Determination of $B(D_s^+ \rightarrow \phi \pi^+)$ via Observation of $D_s^+ \rightarrow \phi l^+ \nu$

J. Alexander, (1) M. Artuso, (1) C. Bebek, (1) K. Berkelman, (1) T. Browder, (1) D. G. Cassel, (1) E. Cheu, (1)
Gittelman, (1) S. W. Gray, (1) A. M. Halling, (1) D. L. Hartill, (1) B. K. Heltstey, (1) J. Kandaswamy, (1) N.
Katayama, (1) D. L. Kreinin, (1) J. D. Lewis, (1) G. S. Ludwig, (1) N. B. Mistry, (1) J. Mueller, (1) S.
Nandi, (1) E. Nordberg, (1) C. O'Grady, (1) D. Peterson, (1) M. Pisarchy, (1) D. Riley, (1) M. Sapper, (1) M.
Selen, (1) A. Silverman, (1) S. Stone, (1) H. Worden, (1) M. Worr, (1) A. J. Sadoff, (2) P. Avery, (3) D.
Besson, (3) L. Garren, (3) J. Yelton, (3) T. Bowcock, (4) K. Kinoshita, (4) F. M. Pipkin, (4) M. Procario, (4)

(1) Cornell University, Ithaca, New York 14853
(2) Ithaca College, Ithaca, New York 14850
(3) University of Florida, Gainesville, Florida 32611
(4) Harvard University, Cambridge, Massachusetts 02138
(5) University of Kansas, Lawrence, Kansas 66045
(6) University of Minnesota, Minneapolis, Minnesota 55455
(7) Ohio State University, Columbus, Ohio 43210
(8) Purdue University, West Lafayette, Indiana 47907
(9) University of Rochester, Rochester, New York 14627
(10) State University of New York at Albany, Albany, New York 12222
(11) Syracuse University, Syracuse, New York 13244
(12) Vanderbilt University, Nashville, Tennessee 37235
(Received 28 June 1990)

Using the CLEO detector at the Cornell Electron Storage Ring (CESR), we have determined the ratio
$\Gamma(D_s^+ \rightarrow \phi l^+ \nu) / \Gamma(D_s^+ \rightarrow \phi \pi^+)$ = 0.49 ± 0.10 ± 0.08. We use this measurement to derive $B(D_s^+ \rightarrow \phi \pi^+)$. 
PACS numbers: 13.20.Fc, 13.25.+m, 14.40.Jz

Although the $D_s$ meson has been observed in several decay modes, there are no direct measurements of an absolute branching fraction to any channel. Theoretical models of semileptonic $D$ decay predict almost equal widths for $D_s^+ \rightarrow \phi l^+ \nu$ and $D^+ \rightarrow K^* l^+ \nu$, with small corrections ($\sim 20\%$) due to phase-space and form-factor differences. Since

$$\Gamma(D_s^+ \rightarrow K^* l^+ \nu) = \Gamma(D_s^+ \rightarrow \phi l^+ \nu) / \tau_{D_s^+}$$

has been measured,\(^2\)

$$B(D_s^+ \rightarrow \phi l^+ \nu) = \Gamma(D_s^+ \rightarrow \phi l^+ \nu) / \tau_{D_s^+}$$

can be calculated. By measuring the ratio of branching ratios $B(D_s^+ \rightarrow \phi \pi^+) / B(D_s^+ \rightarrow \phi l^+ \nu)$ one can measure the absolute branching ratio of $D_s^+ \rightarrow \phi \pi^+$. Previous estimates of this branching ratio are $2\%$ to $4\%$ derived from a guess of the relative production rates for the $D_s$ and the sum of the $D_s$, $D^0$, and $D^+$ in continuum $e^+e^-$ annihilations,\(^1\), and $(2 \pm 1)\%$ derived by assuming that the charm production cross section is $37\%$ of the total cross section in continuum $e^+e^-$ annihilations.\(^4\). There is also an upper limit of $4.1\%$ from Mark III,\(^5\), and a lower limit of $3.4\%$ from E691 which did not observe a signal for $D_s^+ \rightarrow \phi l^+ \nu$.\(^6\)

We use data taken with the CLEO detector at the Cornell Electron Storage Ring (CESR). The luminosities used consist of $212 \text{ pb}^{-1}$ accumulated at the $Y(4S)$ resonance, $102 \text{ pb}^{-1}$ taken at a center-of-mass energy $60 \text{ MeV}$ below the $Y(4S)$, and $116 \text{ pb}^{-1}$ taken at the $Y(5S)$ resonance. The sample consists of approximately $1100000$ continuum events, $240000$ $Y(4S)$ decays, and $35000 Y(5S)$ decays. The CLEO detector is described in detail elsewhere.\(^7\)

