Dalitz Analysis of $D^0 \to K_{S}^{0}\pi^+\pi^-$


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In $e^+e^-$ collisions using the CLEO detector, we have studied the decay of the $D^0$ to the final state $K_{S}^{0}\pi^+\pi^-$ with the initial flavor of the $D^0$ tagged by the decay $D^{*+} \to D^0\pi^+$. We use the Dalitz technique to measure the resonant substructure in this final state and clearly observe ten different contributions by fitting for their amplitudes and relative phases. We observe a $K^+(892)^+\pi^-$ component which arises from doubly Cabibbo suppressed decays or $D^{*0}-D^0$ mixing.

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Weak hadronic decays of charmed mesons are expected to proceed dominantly by resonant two-body decays in several theoretical models [1–5]. A clearer understanding of final state interactions in exclusive weak decays is an important ingredient for our ability to model decay rates as well as for our understanding of interesting phenomena such as mixing [6]. In this context, an interesting final state is \( D^0 \to K^0 \pi^+ \pi^- \) which can proceed through a number of two-body states. Previous investigations [7–11] of the substructure in this channel were limited by statistics to the Cabibbo favored decays. A key motivation is to observe one or more of the double Cabibbo suppression, such as \( K^*(892)^+ \pi^- \) or \( K_0(1430)^+ \pi^- \), and to measure their phase relative to the corresponding unsuppressed \( K^0 \pi^+ \pi^- \) submodes.

This analysis uses an integrated luminosity of 9.0 fb\(^{-1}\) of \( e^+ e^- \) collisions at \( \sqrt{s} = 10 \) GeV provided by the Cornell Electron Storage Ring (CESR). The data were taken with the CLEO II IV configuration of the CLEO II multipurpose detector [12]. A silicon vertex detector (SVX) was installed in the upgraded configuration [13].

The event selection is similar to that used in our search for \( D^0 D^\ast \) mixing via the process \( D^0 \to D^\ast \to K^0 \pi^+ \pi^- \) [14]. We reconstruct candidates for the decay sequence \( D^\ast^+ \to \pi^+ D^0, D^0 \to K^0 \pi^+ \pi^- \). Consideration of charge conjugated modes is implied throughout this Letter. The charge of the slow pion (\( \pi^+_S \) or \( \pi^-_S \)) identifies the charm state at \( t = 0 \) as either \( D^0 \) or \( D^0 \). We require the \( D^+ \) momentum \( p_{D^\ast} \) to exceed 2.0 GeV/c. We reconstruct \( K^0_S \to \pi^+ \pi^- \) with the requirement that the daughter pion tracks form a common vertex, in three dimensions, with a confidence level > 10\(^{-6}\). Signal candidates pass the vertex requirement with 96% relative efficiency. Throughout this Letter, relative efficiency is defined as the number of events passing all requirements relative to the number of events when only the requirement under study is relaxed.

Our silicon vertex detector provides precise measurement of the charged tracks in three dimensions [15]. We exploit the precision tracking of the SVX by refitting the \( K^0_S \) and \( \pi^\pm \) tracks with a requirement that they form a common vertex in three dimensions. We use the trajectory of the \( K^0_S \pi^+ \pi^- \) system and the position of the CESR luminous region to obtain the \( D^0 \) production point. We refit the \( \pi^+ \) track with a requirement that the trajectory intersect the \( D^0 \) production point. We require that the confidence level of each refit exceed 10\(^{-4}\). The signal candidates pass the \( D^0 \) mass and decay vertex requirement with 85% and 91% relative efficiency, respectively.

We reconstruct the energy released in the \( D^+ \to \pi^+ D^0 \) decay as \( Q = M^2 - M^2 - m_{\pi^\pm} \), where \( M \) is the reconstructed mass of the \( \pi^+ K^0_S \pi^- \) system, \( M^2 \) is the reconstructed mass of the \( K^0_L \pi^+ \pi^- \) system, and \( m_{\pi^\pm} \) is the charged pion mass. The addition of the \( D^0 \) production point to the \( \pi^+ \) trajectory yields the resolution \( \sigma_Q = 220 \pm 4 \) keV, where \( \sigma_Q \) is the core value from a fit to a bifurcated student’s \( t \) distribution. We obtain a resolution on \( M \) of \( \sigma_M = 4.8 \pm 0.1 \) MeV and a resolution on \( m_{K_S^0} \) of \( \sigma_{m_{K_S^0}} = 2.4 \pm 0.1 \) MeV.

