomenologically interesting and experimentally important to search for, many of the exotic states are also theoretically motivated. For example, color-antitriplet scalars may be produced via quark-quark annihilation as squarks in R-parity violating supersymmetric (SUSY) theories [1], or as “diquarks” in E_6 grand unified theories [2]. Color-sextet scalars can arise in partially unified Pati-Salam theories [3–5] and be produced also via quark-quark annihilation. Color-triplet fermions can

be produced via quark-gluon annihilation as “excited quarks” in composite models [6–10]. Sextet fermions, the so-called “quixes”, associated with chiral color [11] and top quark condensate models [12] may also be produced via quark-gluon annihilation. Color-octet scalars that are $SU(2)_L$ singlets can arise in technicolor models [13], and in universal extra dimensions [14, 15]. Color-octet vectors have been extensively explored as axigluons [11, 16] and colorons [17–19]. There has also been much recent interest in studying the similar states in the context of Kaluza-Klein gluons [20–22], and low-scale string resonances [23–27] via gluon-gluon, or quark-antiquark annihilation.

Any new resonant states produced at the LHC through interactions with light partons will contribute to the dijet production, leading to one of the simplest signal topologies. Both the ATLAS and CMS collaborations have recently searched for this class of signal and obtained 95% confidence level limits on the production cross section of such resonant states. From these limits they were able to already put the most stringent bound on the mass of an excited quark of 1.53 TeV from ATLAS [28] and 1.58 from CMS [29], and on a string resonance [29] of 2.5 TeV.

Motivated by the above considerations, we study the colored resonances in a most general way. We classify them according to their couplings to light partons, solely based on group theory decomposition as shown in section 2. Among those possible colored resonances, we focus on those produced by the leading parton luminosities directly from valence quarks or gluons. We then construct their couplings to light partons and describe their general features in section 3. In section 4 we calculate the cross sections for their resonant production at the LHC with c.m. energies of 7 and 14 TeV. We apply the new ATLAS and CMS data to put bounds on various possible colored resonant states in section 5. Finally, we conclude in section 6. A few appendices contain the QCD color treatment, and a list of Feynman rules for the resonance couplings to the initial state light partons.

2 Classification of resonant particles in hadronic collisions

The resonance structures can be classified according to the spin (J) and the quantum numbers under the SM gauge group $SU(3)_C \times SU(2)_L \times U(1)_Y$. We adopt a notation of group structure

$$(SU_3, SU_2)_{Q_e}^J, \tag{2.1}$$

where Q_e indicates the electric charge ($T_3 + Y$).

In pp collisions at the LHC, we consider the dominant partons participating in the heavy resonance production to be the valence quarks and gluons. We express them with our notation as

Q	$(\mathbf{3}, \mathbf{2})_{2/3, -1/3}^{1/2}$	Left – handed doublet	
U	$(\mathbf{3}, \mathbf{1})_{2/3}^{1/2}$	Right – handed singlet	(2.2)
D	$(\mathbf{3}, \mathbf{1})_{-1/3}^{1/2}$	Right – handed singlet	
A	$(\mathbf{8}, \mathbf{1})_0^1$	vector.	

We can thus classify the single particle production via the annihilation of any two partons above. Table 1 lists the quantum numbers of possible resonances in our notation from two

initial state	J	$SU(3)_C$	$SU(2)_L$	$U(1)_Y$	$ Q_e $	B
QQ	0	$\bar{\mathbf{3}} \oplus \mathbf{6}$	$\mathbf{1} \oplus \mathbf{3}$	$\frac{1}{3}$	$\frac{4}{3}, \frac{2}{3}, \frac{1}{3}$	$\frac{2}{3}$
QU	1	$\bar{\mathbf{3}} \oplus \mathbf{6}$	$\mathbf{2}$	$\frac{5}{6}$	$\frac{4}{3}, \frac{1}{3}$	$\frac{2}{3}$
QD	1	$\bar{\mathbf{3}} \oplus \mathbf{6}$	$\mathbf{2}$	$-\frac{1}{6}$	$\frac{2}{3}, \frac{1}{3}$	$\frac{2}{3}$
UU	0	$\bar{\mathbf{3}} \oplus \mathbf{6}$	$\mathbf{1}$	$\frac{4}{3}$	$\frac{4}{3}$	$\frac{2}{3}$
DD	0	$\bar{\mathbf{3}} \oplus \mathbf{6}$	$\mathbf{1}$	$-\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$
UD	0	$\bar{\mathbf{3}} \oplus \mathbf{6}$	$\mathbf{1}$	$\frac{1}{3}$	$\frac{1}{3}$	$\frac{2}{3}$
QA	$\frac{1}{2}, \frac{3}{2}$	$\mathbf{3} \oplus \bar{\mathbf{6}} \oplus \mathbf{15}$	$\mathbf{2}$	$\frac{1}{6}$	$\frac{2}{3}, \frac{1}{3}$	$\frac{1}{3}$
UA	$\frac{1}{2}, \frac{3}{2}$	$\mathbf{3} \oplus \bar{\mathbf{6}} \oplus \mathbf{15}$	$\mathbf{1}$	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{1}{3}$
DA	$\frac{1}{2}, \frac{3}{2}$	$\mathbf{3} \oplus \bar{\mathbf{6}} \oplus \mathbf{15}$	$\mathbf{1}$	$\frac{1}{3}$	$\frac{1}{3}$	$\frac{1}{3}$
AA	0, 1, 2	$\mathbf{1} \oplus \mathbf{8} \oplus \mathbf{8} \oplus \mathbf{10} \oplus \bar{\mathbf{10}} \oplus \mathbf{27}$	$\mathbf{1}$	0	0	0
$Q\bar{Q}$	1	$\mathbf{1} \oplus \mathbf{8}$	$\mathbf{1} \oplus \mathbf{3}$	0	1, 0	0
$Q\bar{U}$	0	$\mathbf{1} \oplus \mathbf{8}$	$\mathbf{2}$	$-\frac{1}{2}$	1, 0	0
$Q\bar{D}$	0	$\mathbf{1} \oplus \mathbf{8}$	$\mathbf{2}$	$\frac{1}{2}$	1, 0	0
$U\bar{U}, D\bar{D}$	1	$\mathbf{1} \oplus \mathbf{8}$	$\mathbf{1}$	0	0	0
$U\bar{D}$	1	$\mathbf{1} \oplus \mathbf{8}$	$\mathbf{1}$	1	1	0

Table 1. The $SU(3)_C \times SU(2)_L \times U(1)_Y$ quantum numbers and spins (J) of possible resonant states created by initial state quarks and gluons. The electric charge ($Q_e = T_3 + Y$) and baryon number (B) carried by the two initial state partons are also provided.

initial partons. Since the LHC is a “QCD machine”, it is natural to start primarily based on the $SU(3)_C$ quantum numbers of the two initial states. We thus have partonic collisions of quark-quark: $\mathbf{3} \otimes \mathbf{3}$; quark-gluon: $\mathbf{3} \otimes \mathbf{8}$; gluon-gluon: $\mathbf{8} \otimes \mathbf{8}$; and quark-antiquark: $\mathbf{3} \otimes \bar{\mathbf{3}}$.

Possible spins and the electric charges are also given in table 1. In principle, neutral particles may be further classified by the discrete symmetries according to their parity (P), charge conjugation (C), and CP properties if these quantum numbers are conserved in their interactions. We will discuss them in the next section. In the last column, we add baryon numbers (B) carried by the initial state partons. Depending on the underlying theory for the new resonances, baryon number may or may not be conserved in their interactions.

3 Parton-resonance interactions

We now construct the interaction Lagrangians for the resonances and partons guided by the SM gauge symmetry. We limit our consideration only to those colored states listed in table 1. We will not postulate their interactions with other particles (leptons, electroweak bosons, or even new particles beyond the SM). Although an incomplete description for a resonant particle as a full interacting theory, this minimal approach is sufficient for evaluating the production rate at the LHC. Assuming these interactions dominate, then their decay to dijets would also be the leading channel. Furthermore, we will not consider higher dimensional color representations beyond $\mathbf{8}$ again due to the minimality considerations.

Should there exist a color “**15-tet**” fermion, a simple calculation of the QCD beta-function would indicate the loss of the asymptotic freedom of QCD [30].

A similar approach to ours has been carried out to construct the potentially large signals at the early run of the LHC with minimal model input [31–34]. There has also been previous work on classifying exotic particles at the LHC [35, 36].

3.1 $\mathbf{3} \otimes \mathbf{3}$

At the LHC the valence-valence initial states consist of two quarks, uu , dd , or ud . Hence, the production cross section of a heavy particle that couples to two quarks will receive an enhancement from the parton luminosity of the initial state. As listed on the top section of table 1, such states can be color-antitriplets or sextets. They also carry an exotic baryon number of $2/3$ (if B is conserved) and thus are often referred to “diquarks”.¹ According to their electroweak (EW) quantum numbers under $SU(2)_L \otimes U(1)_Y$, there are 6 such states. We denote them by the notation in eq. (2.1) as

$$\begin{aligned} \Phi &\sim (\mathbf{3} \oplus \bar{\mathbf{6}}, \mathbf{3})_{-4/3, 2/3, -1/3}^0, & \Phi_q &\sim (\mathbf{3} \oplus \bar{\mathbf{6}}, \mathbf{1})_q^0 \quad (q = -1/3, 2/3, -4/3), \\ V_U^\mu &\sim (\mathbf{3} \oplus \bar{\mathbf{6}}, \mathbf{2})_{-1/3, -4/3}^1 & V_D^\mu &\sim (\mathbf{3} \oplus \bar{\mathbf{6}}, \mathbf{2})_{2/3, -1/3}^1. \end{aligned} \quad (3.1)$$

We construct the gauge invariant Lagrangian as follows

$$\begin{aligned} \mathcal{L}_{qqD} &\sim K_{ab}^j \left[y_{\alpha\beta} \overline{Q_{\alpha a}^C} i\sigma_2 \Phi^j Q_{\beta b} + \kappa_{\alpha\beta} \Phi_{-1/3}^j \overline{Q_{\alpha a}^C} i\sigma_2 Q_{\beta b} \right. \\ &\quad + \lambda_{\alpha\beta}^{1/3} \Phi_{-1/3}^j \overline{D_{\alpha a}^C} U_{\beta b} + \lambda_{\alpha\beta}^{2/3} \Phi_{2/3}^j \overline{D_{\alpha a}^C} D_{\beta b} + \lambda_{\alpha\beta}^{4/3} \Phi_{-4/3}^j \overline{U_{\alpha a}^C} U_{\beta b} \\ &\quad \left. + \lambda_{\alpha\beta}^U \overline{Q_{\alpha a}^C} i\sigma_2 \gamma_\mu V_U^{j\mu} U_{\beta b} + \lambda_{\alpha\beta}^D \overline{Q_{\alpha a}^C} i\sigma_2 \gamma_\mu V_D^{j\mu} D_{\beta b} \right] + \text{h.c.}, \end{aligned} \quad (3.2)$$

where $\Phi^j = \frac{1}{2}\sigma_k \Phi_k^j$ with σ_k the $SU(2)_L$ Pauli matrices and K_{ab}^j are $SU(3)_C$ Clebsch-Gordan coefficients with the quark color indices $a, b = 1 - 3$, and the diquark color index $j = 1 - N_D$. N_D is the dimension of the ($N_D = 3$) triplet or ($N_D = 6$) antisextet representation. C denotes charge conjugation, and α, β are the fermion generation indices. The color factor K_{ab}^j is symmetric (antisymmetric) under ab for the $\mathbf{6}$ ($\bar{\mathbf{3}}$) representation. Their normalization convention is given in appendix A.