The event sample is defined by using standard CLEO hadronic-event-selection criteria.\(^8\) In order to suppress $Y(4S)$ and $Y(5S)$ resonance decays, we require that the ratio of Fox-Wolfram event-shape parameters,\(^9\) $H_3/H_0$,
be greater than 0.25. This cut has a 90% efficiency for the continuum charm events we are interested in, while rejecting 74% of the resonant background. Candidate muons must have momentum above 1.4 GeV/c and penetrate all the detector iron. Electrons above 1.4 GeV/c are identified either by $dE/dx$ in the drift chamber or a combination of this criterion with outer $dE/dx$ information and shower-counter information. For the momentum interval 1.0–1.4 GeV/c we require that shower-counter information be present. We have 4400 muons and 10400 electrons in our sample.

Positive identification of the $D_s^+ \to \phi l^+ \nu$ decay is difficult because of the missing $\nu$. To examine the signatures of such decays we simulate $\phi l^+ \nu$ decays using the model of Isgur et al.\textsuperscript{1} The parent $D_s$ momentum distribution is generated according to our measurements using the $\phi \pi^+$ mode. We require that the $\phi l^+$ momenta be greater than 2 GeV/c. In continuum $e^+e^-$ annihilations this cut maximizes the signal relative to the background. In approximately 90% of the retained Monte Carlo events the $\phi$ has a momentum greater than 1 GeV/c. In addition, we find that 99% of the decays have $\phi l^+$ mass below 1.9 GeV.

In the data we search for $\phi$'s only in the $K^+K^-$ decay mode. We then consider all $K^+K^-l^{\pm}$ combinations which have invariant mass below 1.9 GeV and momentum above 2.0 GeV/c. In addition, we require that the $K^+K^-$ momentum be above 1.0 GeV/c. The resulting $K^+K^-$ invariant-mass distribution is shown in Fig. 1, separately for electrons and muons. We fit these distributions with a Gaussian centered at the $\phi$ mass and fixed width determined by investigating all $\phi$'s in our data sample having momenta between 1 and 2 GeV/c. We have $48.5 \pm 9.0$ and $26.3 \pm 6.4$ $\phi$'s in the electron and muon samples, respectively. The numbers of events and detection efficiencies are shown in Table 1.\textsuperscript{10} Because we will be interested in comparing with the $\phi \pi^+$ rate above 2.5 GeV/c, the detection efficiencies shown in Table 1 correspond to the number of detected events normalized to the number of the $D_s$ produced in the momentum range above 2.5 GeV/c.

Background sources include fake leptons and random combinations of real $\phi$'s and real leptons which happen to fall in the signal region. The latter contain contributions from continuum charm events, the only known source of real leptons in the continuum, and $Y(4S)$ and $Y(5S)$ resonant decays which have been suppressed by the shape cut mentioned above.

In order to determine the number of fake leptons we count the number of charged tracks in events with real $\phi$'s, as a function of momentum, that satisfy the kinetic cuts discussed above. (To get the number associated with only the $\phi$ signal we do a sideband subtraction in the $K^+K^-$ mass plot.) We then assume that the mixture of the particle species of this track sample is the same as the nominal continuum. We determine a fake rate per track from the fake rates measured separately for $\pi^{\pm}$, $K^{\pm}$, $\rho$, and $\bar{p}$ multiplied by the assumed particle fractions.\textsuperscript{11} We find a total of $8.6 \pm 2.0$ electron fakes and $8.0 \pm 1.5$ muon fakes, where the errors reflect the uncertainty in the fake rates and particle fractions. We have also investigated the contribution of converted $\gamma$'s in our electron sample. It is found to be negligible.

In continuum events real leptons can only come from charm decays. To determine the level of uncorrelated $\phi-l^{\pm}$ combinations from this source, we use a sample of fully reconstructed charmed mesons to find the yield of the $\phi$ associated with a charmed particle. We sum $D_s^{0}$'s in the decay modes $K^+\pi^+$ and $K_S\pi^+\pi^-$, and $D^0$'s from $D^{*+} \to \pi^+D^0$ with $D^0$ decaying into $K^+\pi^+\pi^-$. We have 12,200 events above 2.5 GeV/c in the $D^0$ mass peak. The $\phi$'s we are interested in have momenta above 1 GeV/c. The $\phi$'s within 90° of the $D^0$ direction (same hemisphere) are quite likely to end up in the signal region ($M_{\phi l} < 1.9$ GeV) while the $\phi$'s in the opposite hemisphere make large invariant masses and do not affect the