We apply a set of “prophylactic” requirements to exclude candidates with a poorly determined \( Q, M, \) or \( D^0 \) flight time, and \( K_S^0 \) candidates that are likely to be background. We reconstruct the flight time using only the vertical (\( y \)) component of the flight distance of the \( D^0 \) candidate. This is effective because the vertical extent of the \( e^+ e^- \) luminous region has \( \sigma_y = 7 \mu\text{m} \) [16]. The typical computed \( \sigma \) for \( Q, M, \) and flight time is 150 keV, 5 MeV, and 0.5\( \tau_{D^0} \), respectively. These are computed from the reconstruction covariance matrix of the daughters of the \( D^0 \) candidate. We reject candidates where \( \sigma_Q, \sigma_M, \) or flight time error exceeds 300 keV, 10 MeV, or 2.0\( \tau_{D^0} \), respectively. The relative efficiencies for the signal candidates to pass these cuts are 98%, 98%, and 89%, respectively. We exclude \( K_S^0 \) candidates with a vertical flight distance less than 500 \( \mu\text{m} \) to remove combinatoric background with zero lifetime. The signal candidates survive this requirement with 95% relative efficiency. The distributions of \( Q \) and \( M \) for our data are shown in Fig. 1.

We select 5299 candidates within 3 standard deviations of the expected \( Q, M, \) and \( m_{K_S^0} \). The efficiency for the selection described above is nearly uniform across the Dalitz distribution. In our simulation, we use the \( D^0 \to K_{S}^{0} \pi^+ \pi^- \) uniformly populating the allowed phase space. We study our efficiency with a GEANT [17] based simulation of \( e^+ e^- \to c\bar{c} \) events in our detector with a luminosity corresponding to more than 3 times our data sample. We observe that the selection introduces distortions due to inefficiencies near the edge of phase space, and fit the efficiency to a two-dimensional cubic polynomial in \( (m_{K_S^{0}} - m_{\pi^+ \pi^-}), (m_{\pi^+ \pi^-}) \). Our standard result uses this efficiency parametrization to interpret the Dalitz distribution. To take into account a systematic uncertainty in our selection efficiency, we compare the standard result

![FIG. 1 (color online). Distribution of (a) \( M \) and (b) \( Q \) for the process \( D^0 \to K_{S}^{0} \pi^+ \pi^- \). The candidates pass all selection criteria discussed in the text.](251802-2)
with an efficiency that is uniform across the allowed Dalitz distribution.

Figure 1 shows that the background is small, but non-negligible. Fitting the $M$ distribution to the signal shape as described above plus a quadratic background shape, we find a background fraction of $2.1\% \pm 1.5\%$. We use this fraction as a constraint when fitting the Dalitz distribution. To model the background contribution in the Dalitz distribution, we consider those events in the data that are in sidebands five to ten standard deviations from the signal in $Q$ and $M$ and within three in $m_{K^0}$. There are 445 candidates in this selection, about 4 times the amount of background we estimate from the signal region. We compare these with background from our simulation also including $e^+e^-$ annihilations producing the lighter quarks. We note that the background from the simulation is dominated by random combinations of unrelated tracks, and the shape of the background in the simulation and the sideband data sample agree well. The simulation predicts that the background uniformly populates the allowed phase space, and we model this contribution to the Dalitz distribution by fitting the data sideband sample to a two-dimensional cubic polynomial in $(m_{K^0\pi^+}^2, m_{\pi^-}^2)$. All parameters except the constant are consistent with zero. Other possible contributions to the background, resonances combined with random tracks, and real $D^0$ decays combined with random soft pions of the wrong charge, are negligible in the simulation. The latter, called mistags, are especially dangerous to our search for “wrong sign” $D^0$ decays. Mistags populate the Dalitz distribution in a known way that depends on the shape of the signal. When we analyze the Dalitz distribution, we allow a mistag fraction with an unconstrained contribution. We have looked for the contribution of a resonance, such as $r^0$ or $K^*(892)^-$, plus random tracks to the background in the data by studying the sidebands in $Q, M$, and $m_{K^0}$, and conclude that any such contributions are negligible.