After electroweak symmetry breaking, the states in eq. (3.1) mix and reclassify themselves according to color ($\mathbf{3}$, $\bar{\mathbf{6}}$) and electric charges ($-4/3$, $2/3$, $-1/3$), denoted by $E_{N_D}, U_{N_D}, D_{N_D}$. The relevant interactions among the physical states are then

$$\begin{aligned} \mathcal{L}_{qqD} &= K_{ab}^j \left[\lambda_{\alpha\beta}^E E_{N_D}^j \overline{u_{\alpha a}^C} P_\tau u_{\beta b} + \lambda_{\alpha\beta}^U U_{N_D}^j \overline{d_{\alpha a}^C} P_\tau d_{\beta b} + \lambda_{\alpha\beta}^D D_{N_D}^j \overline{d_{\alpha a}^C} P_\tau u_{\alpha a} \right. \\ &\quad + \lambda_{\alpha\beta}^{E'} E_{N_D}^{j\mu} \overline{u_{\alpha a}^C} \gamma_\mu P_R u_{\beta b} + \lambda_{\alpha\beta}^{U'} U_{N_D}^{j\mu} \overline{d_{\alpha a}^C} \gamma_\mu P_R d_{\beta b} \\ &\quad \left. + \lambda_{\alpha\beta}^{D'} D_{N_D}^{j\mu} \overline{u_{\alpha a}^C} \gamma_\mu P_\tau d_{\beta b} \right] + \text{h.c.} \end{aligned} \quad (3.3)$$

where $P_\tau = \frac{1}{2}(1 \pm \gamma_5)$ with $\tau = R, L$ for the right- and left-chirality projection operators. Here and henceforth, we include a superscript μ to indicate a vector state.

¹This should not be confused with a possible two-light-quark bound state as “diquark”. We are talking about a new state at a TeV mass scale with a quantum number similar to two quarks.

Naively, the strength of these Yukawa interactions can be naturally of the order of unity, since the interactions among colored states are likely to be similar to QCD strong interaction with a coupling constant $g_s^2 = 4\pi\alpha_s \sim \mathcal{O}(1)$. However, many of them are tightly constrained by flavor physics. A commonly adopted solution is the “minimal flavor violation” (MFV) [37, 38]. This assumption makes the couplings align with the SM Yukawa matrices, and they only become significant when involving heavier quarks such as the top [39]. In some specific model realizations, the MFV is not necessary and certain individual operators involving light flavors can be sizable [40]. We do not introduce additional couplings for those new colored states and thus the baryon number is conserved. In fact, the baryon number can be made a conserved quantum number for the above interactions by the SM gauge symmetry along with a simple extension to the lepton sector [39].

We note that the color-triplet scalars (U_3, D_3) resemble scalar quarks (\tilde{u}, \tilde{d}) in SUSY and the interactions (with the chirality $\tau = L$) are directly analogous to R-parity violating operators of the λ'' terms [1], or the “diquarks” [2]. Color-triplet scalars at the TeV scale have also been considered in SUSY models to present a unified explanation of dark matter and baryogenesis [41]. The color-sextet scalars possess similar nature of “diquark Higgs” in some unified theories [3–5] or some exotic diquarks [42]. The vector states, on the other hand, are more exotic in terms of connections with an underlying model. There has been previous interest in the resonant production of diquark scalars and vectors at the LHC [43–46].

3.2 $\mathbf{3} \otimes \mathbf{8}$

A gluon and a quark can yield large partonic luminosity, and may couple to exotic fermion states. For simplicity, we only consider spin-1/2 states, with quantum numbers as

$$(\mathbf{3} \oplus \bar{\mathbf{6}}, \mathbf{1} \oplus \mathbf{2})_{-1/3, 2/3}^{1/2}$$

We have not included the $\mathbf{15}$ since, as mentioned previously in this section, a $\mathbf{15}$ fermion would spoil the asymptotic freedom of the strong coupling.

Instead of writing down the complete SM gauge invariant operators, we consider the interactions after electroweak symmetry breaking with physical mass eigenstates. These two states are fermionic and of electric charges $-1/3$ and $2/3$. We denote them generically by $q_{N_D}^*$, or specifically by $d_{N_D}^*$ and $u_{N_D}^*$, where $N_D = 3$ or 6 for the dimension of their color representation. The $SU(3)_C$ gauge invariance requires the interactions to start with dimension-five, and are of the color-magnetic dipole form. The Lagrangian for these physical states is then

$$\begin{aligned} \mathcal{L}_{qqF} = & \frac{g_s}{\Lambda} F^{A,\mu\nu} [\bar{u} \bar{K}_{N_D,A} (\lambda_L^U P_L + \lambda_R^U P_R) \sigma_{\mu\nu} u_{N_D}^* \\ & + \bar{d} \bar{K}_{N_D,A} (\lambda_L^D P_L + \lambda_R^D P_R) \sigma_{\mu\nu} d_{N_D}^*] + \text{h.c.} \end{aligned} \quad (3.4)$$

where $F^{A,\mu\nu}$ is the gluon field strength tensor with the adjoint color index $A = 1, \dots, 8$, and \bar{K}_A are $3 \times N_D$ matrices of Clebsch-Gordan coefficients connecting the color indices of the different representations. If the new fermion field is a $\mathbf{3}$, then $\bar{K}_A^\dagger = K^A = \sqrt{2}T^A$, where T^A are the fundamental $SU(3)$ representation matrices. Due to the presence of a gluon

field, we naturally include a QCD coupling g_s . The new physics scale Λ is at least $M_{q_j^*}$ or higher. In a strongly interacting theory, we expect that the strength of the couplings $\lambda_{L,R}^U$ and $\lambda_{L,R}^D$ should be typically of the order of unity. However, if the operators are from one-loop contributions in a weakly coupled theory, then one would expect to have a suppression factor of the order $1/16\pi^2$ [31, 32].

The color-triplet states resemble the excited quarks. They could also be string excitations in a low scale string scenarios [23–27]. The color-sextet fermions arise in theories of chiral color [11] and top quark condensate models [12], the so-called “quixes”. There has been previous interest in the color-sextet fermion production at hadron colliders [47].

3.3 $\mathbf{8} \otimes \mathbf{8}$

LHC is often referred to as a “gluon machine” since it has a large parton luminosity for gluon-gluon initial states. Among the bosonic states from the $\mathbf{8} \otimes \mathbf{8}$ decompositions, many higher dimensional color representations can be embedded into larger theories, unlike the 15-tet fermion states that spoil the asymptotic freedom. We only focus on the color-octet resonances that can result from gluon-gluon fusion. They may carry the quantum numbers

$$(\mathbf{8}_S \oplus \mathbf{8}_A, \mathbf{1})_0^{0,1,2}. \tag{3.5}$$

The symmetric and antisymmetric representations can be utilized with the algebraic relations of the fundamental representation matrices

$$[T^A, T^B] = if^{ABC}T^C, \quad \{T^A, T^B\} = \frac{1}{N_C}\delta^{AB} + d^{ABC}T^C, \tag{3.6}$$

and $N_C = 3$ is the dimension of the $SU(3)_C$ fundamental representation.

The leading operators start from dimension-five. Two possible interactions between gluons and a spin zero octet and spin two octet are

$$\mathcal{L}_{gg8} = g_s d^{ABC} \left(\frac{\kappa_S}{\Lambda_S} S_8^A F_{\mu\nu}^B F^{C,\mu\nu} + \frac{\kappa_T}{\Lambda_T} \left(T_8^{A,\mu\sigma} F_{\mu\nu}^B F_{\sigma}^{\nu} + f T_8^A{}_{\rho} F^{B,\mu\nu} F_{\mu\nu}^C \right) \right), \tag{3.7}$$

where S_8 (T_8) is a scalar (tensor) octet. We again assume that the couplings κ_S, κ_T of the order of unity. The relative coupling factor f is more likely to be 1. If the operators are from one-loop contributions in a weakly coupled theory, then one would expect to have a suppression factor of the order $1/16\pi^2$.

It is also possible to couple two gluons and a CP-odd octet scalar or tensor. The couplings of the CP odd states are identical in form to those in eq. (3.7) with the replacement of one field strength tensor with its dual:

$$\tilde{F}_{\mu\nu}^A = \frac{1}{2}\varepsilon^{\mu\nu\rho\sigma} F_{\rho\sigma}^A, \tag{3.8}$$

where $\varepsilon^{\mu\nu\rho\sigma}$ is the four dimensional antisymmetric tensor.

Finally, the antisymmetric structure constants f^{ABC} can also be used to construct interactions with CP-odd color octets. However, since the color structure is antisymmetric,

the Lorentz structure must also be antisymmetric. Hence, terms proportional to $F_{\mu\nu}\tilde{F}^{\mu\nu}$ are zero and the only surviving term is $\tilde{T}_8^{\mu\sigma}\tilde{F}_{\mu\nu}F_\sigma{}^\nu$, where \tilde{T}_8 is the CP-odd color-octet tensor.

Color-octet (pseudo)scalars can arise in technicolor models [13, 48], and in universal extra dimensions [14, 15]. There has been much recent interest in the gluon fusion production of color-octet scalars at the LHC [49–53]. These interactions were induced via loops which are parameterized by the octet-scalar coupling in eq. (3.7) with an additional suppression from the loop factor. Color-octet vector states have also been studied in the context of low-scale string resonances [24–27] via gluon-gluon annihilation, but it typically leads to a suppressed rate.

3.4 $\mathbf{3} \otimes \bar{\mathbf{3}}$

Although the quark-antiquark annihilation would not result in the largest partonic luminosity at high energies in pp collisions, we include some discussions for resonant production from $\mathbf{3} \otimes \bar{\mathbf{3}}$ for completeness. The resonances may carry the quantum numbers

$$(\mathbf{1} \oplus \mathbf{8}, \mathbf{1} \oplus \mathbf{3})_{-1,0,1}^1, \quad (\mathbf{1} \oplus \mathbf{8}, \mathbf{2})_{0,1}^0. \quad (3.9)$$

Once again, we focus on the color-octet states and ignore the well-known color-singlet states such as Z' 's, W' 's, and Kaluza-Klein gravitons.

We first consider the color-octet vector states. We denote them according to their color and electric charges V_8^0, V_8^\pm . We write their interactions with quarks as

$$\begin{aligned} \mathcal{L}_{q\bar{q}V} = g_s \left[V_8^{0,A,\mu} \bar{u}T^A\gamma_\mu(g_L^U P_L + g_R^U P_R)u + V_8^{0,A,\mu} \bar{d}T^A\gamma_\mu(g_L^D P_L + g_R^D P_R)d \right. \\ \left. + \left(V_8^{+,A,\mu} \bar{u}T^A\gamma_\mu(C_L V_L^{CKM} P_L + C_R V_R^{CKM} P_R)d + \text{h.c.} \right) \right], \quad (3.10) \end{aligned}$$

where $V_{L,R}^{CKM}$ are the left- and right-handed CKM matrices. Due to the stringent constraints from flavor physics, we have assumed that there is no FCNC, and the charged current aligns with the SM CKM. The couplings $C_{L,R}$ and $g_{L,R}$ are thus diagonal and naturally order of unity. Well-known examples of color-octet vectors coupled to $q\bar{q}$ include the axigluon [11, 16], a coloron or Techni- ρ [17–19], a Kaluza-Klein gluon [20–22], and low-scale string resonances [23–27] via $q\bar{q}$ annihilation.