![Fig. 1. Invariant $K^+K^-$ mass (a) for electron events and (b) for muon events selected by the kinematic cuts described in the text. The curves show the fits to the background and signal.](image)

<table>
<thead>
<tr>
<th>TABLE 1. Summary of event numbers.</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
</tr>
<tr>
<td>Number of events</td>
</tr>
<tr>
<td>Lepton fakes</td>
</tr>
<tr>
<td>$B\bar{B}$ background</td>
</tr>
<tr>
<td>Fake subtracted</td>
</tr>
<tr>
<td>Efficiency</td>
</tr>
<tr>
<td>Corrected yield</td>
</tr>
</tbody>
</table>
result. We find $0.6 \pm 8.8 \phi$'s in the same hemisphere.\textsuperscript{12}

After normalizing to the total of 14800 lepton events in our sample we assign an asymmetric systematic error of $^{+0.1}_{-0.1}$ events.\textsuperscript{13}

To calculate the level of uncorrelated real $\phi$-$J_{\psi}$ combinations from resonant $Y(4S)$ and $Y(5S)$ decays, we take the measured momentum spectrum of $\phi$'s and leptons from $B$ decays and use a Monte Carlo simulation to determine how many $\phi$-$J_{\psi}$ pairs populate our signal region. The resulting numbers are also shown in Table I.

We have considered the possibility that our $\phi l^\pm$ sample is contaminated with events containing extra particles. Two candidate reactions are $D \to \phi Kl\nu$ or $D_\ell \to \phi l\ell\nu$. The first case, even if such a final state existed, is excluded by our lepton and $\phi$ momentum cuts. If the second reaction existed, our kinematic cuts would not necessarily exclude it. However, we note that $\phi \pi^0$ production, from $s\bar{s}$ quark pair hadronization by simple $u\bar{u}$ or $d\bar{d}$ popping is Okubo-Zweig-Ili'uka suppressed.\textsuperscript{14,15}

Furthermore, we note that our measurement of $K^{+}\pi^{-}\nu$ (see below) compares well with the previous measurement and thus gives evidence that our detection technique does not introduce large backgrounds.

Another way of displaying the signal and background components is to select a $\phi$ sample on the basis of $K^+K^-$ mass and then plot the $\phi l^\pm$ mass for $\phi$ momentum greater than 1 GeV/c and $\phi l^\pm$ momentum greater than 2 GeV/c. In Fig. 2 we display the $\phi l^\pm$ mass spectrum after $\phi$ sideband subtraction. Also shown is the sum of background shapes from lepton fakes, uncorrelated $\phi$-lepton production, and $B$ decays. We see that the signal shape agrees reasonably with the Monte Carlo spectra for semileptonic decay.

We have previously reported signals for the channel $D_\ell \to \phi \pi^\pm$ and $D \to \phi \pi^0$. In this analysis we use a procedure similar as possible to the one used in finding the $\phi l\nu$ rate. We first find $K^+K^-\pi^\pm$ candidates consistent with the $D_\ell$ mass and having momentum greater than 2.5 GeV/c. Then we fit the $K^+K^-$ mass spectrum with a Gaussian. We find 400 $\pm 27 D_\ell$ events.

After averaging the $\phi\mu\nu$ and $\phi\ell\nu$ samples we find

\[
\frac{B(D_\ell \to \phi l^+\nu)}{B(D_\ell \to \phi \pi^+)} = 0.49 \pm 0.10_{-0.06}^{+0.12},
\]

where the first error is statistical and the second is systematic and includes the uncertainties in the background subtraction and efficiencies. This number is marginally consistent with an upper limit at 90% confidence level of 0.45 as reported by E691.\textsuperscript{6}

We derive a $\phi l^+\nu$ branching ratio from the following relation:

\[
B(D_\ell \to \phi l^+\nu) = \frac{\Gamma(D_\ell \to \phi l^+\nu)}{\Gamma_{\text{tot}}} = \frac{\Gamma(D_\ell \to \phi l^+\nu)}{\tau_D l^+\nu} = (0.80 \pm 0.08)\frac{B(D \to K^*l^+\nu)}{\tau_D l^+\nu}.
\]

The factor 0.8 is the average of two theoretical results,\textsuperscript{1} and the error reflects a large range of possible differences in form factors. The measured branching ratio\textsuperscript{2} for $D^+ \to K^{*0}e^+\nu$ is $(4.5 \pm 0.7 \pm 0.5)\%$ and the ratio of $D^+/D^+$ lifetimes\textsuperscript{16} is $0.42 \pm 0.03$. The resulting estimate is $B(D_\ell \to \phi l^+\nu)/(1.50 \pm 0.31)\%$, where the error contains uncertainties on the $D^+$ branching ratio, the lifetime ratio, and theory. Then $B(D_\ell \to \phi \pi^+)/(3.1 \pm 0.6 \pm 0.7)\%$, where the first error is statistical, the second systematic, and the third is also systematic and arises from the uncertainty on the predicted value of $B(D_\ell \to \phi l\nu)$.