Figure 2 shows the Dalitz distribution for the $D^0 \rightarrow K_S^0 \pi^+ \pi^-$ candidates. A rich structure is evident. Contributions from $K^*(892)^-\pi^+$ and $K_S^0\rho^0$ are apparent. Depopulated regions exist suggesting destructive interference between some resonances and the dominant decay modes.

We parametrize the $K_S^0 \pi^+ \pi^-$ Dalitz distribution following the methodology described in Ref. [18] using the same sign convention used in previous investigations of this decay channel [8,11]. We consider 19 resonant subcomponents, $K^*(892)^-\pi^+$, $\kappa(800)^-\pi^+$, $K^*(1410)^-\pi^+$, $K_S^0(1430)^-\pi^+$, $K^*(1680)^-\pi^+$, $K_S^0(1780)^-\pi^+$, $K_S^0\rho$, $K_S^0\omega$, $K_S^0\rho(1450)$, $K_S^0\rho(1700)$, $K_S^0\sigma(500)$, $K_S^0f_0(980)$, $K_S^0f_2(1270)$, $K_S^0f_0(1370)$, $K_S^0f_0(1500)$, $K_S^0f_0(1710)$, and the wrong sign $K^*(892)^-\pi^-$ and $K_S^0(1430)^+\pi^-$, as well as a non-resonant contribution. The parameters of the established resonances are taken from Ref. [19] except for the $f_0$. We use Ref. [20] for the $f_0(980)$ and the coupled channel analysis of Ref. [21] for the $f_0(1370), f_0(1500)$, and $f_0(1710)$. We consider that each of the resonances has its own amplitude and relative phase. The nonresonant contribution is modeled as a uniform distribution across the allowed phase space with a fixed relative phase. The phases and widths of the resonance contributions vary as given by the spin of the resonance as described in Ref. [18]. When we consider the unconfirmed scalar $\sigma(500)$ [22] and $\kappa(800)^-$ [23] resonances, we allow the masses and widths of these resonances to float.

This study is sensitive only to relative phases and amplitudes. Thus, we fix one phase and one amplitude. To minimize correlated errors on the phases and amplitudes, we choose the largest color suppressed mode, $K_S^0\rho$, to have a fixed zero phase and an amplitude of one. Since the choice of normalization, phase convention, and amplitude formalism may not always be identical for different experiments, fit fractions are reported in addition to amplitudes to allow for more meaningful comparisons between results. The fit fraction is defined as the integral of a single component divided by the coherent sum of all components. The sum of the fit fractions for all

\[ S = \frac{1}{n} \sum_{i=1}^{n} f_i \]

where $f_i$ is the fit fraction for component $i$.
components will, in general, not be unity because of the effect of interference.

Backgrounds, combinatorics, and mistags are considered as described above. They do not interfere with the signal, but the mistag background shape depends on the signal shape as noted earlier.

One must also consider the statistical errors on the fit fractions. We have chosen to use the full covariance matrix from the fits to determine the errors on fit fractions so that the assigned errors will properly include the correlated components of the errors on the amplitudes and phases. After each fit, the covariance matrix and final parameter values are used to generate 500 sample parameter sets. For each set, the fit fractions are calculated and recorded in histograms. Each histogram is fit with a single Gaussian to extract its width, which is used as a measure of the statistical error on the fit fraction.

We perform an initial fit, using the unbinned maximum likelihood technique including only the resonances, $K^{(892)^-} \pi^+$, $K_2^0(1430)^- \pi^+$, $K_2^0(980)^0$, $K_2^0f_0(1270)$, and $K_2^0f_0(1370)$, observed by E687 [11]. This fit is consistent with the results from E687 but our data is not well described by these six resonances. We then consider each of the intermediates states listed above retaining those that are more than three standard deviations significant. We do not fit the $\kappa(800)^- \pi^+$, $K^*(1410)^- \pi^+$, $K_2^0(1780)^0 \pi^+$, $K_2^0(1540)^0 \pi^+$, $K_2^0(1700)^0 \pi^+$, $K_2^0f_0(1500)^0$, $K_2^0f_0(1710)^0$, and the wrong sign $K_2^0(1430)^- \pi^+$ to be significant. The $K_2^0\sigma(500)$ is a special case. It is excluded in our standard fit, and its possible contribution is discussed further below. The remaining ten resonances, a nonresonant contribution, and backgrounds as described above are included in our standard fit and give our central results.