As for the color-octet scalar states, we note that the renormalizable interactions between a color-octet scalar and two quarks are Yukawa type interactions, and the SM gauge invariant interactions require the scalar to be a doublet [54] under $SU(2)_L$. Once again, due to the assumption of MFV, their couplings to light quarks would be small, and the only significant coupling would be to the top or bottom quarks. The single production of charged and neutral scalars through initial state bottom quarks has been studied previously [55]. However, similar to Higgs production, the dominant resonant production of the scalar states would be via gluon fusion through top quark loops due to the increased parton luminosity and enhanced couplings. The effective couplings should be of the same form as in eq. (3.7) for S_8 , but with a suppressed coupling.

We summarize the resonant states of our phenomenological interests in table 2. We propose notations for their names, give their conserved quantum numbers, leading couplings to initial state partons, and related theoretical models.

Particle Names (leading coupling)	J	$SU(3)_C$	$ Q_e $	B	Related models
$E_{3,6}^\mu (uu)$	0, 1	$\mathbf{3}, \bar{\mathbf{6}}$	$\frac{4}{3}$	$-\frac{2}{3}$	scalar/vector diquarks
$D_{3,6}^\mu (ud)$	0, 1	$\mathbf{3}, \bar{\mathbf{6}}$	$\frac{1}{3}$	$-\frac{2}{3}$	scalar/vector diquarks; \tilde{d}
$U_{3,6}^\mu (dd)$	0, 1	$\mathbf{3}, \bar{\mathbf{6}}$	$\frac{2}{3}$	$-\frac{2}{3}$	scalar/vector diquarks; \tilde{u}
$u_{3,6}^* (ug)$	$\frac{1}{2}, \frac{3}{2}$	$\mathbf{3}, \bar{\mathbf{6}}$	$\frac{2}{3}$	$\frac{1}{3}$	excited u ; quixes; stringy
$d_{3,6}^* (dg)$	$\frac{1}{2}, \frac{3}{2}$	$\mathbf{3}, \bar{\mathbf{6}}$	$\frac{1}{3}$	$\frac{1}{3}$	excited d ; quixes; stringy
$S_8 (gg)$	0	$\mathbf{8}_S$	0	0	π_{TC}, η_{TC}
$T_8 (gg)$	2	$\mathbf{8}_S$	0	0	stringy
$V_8^0 (u\bar{u}, d\bar{d})$	1	$\mathbf{8}$	0	0	axigluon; g_{KK}, ρ_{TC} ; coloron
$V_8^\pm (u\bar{d})$	1	$\mathbf{8}$	1	0	ρ_{TC}^\pm ; coloron

Table 2. Summary for resonant particle names, their quantum numbers, and possible underlying models.

4 Resonance production at the LHC

We will now give analytical formulas and present the expected numerical values of the production cross sections of the colored resonances at the LHC with 7 and 14 TeV hadronic center of momentum (c.m.) energies. The hadronic cross sections are computed by calculating the partonic cross section (σ_{ij}) and convolving it with the parton distribution functions (pdfs). We write the formula as

$$\sigma(S) = \sum_{ij} \int d\tau \frac{dL_{ij}}{d\tau} \sigma_{ij}(s), \tag{4.1}$$

$$\frac{dL_{ij}}{d\tau} \equiv (f_i \otimes f_j)(\tau) = \int_0^1 dx_1 \int_0^1 dx_2 f_i(x_1) f_j(x_2) \delta(x_1 x_2 - \tau), \tag{4.2}$$

where S (s) is hadronic (partonic) c.m. energy squared, f_i the parton i 's distribution function with a momentum fraction x_i , and $\tau = s/S$. For all numerical results here and henceforth, we have used the CTEQ6L1 pdfs [56] and set the factorization and renormalization scales the same at the resonance mass ($Q^2 = M^2$).

For a resonant production, the on-shell condition forces the partonic cross section to go like $\sigma_{ij} \sim \delta(s - M^2)$. Thus the hadronic cross section will be evaluated with the parton luminosity at $\tau = M^2/S$. We first show the partonic luminosities versus the scale at the resonance mass in figure 1 for the parton combinations of $u_1 u_2$, $d_1 d_2$, $u_1 d_2 + d_1 u_2$, $g_1 g_2$, $g_1 u_2 + u_1 g_2$, $g_1 d_2 + d_1 g_2$, $u_1 \bar{u}_2 + \bar{u}_1 u_2$, and $d_1 \bar{d}_2 + \bar{d}_1 d_2$ at (a) 7 and (b) 14 TeV LHC. As expected, initial states involving valence quarks and gluons will have the largest parton luminosities. In particular, gluons dominate at lower masses, while valence quarks take over at higher masses. The cross-over between gg and uu occurs near $M = 0.75$ (1.2) TeV at the 7 (14) TeV LHC. Not only the u quark pdf is about twice as much as that of d at low masses, but also it falls much more slowly at high masses than d . For completeness, we also include \bar{q} initial state when relevant. In fact, the cross-over of

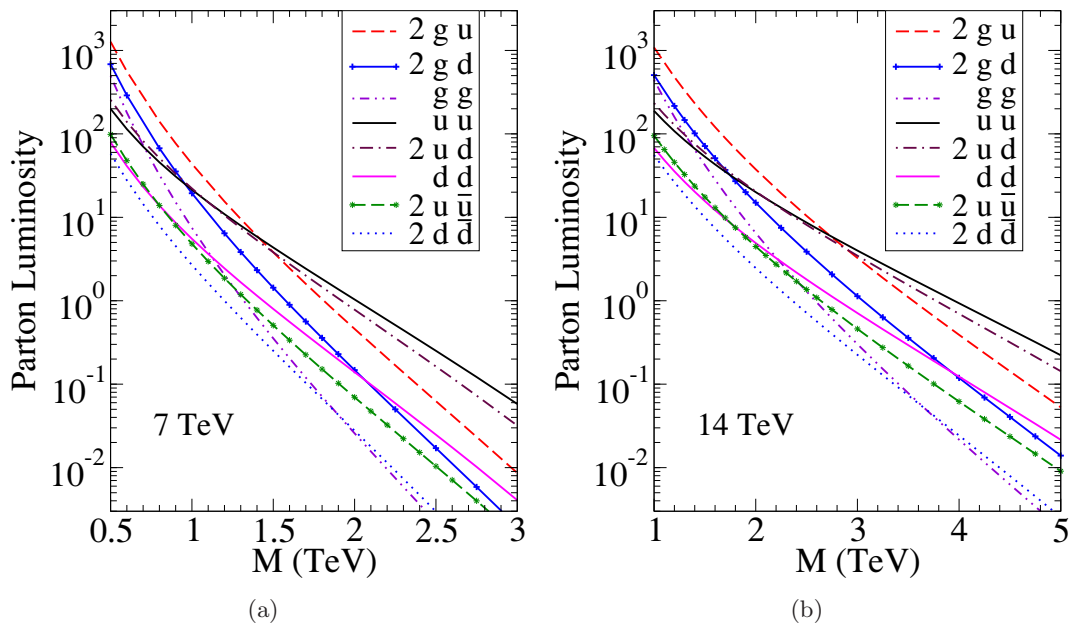


Figure 1. The parton luminosities $dL_{ij}/d\tau$ versus resonance mass at the (a) 7 TeV and (b) 14 TeV LHC.

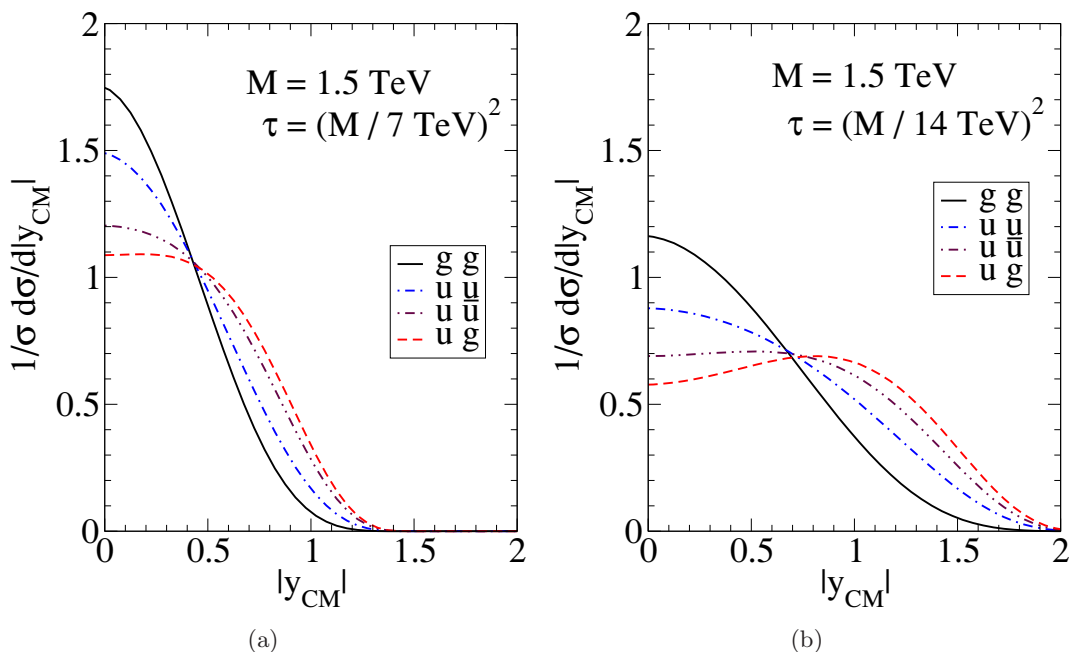


Figure 2. Center of momentum system rapidity distributions for resonance mass of 1.5 TeV and initial states $gg, uu, u\bar{u}$ and ug at the (a) 7 and (b) 14 TeV LHC.

the partonic luminosities between gg and $u\bar{u}$ occurs near $M = 1.2$ (2.2) TeV at the 7 (14) TeV LHC. The rapidity of the partonic c.m. system is also of significant interest, which is

defined as

$$y_{CM} = \frac{1}{2} \ln \frac{x_1}{x_2}. \tag{4.3}$$

We show the y_{CM} distributions at the 7 and 14 TeV LHC for $M = 1.5$ TeV in figures 2(a) and 2(b) respectively. These distributions measure the longitudinal boost due to the asymmetry between the two parton energies. The gg and uu initial states are symmetric and hence peaked at zero rapidity. Due to the up-quark being valence with a broader distribution in x , the uu initial state develops a larger discrepancy between parton momentum fractions than the gg initial state and is therefore broader. Also, the $u\bar{u}$ and ug initial states have a large imbalance in the momentum fractions and are broader than the uu and gg initial states. In fact, at the 14 TeV LHC the imbalance is so pronounced for ug that the rapidity distribution peaks at $|y_{CM}| \approx 0.9$. Since the 14 TeV LHC probes lower τ than the 7 TeV LHC, a larger discrepancy between the parton momentum fractions can develop and the rapidity distributions are considerably broader than at the 7 TeV LHC. This fact will have an impact on the experimental acceptance for the final state jets.