As a check on this analysis we have repeated the procedure on the reaction $D^0 \to K^*-\nu$. Here the signal region is defined by having the $K_S\pi^\pm l^+$ invariant mass between 0.9 and 1.8 GeV, the $K_S\pi^\pm l^+$ momentum above 2 GeV/c, and the $K_S\pi^\pm$ momentum above 1 GeV/c. The $K_S\pi^\pm$ invariant-mass spectrum is shown in Fig. 3 for the sum of electron and muon events. Fits to a polynomial background and Breit-Wigner shapes fixed at the known $K^\pm$ mass and width give 82 $\pm 24$ electrons and 55 $\pm 14$ muon events. To find the branching ratio we normalize to the decay $D^0 \to K_S\pi^+\pi^-$. Following the same procedure as above we have

\[
\frac{B(D^0 \to K^*-l^+)\nu}{B(D^0 \to \bar{K}^0\pi^+\pi^-)} = 0.24 \pm 0.07 \pm 0.06,
\]

where the first error is statistical and the second is systematic. This translates into a branching ratio for
\( D^0 \rightarrow K^+ l^- \nu \) of \((1.5 \pm 0.4 \pm 0.4)\% \).\(^{17}\) By scaling the E691 measurement\(^2\) of \( B(D^+ \rightarrow K^{*0} l^+ \nu) \) by the ratio of \( D^+ \) to \( D^0 \) lifetimes,\(^\text{16} \) we extract a branching ratio of \((1.8 \pm 0.3)\% \). Thus our measurement is consistent with the E691 data.

In conclusion, we have presented the first positive evidence of a signal for \( D_s \rightarrow \phi l \nu \). Using the expected near equality of semileptonic widths for pseudoscalar to vector transitions of charm mesons we infer \( B(D_s^+ \rightarrow \phi \pi^+) = (3.1 \pm 0.6^{+0.9}_{-0.8} \pm 0.6)\% \). This fits into the range of previous indirect estimates.

We gratefully acknowledge the CESR machine group. This work was supported by the National Science Foundation and the U.S. Department of Energy under Contracts No. DE-AC02-76ER01428, 3064 1545), No. DE-AC02-78ER05001, 83ER05001, 83ER40105), and No. DE-FG05-86ER40272. For support, R.P. thanks the A. P. Sloan Foundation and P.S.D. thanks the Presidential Young Investigators program of the NSF. The supercomputing resources of the Cornell Theory Center were used in this research.

\(^{1}\)N. Isgur \textit{et al.}, Phys. Rev. D 39, 799 (1989) (private communication). These authors predict 0.78 for the ratio \( \Gamma(D^+ \rightarrow \phi l^+ \nu)/\Gamma(D \rightarrow K^* l^+ \nu) \), while M. Wirbel (private communication) predicts 0.83; see M. Wirbel \textit{et al.}, Z. Phys. C 29, 269 (1985).


\(^{10}\)We use the ratio of \( \Gamma_l/\Gamma_T \) measured in Ref. 2. Our efficiency varies only 3% between longitudinal and transversely polarized \( \phi \)’s.


\(^{12}\)We find \( 45 \pm 22 \phi \)’s in the hemisphere opposite to the \( D^0 \) direction.

\(^{13}\)The background from semileptonic \( D \) decays with momenta below 2.5 GeV/c combined with real \( \phi \)’s is much reduced in our signal region because these \( D \)’s produce leptons with sufficiently small momentum that they generally do not satisfy our lepton momentum cut or our \( \phi \) momentum cut.

\(^{14}\)Also, although it is possible that the \( D \) decays to an excited \( s \bar{s} \) state, no such state has been found which decays into \( \phi \)’s.

\(^{15}\)Another possible background could come from \( D^* \rightarrow \phi l^+ \nu \). However, this reaction is Cabbibo suppressed at the quark level and the \( d \bar{d} \) system must form a \( \phi \), which is unlikely.


\(^{17}\)Our measurement allows extra \( \pi^0 \)’s in the final state. E691 can limit this from the small size of the non-\( K^* \) signal in their \( K\pi \) mass distribution. We use this comparison to justify that there are no other additional sources of background.