We consider the leading production with the resonances as listed in table 2. We do not attempt to calculate the decay of the resonances. Instead, we parameterize the production rate to dijets simply by a branching fraction (BR). Thus the total signal cross section will be governed by a coupling constant to the initial state partons, a branching fraction, and the resonance mass.

In the following calculations we employ the narrow width approximation, which is valid for $\Gamma \ll M$, where Γ and M are the total width and mass of the resonant particle, respectively. Using the interactions listed in section 3, for a resonance mass on the order of a TeV and order one couplings between the new resonance and SM partons we find $\Gamma \lesssim 0.15 M$. However, if the couplings of the resonance are large or there are many additional decay channels, the width may be sizeable and its effects will have to be included.

4.1 Quark-quark annihilation

The uu , dd , and ud initial states can annihilate into color-antitriplet and sextet spin 0 and spin 1 particles, often referred as diquarks. Based on the interactions of section 3.1 and using the Feynman rules in the appendix, for a resonant diquark mass of M the hadronic cross section from uu and dd initial states is found to be

$$\sigma_{qq} = \lambda^2 \frac{\pi N_D}{N_C^2} \frac{1}{S} (q \otimes q)(\tau_0) \tag{4.4}$$

for both scalar and vector diquarks and for the ud initial state

$$\sigma_{ud} = \lambda^2 \frac{\pi N_D}{2^2 N_C^2} \frac{1 + \delta_{1J}}{S} ((u \otimes d)(\tau_0) + (d \otimes u)(\tau_0)), \tag{4.5}$$

where the coupling constant λ specifies the resonance as in eq. (3.3) and J is the spin of the resonance. N_D is the dimension of the antitriplet ($N_D = 3$) or sextet ($N_D = 6$) representation. Here and henceforth, $\tau_0 = M^2/S$.

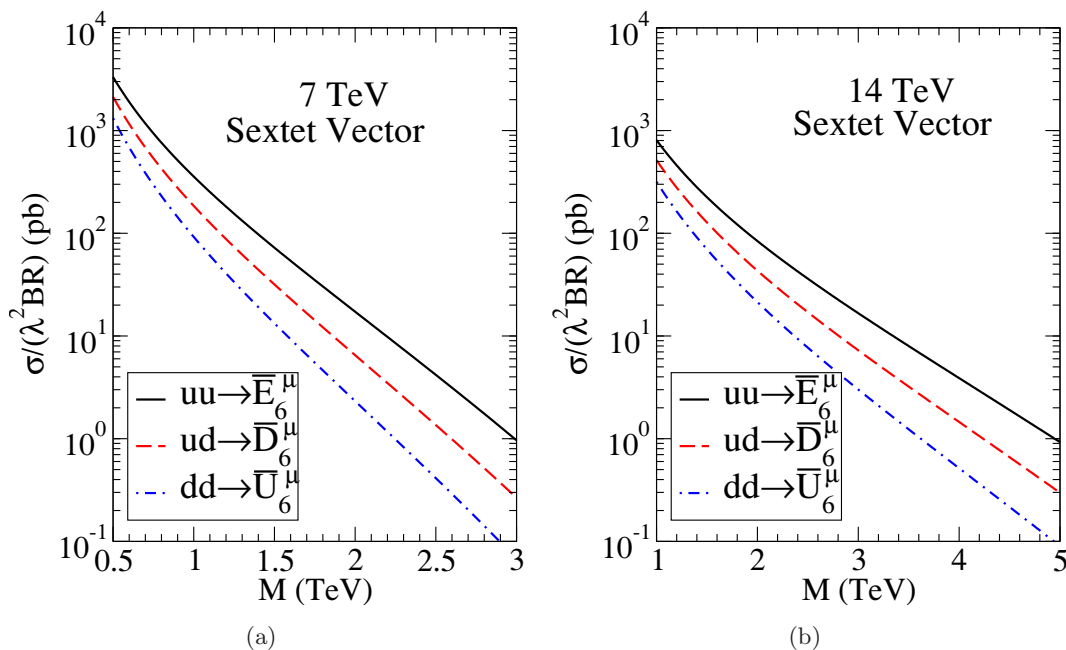


Figure 3. Dijet cross sections for color-sextet vector production via uu, ud and dd initial states versus its mass at the LHC for (a) 7 TeV and (b) 14 TeV. Subleading contributions from antiquarks for the conjugate particle production are also included. The coupling constant to initial state partons and the branching fraction to dijet have been factorized out.

The production cross sections of the color-sextet vector diquarks to dijet at a 7 TeV and 14 TeV LHC are shown in figures 3(a) and 3(b), respectively. The production cross sections of the scalars E_6, U_6 are the same as those for the vectors E_6^μ, U_6^μ while the production rate for the scalar D_6 is half that of D_6^μ .

Due to the antisymmetric factor on the quark color indices, the only non-zero valence quark configuration to give an antitriplet scalar diquark is the flavor-off diagonal contribution $ud \rightarrow \bar{D}_3$. However, the antitriplet vector diquarks can be produced from both the flavor diagonal $uu \rightarrow \bar{E}_3^\mu, dd \rightarrow \bar{U}_3^\mu$ and flavor-off diagonal $ud \rightarrow \bar{D}_3^\mu$ contributions from valence quarks. Also, since the cross section is proportional to the dimension of the diquark representation, the production cross sections for the antitriplet diquarks are half that of the respective sextet diquarks.

Besides the leading contribution from the valence quarks, we have also included the antiquark contributions for the conjugate particle production in the numerical results presented here. We summarize a few representative cross sections for the color-sextet vector diquarks, along with the percentage contribution from the antiquarks.

7 TeV LHC :	\bar{E}_6^μ	\bar{D}_6^μ	\bar{U}_6^μ
$\sigma(\text{pb}) M = 0.5 \text{ TeV}$	3400	2100	1300
$\bar{q}\bar{q}'$	2.8%	5.6%	11%
$\sigma(\text{pb}) M = 3 \text{ TeV}$	0.96	0.27	0.064
$\bar{q}\bar{q}'$	0.011%	0.028%	0.068%

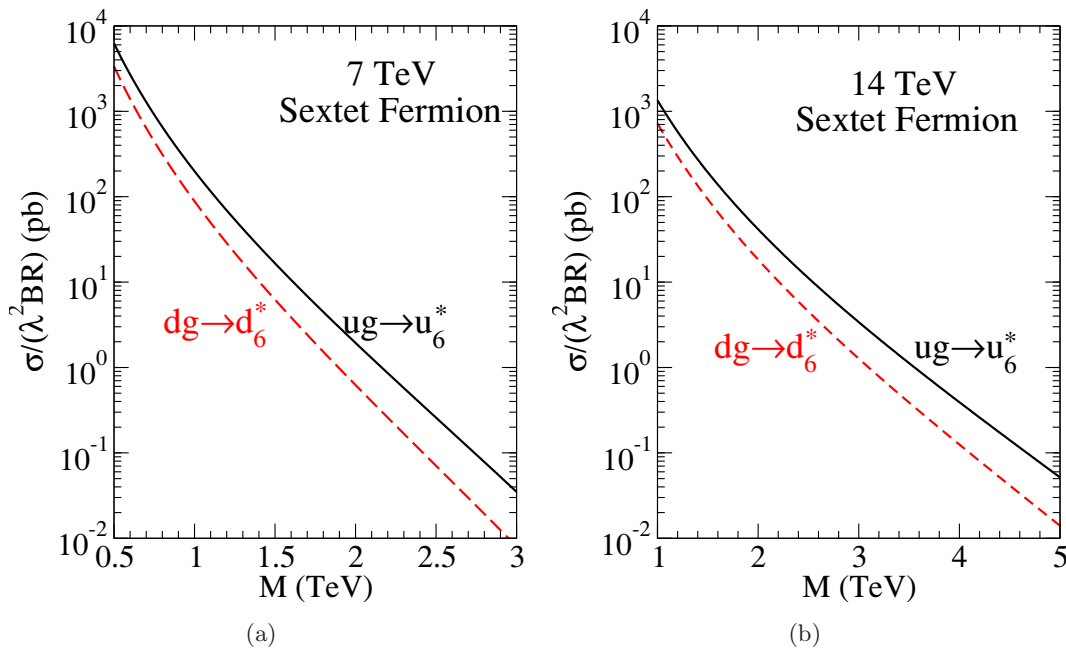


Figure 4. Dijet cross sections for color-sextet fermion production via ug and dg initial states versus its mass at the LHC for (a) 7 TeV and (b) 14 TeV. Subleading contributions from antiquarks for the conjugate particle production are also included. The coupling constant to initial state partons and the branching fraction to dijet have been factorized out. The new physics scale, Λ , has been set equal to $2M$.

14 TeV LHC :	\bar{E}_6^μ	\bar{D}_6^μ	\bar{U}_6^μ
$\sigma(\text{pb})$ $M = 1$ TeV	800	510	320
$\bar{q}\bar{q}'$	2.8%	5.5%	11%
$\sigma(\text{pb})$ $M = 5$ TeV	0.92	0.30	0.090
$\bar{q}\bar{q}'$	0.026%	0.075%	0.21%

Once again, we have pulled out the coupling constant λ^2 and the branching fraction (or equivalent to setting $\lambda^2 = \text{BR} = 1$).

The next-to-leading order (NLO) QCD corrections to scalar diquark production have been previously calculated [57] and sizable corrections were found. For instance, the cross section with masses between 0.5 and 1.5 TeV can be increased by about 20% for U_6 and 30–35% for D_3 . It is expected that the corrections to the other color-sextets and antitriplets should be similar to the above.

4.2 Quark-gluon annihilation

The ug and dg initial states can produce color-triplet and sextet excited quarks. Using the Feynman rules in the appendix, the hadronic cross section for excited quarks of mass M is

$$\sigma_{qg} = 8\pi^2 \lambda^2 \frac{\alpha_s}{N_C} \frac{M^2}{\Lambda^2} \frac{1}{S} (g \otimes q)(\tau_0), \tag{4.6}$$

where $\lambda^2 = \lambda_L^2 + \lambda_R^2$ and $\lambda_{L,R}$ specify the interactions as in eq. (3.4). Since the Clebsch-Gordan coefficients for the color-triplet and sextet states are normalized the same it follows

that the production cross sections are the same. Comparing with the convention in ref. [9, 10], the new physics scale Λ here corresponds to twice the excited quark mass.

Figure 4 presents the production cross section of excited sextet quarks u_6^* and d_6^* produced from ug and dg initial states, respectively, at the (a) 7 and (b) 14 TeV LHC. The u_6^* production rate is larger than the d_6^* production rate by about a factor of two at low mass, due to the larger u quark pdf. We have taken the cutoff $\Lambda = 2M$ in the numerical evaluation. With our CG coefficient normalization, our results should be a factor of two larger than that using the convention of [9, 10].

For the numerical results we have once again included the conjugates, produced from $\bar{u}g, \bar{d}g \rightarrow \bar{u}^*, \bar{d}^*$. Representative results for the total cross section and the percentage contribution from antiquarks, after factorizing out the overall constants, are

7 TeV LHC :	u_6^*	d_6^*
$\sigma(\text{pb}) M = 0.5 \text{ TeV}$	6200	3400
$\bar{q}g$	8.5%	20%
$\sigma(\text{pb}) M = 3 \text{ TeV}$	0.035	0.0080
$\bar{q}g$	0.82%	2.6%
14 TeV LHC :	u_6^*	d_6^*
$\sigma(\text{pb}) M = 1 \text{ TeV}$	1300	720
$\bar{q}g$	8.4%	20%
$\sigma(\text{pb}) M = 5 \text{ TeV}$	0.052	0.014
$\bar{q}g$	1.2%	4.2%

4.3 Gluon-gluon annihilation

Gluon-gluon annihilation can result in color-octet scalars and tensors. Using the parameterization of eq. (3.7) and Feynman rules in the appendix, the hadronic production cross section of a color-octet scalar and tensor of mass M from gluon-gluon fusion is

$$\sigma_{gg} = 4\pi^2 \alpha_s \kappa^2 \frac{N_C^2 - 4}{N_C(N_C^2 - 1)} \frac{M^2}{\Lambda^2} \frac{1 + \delta_{0J}}{S} (g \otimes g)(\tau_0), \quad (4.7)$$

where κ and Λ are specified by the interaction. Since on-shell tensor polarizations are traceless, the $T_8^\rho{}_\rho$ term in eq. (3.7) does not contribute to the resonant production of the color-octet tensor.

The production cross sections for the color-octet scalar to dijets are presented in figure 5 for the LHC at 7 TeV (dashed curve) and 14 TeV (solid curve). For the numerical results presented the new physics scale Λ has been set equal to the resonant mass. The color-octet tensor cross section is one half that of the the color-octet scalar. Since the gluon luminosity falls fast at a higher mass, the cross section at 7 TeV LHC drops by more than five orders of magnitude from 6000 pb at $M = 0.5 \text{ TeV}$ to 0.02 pb at $M = 2.5 \text{ TeV}$, and at 14 TeV LHC by about five orders of magnitude from 1200 pb at $M = 1 \text{ TeV}$ to 0.01 pb at $M = 4.6 \text{ TeV}$.

The next-to-leading logarithm (NLL) soft-gluon resummation correction to scalar octet production via gluon fusion has been previously calculated and sizable corrections were

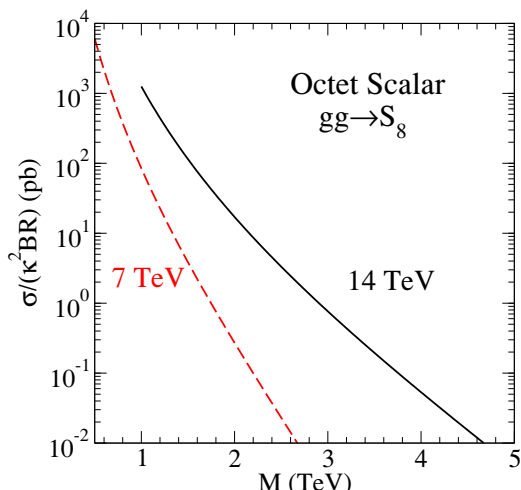


Figure 5. Dijet cross sections for color-octet scalar production via gg initial states versus its mass at the LHC for 7 TeV (dashed curve) and 14 TeV (solid curve). The coupling constant to initial state partons and the branching fraction to dijet have been factorized out. The new physics scale, Λ , has been set equal to M .

found [53]. The cross section can be increased by a factor of 2.4 at mass 0.5 TeV and 3.5 at a mass of 2.5 TeV.

4.4 Quark-antiquark annihilation

Although the parton luminosity is lower than the previously discussed initial states, we also include resonant production from $u\bar{u}$, $d\bar{d}$, $u\bar{d}$, and $d\bar{u}$ initial states. These states can couple to color-octet vectors. Using the interactions in eq. (3.10), the production cross section for a color-octet vector of mass M from $q\bar{q}'$ initial states is

$$\sigma_{q\bar{q}'} = 4\pi^2 g^2 \alpha_s \frac{C_F}{N_C} \frac{1}{S} (q \otimes \bar{q}') (\tau_0) \tag{4.8}$$

where

$$g^2 = \begin{cases} \frac{1}{2} (|C_L V_L^{CKM}|^2 + |C_R V_R^{CKM}|^2) & \text{for charged states,} \\ \frac{1}{2} (|g_L^{U,D}|^2 + |g_R^{U,D}|^2) & \text{for neutral states.} \end{cases}$$

The color factor $C_F = (N_C^2 - 1)/2N_C = 4/3$.

The cross sections for color-octet vectors are presented in figure 6 for the (a) 7 TeV and (b) 14 TeV LHC. Since the u quark pdf is greater than the d quark pdf, the neutral vectors are produced more favorably by the $u\bar{u}$ initial state than by $d\bar{d}$. Due to the \bar{d} quark pdf being larger than the \bar{u} quark pdf, the production of V_8^+ is larger than the production rate of V_8^0 from $u\bar{u}$ initial state and V_8^0 production rate from $d\bar{d}$ initial state is larger than

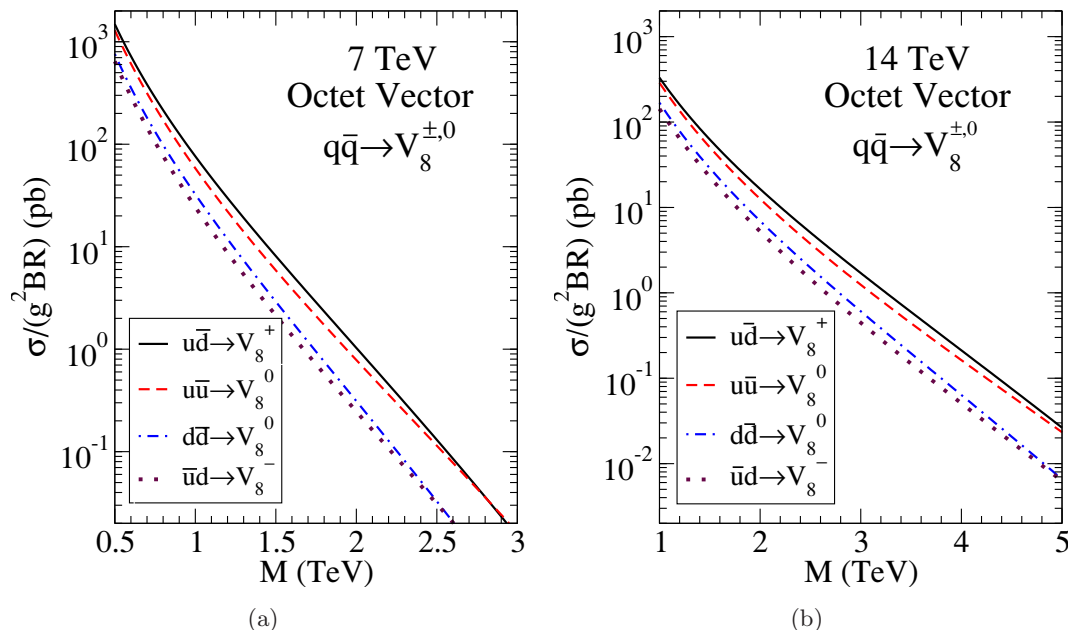


Figure 6. Dijet cross sections for color-octet vector production via $u\bar{d}$, $u\bar{u}$, $d\bar{d}$, and $d\bar{u}$ initial states versus its mass at the LHC for (a) 7 TeV and (b) 14 TeV. The coupling constant to initial state partons and the branching fraction to dijet have been factorized out.

the production rate of V_8^- . Some representative cross sections values are listed below.

7 TeV LHC :	$u\bar{d} \rightarrow V_8^+$	$d\bar{u} \rightarrow V_8^-$	$u\bar{u} \rightarrow V_8^0$	$d\bar{d} \rightarrow V_8^0$
$\sigma(\text{pb}) M = 0.5 \text{ TeV}$	1500	640	1300	760
$\sigma(\text{pb}) M = 3 \text{ TeV}$	0.015	0.0037	0.016	0.0030
14 TeV LHC :	$u\bar{d} \rightarrow V_8^+$	$d\bar{u} \rightarrow V_8^-$	$u\bar{u} \rightarrow V_8^0$	$d\bar{d} \rightarrow V_8^0$
$\sigma(\text{pb}) M = 1 \text{ TeV}$	330	140	290	170
$\sigma(\text{pb}) M = 5 \text{ TeV}$	0.026	0.0063	0.023	0.0066

Once again, we have pulled out the coupling constant λ^2 and the branching fraction (or equivalent to setting $\lambda^2 = \text{BR} = 1$).

All the cross sections presented in this section are at leading order in QCD. The production cross section of colored resonance can receive sizable QCD corrections as shown for the color-triplet and sextet scalar diquarks [57] and color octet scalars [53]. We will take this into account when setting the bounds.

Throughout this paper, we neglect the color-singlet states, such as Z' , W' or KK gravitons. Our formalism for is equally applicable to those by adjusting the couplings $g_s \rightarrow e/\sin\theta_W$ and setting the color factor C_F to 1. Before folding in the decay branching fraction to the final state, the production rates for a color-singlet state would be smaller than the colored resonance by roughly about a factor of 30.

5 Bounds from the LHC Dijet spectrum

Searching for new physics signals in the dijet spectrum at hadron colliders has been long carried out. The Tevatron [58] and LHC [59, 60] experiments have both utilized measurement of the dijet angular distribution to bound the strength of four-fermion contact interactions. The standard form of the four-fermion contact interaction in the literature is [61]:

$$\mathcal{L}_{4q} = \frac{2\pi}{\Lambda^2} \bar{q}_L \gamma^\mu q_L \bar{q}_L \gamma_\mu q_L \quad (5.1)$$

For a sufficiently high mass, the new resonant states can be integrated out and the $\mathbf{3} \otimes \mathbf{3}$ and $\mathbf{3} \otimes \bar{\mathbf{3}}$ vector interactions can produce similar interactions to eq. (5.1). The bounds on the four fermion interactions can be roughly translated into bounds on our interactions with the identification

$$\frac{2\pi}{\Lambda^2} \sim \frac{\lambda^2}{2M^2}, \quad (5.2)$$

where M is the mass of the resonant state of our current interest. Assuming a coupling constant of unity, the current LHC bound of $\Lambda \geq 4$ TeV translates into

$$M \gtrsim 1.1 \text{ TeV}.$$

Note this bound is only a rough estimate since one would have to be careful in computing the color factor and counting the contributing light partons.

Using measurements of dijet production rates at 7 TeV LHC, the ATLAS and CMS collaborations have recently released bounds on the dijet production cross sections as a function of resonance mass based on the first data of 3.1 pb^{-1} [28] and 2.9 pb^{-1} [29], respectively. Even with such small amount of initial data, the LHC experiments have gone beyond the existing Tevatron results, pushing the LHC to the phase of discovery for new physics.

We model the experimental efficiencies by a simple parameterization. The detector acceptance for dijet events at ATLAS was about 31% for an excited quark mass around 300 GeV, and about 48% around 1700 GeV. For our study we model this acceptance as

$$\mathcal{A}_{ATLAS} = \begin{cases} \frac{0.17}{1400 \text{ GeV}}(m - 300 \text{ GeV}) + 0.31 & m \leq 1700 \text{ GeV} \\ 0.48 & m > 1700 \text{ GeV} \end{cases} \quad (5.3)$$

To model the CMS detector acceptances we compared our results for dijet production cross section without detector acceptance to the the CMS results including detector acceptance. Using their axigluon and excited quark results, we model the CMS detector acceptance as

$$\mathcal{A}_{CMS} = \frac{\Delta}{2100 \text{ GeV}}(m - 500 \text{ GeV}) + 0.47, \quad (5.4)$$

where $\Delta = 0.08$ for the quark-quark final state and $\Delta = 0.17$ for the quark-gluon final state. There was no analogous data to find the acceptance for gluon-gluon final states. We therefore also use the quark-gluon acceptance for the gluon-gluon final state.

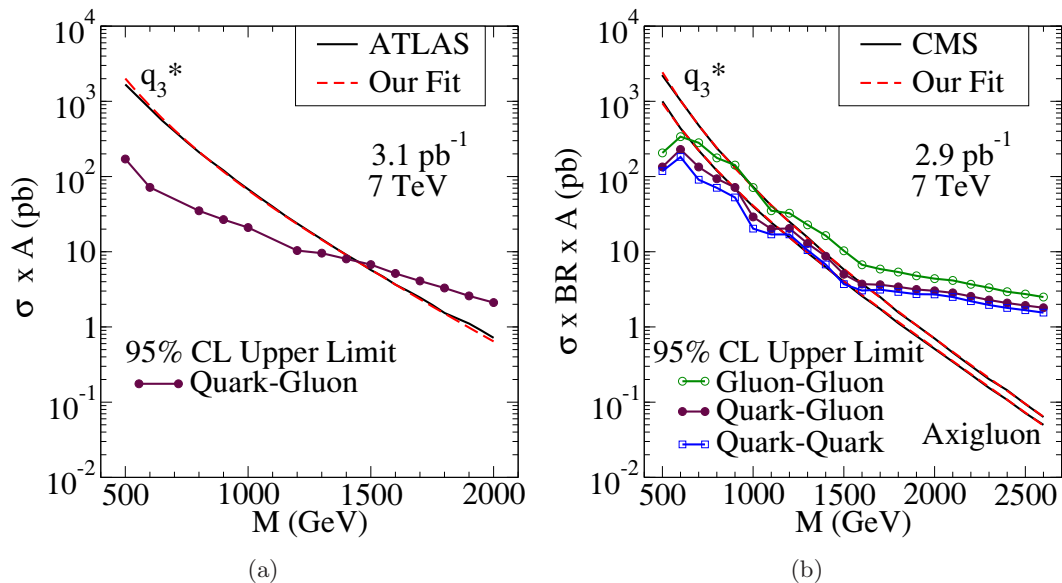


Figure 7. 95% confidence level upper limits on dijet production cross sections versus resonant mass for (a) ATLAS results (solid circles) and (b) CMS results from the contributions of gluon-gluon (open circles), quark-gluon (solid circles), and quark-quark (open boxes). Our fits (dashed curve) almost overlap with the theoretical predictions (solid curves) provided by ATLAS for q_3^* and CMS for q_3^* and axigluon.

The predicted dijet cross sections for triplet excited quarks at ATLAS and triplet excited quarks and axigluons at CMS are presented by the solid curves in figures 7(a) and 7(b), respectively. To reproduce their results for the triplet excited quark production, we set $\lambda = 1$ in eq. (4.6) and summed over all possible initial state quarks. As can be seen, using the acceptances in eqs. (5.3) and (5.4), our simulations (dashed curves) fit well the results provided by the ATLAS and CMS collaborations (solid curves). The current 95% confidence level upper limits for dijet production cross sections at both ATLAS and CMS are also presented in figure 7.

All of the colored resonances presented in the previous sections can contribute to the dijet signal; hence, the ATLAS and CMS dijet cross section bounds can be used to place limits on the mass and couplings of these new particles. We consider the current bounds on those colored resonances as summarized in table 2. In presenting our results for the current bound, we once again parameterize the signal rates by an overall coupling to the initial state partons and a branching fraction to decay to the final state dijets. The limits on the product of the two constants of new colored resonances as a function of the resonant mass are shown in figure 8. The color-sextet vector diquark and color-octet scalar bounds are based on the leading order QCD calculations presented here with K-factors from QCD corrections, while all other bounds are based solely on the leading order calculations. The regions above the corresponding curves are excluded, thus providing meaningful upper bounds for the couplings and lower bounds for the resonant masses. The zigzag shapes of the curves are due to the non-smooth experimental bounds for different masses as in figure 7(b).

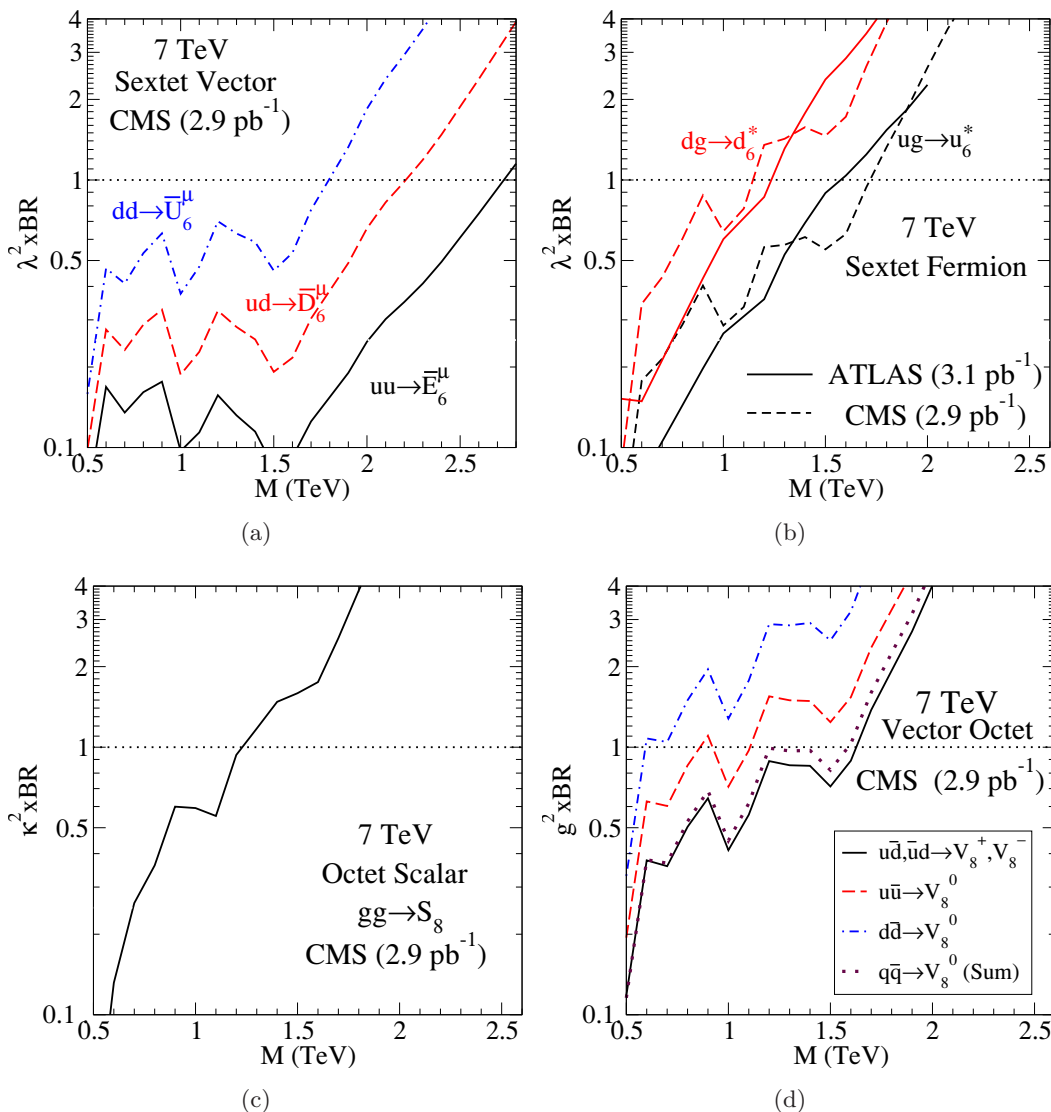


Figure 8. Bounds on the products of SM parton couplings to the resonances and dijet branching ratios (vertical axis) versus the resonant mass for (a) color-sextet vector diquarks, (b) color-sextet (or color-triplet) excited quarks, (c) color-octet scalar, and (d) color-octet vectors from (a,b,c,d) CMS and (b) ATLAS.

Figure 8(a)² shows the CMS bounds on the sextet vector diquarks with a NLO K-factor of 1.2 included [57]. The bounds on the scalar U_6, E_6 couplings are the same as those on vector U_6^μ, E_6^μ and the bounds on the D_6 couplings are twice weaker than the bound on D_6^μ . Furthermore, taking into account the different K-factors of 1.3 for the triplets and 1.2 for the sextets, the bound on the antisextet vectors are 1.8 times stronger than the bounds on the triplet vectors and the bounds on D_6^μ are 3.7 times stronger than D_3 .

Figure 8(b) shows the bounds on the excited quarks. Results based on the ATLAS data

²We have extended the E_6^μ bound beyond the CMS data point at 2.6 TeV, assuming there has been no event observed.

(solid curves) and CMS data (dashed curves) are comparable. Following the convention in ref. [9, 10], we have set $\Lambda = 2M$. As noted earlier, the results for a color-triplet and sextet are the same. The bounds obtained here are stronger than those for the diquarks above.

Figure 8(c) shows the bounds on octet scalar couplings including NLL K-factors running from 2.4 at resonance mass 0.5 TeV and 3.5 at 2.5 TeV [53]. Even with the K-factor, the weakest bound of all studied are the gg initial processes. This is due to the sharp fall of gg luminosity at higher masses. The bounds on the coupling constants of the T_8 are a factor of two weaker than those of the S_8 .

Although not as large as uu , dd initial states, the $q\bar{q}$ annihilation provides reasonable sensitivity to the colored resonances. In comparison with the Tevatron as a $p\bar{p}$ collider, the LHC is somewhat in a disadvantageous situation with respect to the valence quark dominance. Nevertheless, the LHC results currently have slightly extended the Tevatron bounds on axigluons and universal colorons [29]. We also obtain significant bounds for the color-octet resonances based on the CMS data as seen in figure 8(d). However, due to the much larger data sample, the Tevatron dijet bounds for color-singlet vectors (Z' , W' etc.) are much more stringent than those from the LHC.

Assuming a coupling constant and branching ratio of unity as indicated by the horizontal dotted lines in figure 8, the current mass lower bounds on the colored resonant states are summarized as

E_6^μ	2.7 TeV (CMS)	E_6	2.7 TeV
D_6^μ	2.3 TeV (CMS)	D_6	1.9 TeV
U_6^μ	1.8 TeV (CMS)	U_6	1.8 TeV
E_3^μ	2.5 TeV (CMS)	U_3^μ	0.8, 1.0 – 1.2, 1.4 – 1.6 TeV
D_3^μ	1.9 TeV (CMS)	D_3	0.8, 0.9 – 1.2, 1.3 – 1.7 TeV
u_6^*	1.7 TeV (CMS), 1.6 TeV (ATLAS)	d_6^*	1.1 TeV, 1.2 TeV
V_8^\pm	1.6 TeV (CMS)	V_8^0	1.6 TeV
S_8	1.2 TeV (CMS)	T_8	0.9 TeV ,

where the mass bounds have been rounded to the nearest tenth of a TeV. All of the bounds obtained here are beyond the existing Tevatron analyses.

It should be noted that there are small uncertainties associated with the results above. For instance, the bounds presented above have been obtained by utilizing the narrow width approximation. Also, the detector acceptances are somewhat dependent on the spin of the resonance.

6 Conclusion

Experiments at the LHC have opened up the energy frontier for TeV scale new physics searches. Motivated by the recent ATLAS and CMS dijet analyses, we study the possible

colored resonances in a most general approach. We classify the colored resonances based on group theory decomposition of QCD $SU(3)_C$ interaction as well as other quantum numbers, as listed in table 1. These resonances may carry exotic SM quantum numbers, but all of them find their interesting roles in certain theories beyond the SM.

We then construct their effective couplings to light partons. Based on those features, we name them and list them in table 2. We calculate their resonant production cross section at the LHC. The production rates may be as large as 400 pb (1000 pb) at the c.m. energy of 7 (14) TeV for a mass of 1 TeV, leading to the largest production rates for new physics at the TeV scale, and simplest event topology with dijet final states. Our approach is quite general and applicable to other possible signals of resonant particles other than dijets at the LHC.

We applied the new ATLAS/CMS dijet data to put bounds on various possible colored resonant states. We obtained the lower bounds on their masses ranging from 0.9 to 2.7 TeV, if their couplings are of the order of unity. The results obtained here are beyond the existing Tevatron analyses. In an optimal situation, if a signal above the SM backgrounds is established in the near future, it is then the exciting time to determine the nature of the resonance particle and to untangle the new underlying theory as commented in the text and in table 2. With the anticipated increase of integrated luminosity and c.m. energy, experiments at the LHC will undoubtedly take our understanding of particle physics to an unprecedented level.

Acknowledgments

We would like to thank Georgios Choudalakis, Fabio Maltoni, Tim Tait, and Brian Yencho for discussions. I.L. is supported by a DOE Graduate Fellowship in High Energy Theory. This work was supported in part by the US DOE under contract No. DE-FG02-95ER40896.

A Clebsch-Gordan coefficients

Here we exhibit the Clebsch-Gordan Coefficients relations that are needed in color resonance calculation for general $SU(N)$ groups. Typical initial state group structure includes $N \otimes N$, $N \otimes \bar{N}$, $N \otimes A$ and $A \otimes A$, whereas A denotes the adjoint representation of $SU(N)$.

We assume that the Clebsch-Gordan coefficients obey the following orthogonality relationship:

$$\text{Tr}[K^a \bar{K}_b] = \delta_b^a, \tag{A.1}$$

where $K^a = \bar{K}_a^\dagger$. The Clebsch-Gordan coefficients couple the different irreducible representations together in a gauge invariant way. Hence, depending on the interaction, the indices a take on different values. For example, according to our conventions in eqs. (3.3)

and (3.4):

$$a = \begin{cases} 1, \dots, \frac{N(N-1)}{2} & \text{couplings to the antisymmetric combination of } N \otimes N \text{ boson} \\ 1, \dots, \frac{N(N+1)}{2} & \text{couplings to the symmetric combination of } N \otimes N \text{ boson} \\ 1, \dots, N^2 - 1 & \text{couplings to the new fermion from } N \otimes A \end{cases} \quad (\text{A.2})$$

Using this orthogonality condition, the following identities are used for the appropriate couplings:

$$\text{Tr}[K^a \bar{K}_a] = \begin{cases} \frac{N(N-1)}{2} & \text{couplings to the antisymmetric combination of } N \otimes N \text{ boson} \\ \frac{N(N+1)}{2} & \text{couplings to the symmetric combination of } N \otimes N \text{ boson} \\ N^2 - 1 & \text{couplings to the new fermion from } N \otimes A \end{cases} \quad (\text{A.3})$$

Specifically for SU(3) couplings, the color antisymmetric (symmetric) coupling of two quarks is the triplet-(sextet) scalar or vector diquark. Then we have for the diquark interactions in eq. (3.3) and excited quark interactions in eq. (3.4)

$$\text{Tr}[K^a \bar{K}_a] = \begin{cases} 3 & \text{couplings to the triplet diquark} \\ 6 & \text{couplings to the sextet diquark} \\ 8 & \text{couplings to the triplet and sextet excited quarks} \end{cases} \quad (\text{A.4})$$

The complete symmetric invariant symbol of SU(3) algebra satisfy

$$d^{ABC} d^{ABC} = 2C_F(N^2 - 4) \quad (\text{A.5})$$

where as $C_F = (N^2 - 1)/2N$ is the eigenvalue of the quadratic SU(N) Casimir operator acting on the fundamental representation. For SU(3), $C_F = 4/3$.

B Feynman rules

Here we give the explicit Feynman rules for the interacting vertices constructed in the text, as in section 3.

The diquark Feynman rules are in eq. (B.1) and (B.2): Q_{N_D} may be E_{N_D}, D_{N_D} , or U_{N_D} , depending on the initial state. The labels $q, q' = u, d$ indicate whether the initial state quarks are up-type or down-type and α, β are generation indices. For the triplet diquark the Clebsch-Gordan coefficients are antisymmetric $K_{ab}^j = -K_{ba}^j$, and for the antisextet diquark they are symmetric $K_{ab}^j = K_{ba}^j$. C is the charge conjugation matrix.

The excited quark Feynman rules in eq. (B.3): equally applicable for both $u_{N_D}^*$ and $d_{N_D}^*$.

The spin summation for a spin-2 tensor state (T_8^A) of mass M obeys the relation [62]:

$$\begin{aligned} \Sigma \epsilon_{\mu\nu}(k) \epsilon_{\rho\sigma}^*(k) &= B_{\mu\nu, \rho\sigma}(k) = \left(g_{\mu\rho} - \frac{k_\mu k_\rho}{M^2} \right) \left(g_{\nu\sigma} - \frac{k_\nu k_\sigma}{M^2} \right) \\ &+ \left(g_{\mu\sigma} - \frac{k_\mu k_\sigma}{M^2} \right) \left(g_{\nu\rho} - \frac{k_\nu k_\rho}{M^2} \right) - \frac{2}{3} \left(g_{\mu\nu} - \frac{k_\mu k_\nu}{M^2} \right) \left(g_{\rho\sigma} - \frac{k_\rho k_\sigma}{M^2} \right). \end{aligned}$$

$$\begin{aligned}
 & \text{Diagram (B.1)} \quad -i(1 + \delta_{qq'}) \lambda_{\alpha\beta}^{Q_{ND}} K_{ab}^j C P_\tau \quad (\text{B.1}) \\
 & \text{Diagram (B.2)} \quad \begin{aligned} q = q' : & -i \lambda_{\alpha\beta}^{iQ_{ND}} (K_{ab}^j P_R - K_{ba}^j P_L) C \gamma_\mu \\ q \neq q' : & -i \lambda_{\alpha\beta}^{iD_{ND}} K_{ab}^j P_\tau C \gamma_\mu \end{aligned} \quad (\text{B.2}) \\
 & \text{Diagram (B.3)} \quad -2i \frac{g_s}{\Lambda} K_{ND,A} (\not{k} \gamma_\mu - k_\mu) (\lambda_L^U P_L + \lambda_R^U P_R) \quad (\text{B.3}) \\
 & \text{Diagram (B.4)} \quad -4i g_s d^{ABC} \frac{\kappa_S}{\Lambda_S} ((k_1 \cdot k_2) g_{\mu\nu} - k_{2\mu} k_{1\nu}) \quad (\text{B.4}) \\
 & \text{Diagram (B.5)} \quad \begin{aligned} & -2i g_s d^{ABC} \frac{\kappa_T}{\Lambda_T} (k_{1\alpha} k_{2\beta} g_{\mu\nu} - k_{1\nu} k_{2\beta} g_{\alpha\mu} \\ & + (k_1 \cdot k_2) g_{\alpha\mu} g_{\beta\nu} - k_{1\alpha} k_{2\mu} g_{\beta\nu} \\ & + 2f g_{\alpha\beta} ((k_1 \cdot k_2) g_{\mu\nu} - k_{2\mu} k_{1\nu})) \end{aligned} \quad (\text{B.5}) \\
 & \text{Diagram (B.6)} \quad \begin{aligned} V_8^0 : & -i g_s T^A \gamma^\mu (g_L^{U/D} P_L + g_R^{U/D} P_R) \\ V_8^+ : & -i g_s T^A \gamma^\mu (C_L V_L^{CKM} P_L + C_R V_R^{CKM} P_R) \end{aligned} \quad (\text{B.6})
 \end{aligned}$$

Figure 9. Feynman rules for the vertices of resonant particle couplings to quarks and gluons. All the momenta are incoming and $\tau = L, R$.

References

- [1] R. Barbier et al., *R-parity violating supersymmetry*, *Phys. Rept.* **420** (2005) 1 [[hep-ph/0406039](#)] [[SPIRES](#)].
- [2] J.L. Hewett and T.G. Rizzo, *Low-energy phenomenology of superstring inspired E_6 models*, *Phys. Rept.* **183** (1989) 193 [[SPIRES](#)].
- [3] J.C. Pati and A. Salam, *Lepton number as the fourth color*, *Phys. Rev.* **D 10** (1974) 275 [*Erratum ibid.* **D 11** (1975) 703] [[SPIRES](#)].
- [4] R.N. Mohapatra and R.E. Marshak, *Local B-L symmetry of electroweak interactions, Majorana neutrinos and neutron oscillations*, *Phys. Rev. Lett.* **44** (1980) 1316 [*Erratum ibid.* **44** (1980) 1643] [[SPIRES](#)].
- [5] Z. Chacko and R.N. Mohapatra, *Supersymmetric $SU(2)_L \times SU(2)_R \times SU(4)_c$ and observable neutron antineutron oscillation*, *Phys. Rev.* **D 59** (1999) 055004 [[hep-ph/9802388](#)] [[SPIRES](#)].
- [6] N. Cabibbo, L. Maiani and Y. Srivastava, *Anomalous Z decays: excited leptons?*, *Phys. Lett.* **B 139** (1984) 459 [[SPIRES](#)].

- [7] A. De Rujula, L. Maiani and R. Petronzio, *Search for excited quarks*, *Phys. Lett. B* **140** (1984) 253 [SPIRES].
- [8] J.H. Kuhn and P.M. Zerwas, *Excited quarks and leptons*, *Phys. Lett. B* **147** (1984) 189 [SPIRES].
- [9] U. Baur, I. Hinchliffe and D. Zeppenfeld, *Excited quark production at hadron colliders*, *Int. J. Mod. Phys. A* **2** (1987) 1285 [SPIRES].
- [10] U. Baur, M. Spira and P.M. Zerwas, *Excited quark and lepton production at hadron colliders*, *Phys. Rev. D* **42** (1990) 815 [SPIRES].
- [11] P.H. Frampton and S.L. Glashow, *Chiral color: an alternative to the standard model*, *Phys. Lett. B* **190** (1987) 157 [SPIRES].
- [12] S.P. Martin, *A Tumbling top quark condensate model*, *Phys. Rev. D* **46** (1992) 2197 [hep-ph/9204204] [SPIRES].
- [13] C.T. Hill and E.H. Simmons, *Strong dynamics and electroweak symmetry breaking*, *Phys. Rept.* **381** (2003) 235 [Erratum *ibid.* **390** (2004) 553] [hep-ph/0203079] [SPIRES].
- [14] B.A. Dobrescu, K. Kong and R. Mahbubani, *Leptons and photons at the LHC: Cascades through spinless adjoints*, *JHEP* **07** (2007) 006 [hep-ph/0703231] [SPIRES].
- [15] B.A. Dobrescu, K. Kong and R. Mahbubani, *Massive color-octet bosons and pairs of resonances at hadron colliders*, *Phys. Lett. B* **670** (2008) 119 [arXiv:0709.2378] [SPIRES].
- [16] J. Bagger, C. Schmidt and S. King, *Axigluon production in hadronic collisions*, *Phys. Rev. D* **37** (1988) 1188 [SPIRES].
- [17] C.T. Hill, *Topcolor: top quark condensation in a gauge extension of the standard model*, *Phys. Lett. B* **266** (1991) 419 [SPIRES].
- [18] C.T. Hill and S.J. Parke, *Top production: sensitivity to new physics*, *Phys. Rev. D* **49** (1994) 4454 [hep-ph/9312324] [SPIRES].
- [19] R.S. Chivukula, A.G. Cohen and E.H. Simmons, *New strong interactions at the Tevatron?*, *Phys. Lett. B* **380** (1996) 92 [hep-ph/9603311] [SPIRES].
- [20] K. Agashe, A. Belyaev, T. Krupovnickas, G. Perez and J. Virzi, *LHC signals from warped extra dimensions*, *Phys. Rev. D* **77** (2008) 015003 [hep-ph/0612015] [SPIRES].
- [21] B. Lillie, L. Randall and L.-T. Wang, *The Bulk RS KK-gluon at the LHC*, *JHEP* **09** (2007) 074 [hep-ph/0701166] [SPIRES].
- [22] B. Lillie, J. Shu and T.M.P. Tait, *Kaluza-Klein gluons as a diagnostic of warped models*, *Phys. Rev. D* **76** (2007) 115016 [arXiv:0706.3960] [SPIRES].
- [23] S. Cullen, M. Perelstein and M.E. Peskin, *TeV strings and collider probes of large extra dimensions*, *Phys. Rev. D* **62** (2000) 055012 [hep-ph/0001166] [SPIRES].
- [24] P. Burikham, T. Figy and T. Han, *TeV-scale string resonances at hadron colliders*, *Phys. Rev. D* **71** (2005) 016005 [Erratum *ibid.* **D 71** (2005) 019905] [hep-ph/0411094] [SPIRES].
- [25] Z. Dong, T. Han, M.-x. Huang and G. Shiu, *Top quarks as a window to string resonances*, *JHEP* **09** (2010) 048 [arXiv:1004.5441] [SPIRES].
- [26] L.A. Anchordoqui, H. Goldberg and T.R. Taylor, *Decay widths of lowest massive Regge excitations of open strings*, *Phys. Lett. B* **668** (2008) 373 [arXiv:0806.3420] [SPIRES].

- [27] L.A. Anchordoqui et al., *Dijet signals for low mass strings at the LHC*, *Phys. Rev. Lett.* **101** (2008) 241803 [[arXiv:0808.0497](#)] [[SPIRES](#)].
- [28] ATLAS collaboration and others, *Search for new particles in two-jet final states in 7 TeV proton-proton collisions with the ATLAS detector at the LHC*, ATLAS-CONF-2010-093, *Phys. Rev. Lett.* **105** (2010) 161801 [[arXiv:1008.2461](#)] [[SPIRES](#)].
- [29] CMS collaboration, V. Khachatryan et al., *Search for Dijet resonances in 7 TeV pp Collisions at CMS*, *Phys. Rev. Lett.* **105** (2010) 211801 [[arXiv:1010.0203](#)] [[SPIRES](#)].
- [30] R.S. Chivukula, M. Golden and E.H. Simmons, *Six jet signals of highly colored fermions*, *Phys. Lett. B* **257** (1991) 403 [[SPIRES](#)].
- [31] C.W. Bauer, Z. Ligeti, M. Schmaltz, J. Thaler and D.G.E. Walker, *Supermodels for early LHC*, *Phys. Lett. B* **690** (2010) 280 [[arXiv:0909.5213](#)] [[SPIRES](#)].
- [32] R. Barbieri and R. Torre, *Signals of single particle production at the earliest LHC*, [arXiv:1008.5302](#) [[SPIRES](#)].
- [33] V. Barger, T. Han and D.G.E. Walker, *Top quark pairs at high invariant mass: A model-independent discriminator of new physics at the LHC*, *Phys. Rev. Lett.* **100** (2008) 031801 [[hep-ph/0612016](#)] [[SPIRES](#)].
- [34] R. Frederix and F. Maltoni, *Top pair invariant mass distribution: a window on new physics*, *JHEP* **01** (2009) 047 [[arXiv:0712.2355](#)] [[SPIRES](#)].
- [35] E. Ma, M. Raidal and U. Sarkar, *Probing the exotic particle content beyond the standard model*, *Eur. Phys. J. C* **8** (1999) 301 [[hep-ph/9808484](#)] [[SPIRES](#)].
- [36] E. Del Nobile, R. Franceschini, D. Pappadopulo and A. Strumia, *Minimal matter at the large hadron collider*, *Nucl. Phys. B* **826** (2010) 217 [[arXiv:0908.1567](#)] [[SPIRES](#)].
- [37] R.S. Chivukula and H. Georgi, *Composite technicolor standard model*, *Phys. Lett. B* **188** (1987) 99 [[SPIRES](#)].
- [38] G. D'Ambrosio, G.F. Giudice, G. Isidori and A. Strumia, *Minimal flavour violation: An effective field theory approach*, *Nucl. Phys. B* **645** (2002) 155 [[hep-ph/0207036](#)] [[SPIRES](#)].
- [39] J.M. Arnold, M. Pospelov, M. Trott and M.B. Wise, *Scalar representations and minimal flavor violation*, *JHEP* **01** (2010) 073 [[arXiv:0911.2225](#)] [[SPIRES](#)].
- [40] R.N. Mohapatra, N. Okada and H.-B. Yu, *Diquark higgs at LHC*, *Phys. Rev. D* **77** (2008) 011701 [[arXiv:0709.1486](#)] [[SPIRES](#)].
- [41] K.S. Babu, R.N. Mohapatra and S. Nasri, *Unified TeV scale picture of baryogenesis and dark matter*, *Phys. Rev. Lett.* **98** (2007) 161301 [[hep-ph/0612357](#)] [[SPIRES](#)].
- [42] S. Atag, O. Cakir and S. Sultansoy, *Resonance production of diquarks at the CERN LHC*, *Phys. Rev. D* **59** (1999) 015008 [[SPIRES](#)].
- [43] E. Arik, O. Cakir, S.A. Cetin and S. Sultansoy, *A search for vector diquarks at the CERN LHC*, *JHEP* **09** (2002) 024 [[hep-ph/0109011](#)] [[SPIRES](#)].
- [44] O. Cakir and M. Sahin, *Resonant production of diquarks at high energy pp, ep and e⁺e⁻ colliders*, *Phys. Rev. D* **72** (2005) 115011 [[hep-ph/0508205](#)] [[SPIRES](#)].
- [45] E.L. Berger, Q.-H. Cao, C.-R. Chen, G. Shaughnessy and H. Zhang, *Color sextet scalars in early LHC experiments*, *Phys. Rev. Lett.* **105** (2010) 181802 [[arXiv:1005.2622](#)] [[SPIRES](#)].
- [46] H. Zhang, E.L. Berger, Q.-H. Cao, C.-R. Chen and G. Shaughnessy, *Color sextet vector bosons and same-sign top quark pairs at the LHC*, [arXiv:1009.5379](#) [[SPIRES](#)].

- [47] A. Celikel, M. Kantar and S. Sultansoy, *A search for sextet quarks and leptogluons at the LHC*, *Phys. Lett. B* **443** (1998) 359 [SPIRES].
- [48] E. Eichten, I. Hinchliffe, K.D. Lane and C. Quigg, *Signatures for technicolor*, *Phys. Rev. D* **34** (1986) 1547 [SPIRES].
- [49] M.I. Gresham and M.B. Wise, *Color octet scalar production at the LHC*, *Phys. Rev. D* **76** (2007) 075003 [arXiv:0706.0909] [SPIRES].
- [50] M. Gerbush, T.J. Khoo, D.J. Phalen, A. Pierce and D. Tucker-Smith, *Color-octet scalars at the LHC*, *Phys. Rev. D* **77** (2008) 095003 [arXiv:0710.3133] [SPIRES].
- [51] T. Plehn and T.M.P. Tait, *Seeking sgluons*, *J. Phys. G* **36** (2009) 075001 [arXiv:0810.3919] [SPIRES].
- [52] S.Y. Choi et al., *Color-octet scalars of $N = 2$ supersymmetry at the LHC*, *Phys. Lett. B* **672** (2009) 246 [arXiv:0812.3586] [SPIRES].
- [53] A. Idilbi, C. Kim and T. Mehen, *Factorization and resummation for single color-octet scalar production at the LHC*, *Phys. Rev. D* **79** (2009) 114016 [arXiv:0903.3668] [SPIRES].
- [54] A.V. Manohar and M.B. Wise, *Flavor changing neutral currents, an extended scalar sector and the Higgs production rate at the LHC*, *Phys. Rev. D* **74** (2006) 035009 [hep-ph/0606172] [SPIRES].
- [55] P. Fileviez Perez, R. Gavin, T. McElmurry and F. Petriello, *Grand unification and light color-octet scalars at the LHC*, *Phys. Rev. D* **78** (2008) 115017 [arXiv:0809.2106] [SPIRES].
- [56] J. Pumplin et al., *New generation of parton distributions with uncertainties from global QCD analysis*, *JHEP* **07** (2002) 012 [hep-ph/0201195] [SPIRES].
- [57] T. Han, I. Lewis and T. McElmurry, *QCD corrections to scalar diquark production at hadron colliders*, *JHEP* **01** (2010) 123 [arXiv:0909.2666] [SPIRES].
- [58] D0 collaboration, V.M. Abazov et al., *Measurement of dijet angular distributions at $\sqrt{s}=1.96\text{TeV}$ and searches for quark compositeness and extra spatial dimensions*, *Phys. Rev. Lett.* **103** (2009) 191803 [arXiv:0906.4819] [SPIRES].
- [59] ATLAS collaboration, G. Aad et al., *Search for quark contact interactions in Dijet angular distributions in pp collisions at $\sqrt{s} = 7\text{TeV}$ measured with the ATLAS detector*, arXiv:1009.5069 [SPIRES].
- [60] CMS collaboration, V. Khachatryan et al., *Search for quark compositeness with the Dijet centrality ratio in pp collisions at $\sqrt{s}=7\text{TeV}$* , arXiv:1010.4439 [SPIRES].
- [61] E. Eichten, K.D. Lane and M.E. Peskin, *New tests for quark and lepton substructure*, *Phys. Rev. Lett.* **50** (1983) 811 [SPIRES].
- [62] T. Han, J.D. Lykken and R.-J. Zhang, *On Kaluza-Klein states from large extra dimensions*, *Phys. Rev. D* **59** (1999) 105006 [hep-ph/9811350] [SPIRES].