Table I gives the results of our standard fit. Figure 2 shows the three projections of the fit. We note that there is a significant wrong sign $D^0 \rightarrow K^*(892)^+ \pi^-$. Mistags are not significant, having a rate of $0.1 \pm 0.4\%$. When we compare the likelihood of our standard fit to one where the $K^*(892)^+ \pi^-$ amplitude fixed to zero, we see that the statistical significance of the $K^*(892)^+ \pi^-$ amplitude is 5.5 standard deviations. Also, we note that the phase difference between the $K^*(892)^+ \pi^-$ and $K^*(892)^+ \pi^-$ contributions is consistent with $180^\circ$, as expected from Cabibbo factors.

We consider systematic uncertainties that arise from our model of the background, the efficiency, and biases due to experimental resolution. Our general procedure is to change some aspect of our standard fit and interpret the change in the values of the amplitudes and phases as an estimate of the systematic uncertainty. The background is modeled with a two-dimensional cubic polynomial and the covariance matrix of the polynomial coefficients determined from a sideband. Our standard fit fixes the coefficients of the background polynomial, and to estimate the systematic uncertainty on this background shape we perform a fit with the coefficients allowed to float constrained by the covariance matrix. Similarly, we perform a fit with a uniform efficiency rather than the efficiency shape determined from the simulation as an estimate of the systematic uncertainty due to the efficiency. We change selection criteria in the analysis to test whether our simulation properly models the efficiency. These variations to the standard fit are the largest contribution to our experimental systematic errors. To study the effect of the finite resolution our experiment has on the variables in the Dalitz plots, we vary the size of the bins used to compute the overall normalization.

### Table I

<table>
<thead>
<tr>
<th>Component</th>
<th>Amplitude</th>
<th>Phase</th>
<th>Fit fraction (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>$K^<em>(892)^+ \pi^- \times [K^</em>(892)^+ \rightarrow K^0\pi^+]$</td>
<td>$(11 \pm 2^{+1+0}_{-1+0}) \times 10^{-2}$</td>
<td>$321 \pm 10 \pm 3^{+5}_{-5}$</td>
<td>0.34 $\pm 0.13 \pm 0.26 \pm 0.03 \pm 0.02$</td>
</tr>
<tr>
<td>$K^0\rho^0$</td>
<td>1.0 (fixed)</td>
<td>0 (fixed)</td>
<td>26.4 $\pm 0.9^{+0.9+0.4}_{-0.7-2.5}$</td>
</tr>
<tr>
<td>$K^0\omega \times [B(\omega \rightarrow \pi^+\pi^-)]$</td>
<td>$(37 \pm 5 \pm 1^{+0+0}_{-0-0}) \times 10^{-3}$</td>
<td>$114 \pm 7^{+6+4}_{-5-4}$</td>
<td>0.72 $\pm 0.18^{+0.04+0.10}_{-0.06-0.07}$</td>
</tr>
<tr>
<td>$K^<em>(892)^- \pi^+ \times [K^</em>(892)^- \rightarrow K^0\pi^-]$</td>
<td>$1.56 \pm 0.03 \pm 0.02^{+0.05}_{-0.03}$</td>
<td>$150 \pm 2 \pm 3^{+2+2}_{-3-3}$</td>
<td>65.7 $\pm 1.3^{+1.1+1.4}_{-2.6-3.0}$</td>
</tr>
<tr>
<td>$K_2^0f_0(980)$</td>
<td>$0.34 \pm 0.02^{+0.04+0.04}_{-0.03-0.02}$</td>
<td>$188 \pm 4^{+5+8}_{-3-6}$</td>
<td>4.3 $\pm 0.5^{+1.1+0.4}_{-0.5-0.5}$</td>
</tr>
<tr>
<td>$K_2^0f_0(1270)$</td>
<td>$0.7 \pm 0.2^{+0.3+0.1}_{-0.1-0.4}$</td>
<td>$308 \pm 12^{+18+16}_{-23-5}$</td>
<td>0.27 $\pm 0.15^{+0.24+0.28}_{-0.09-0.14}$</td>
</tr>
<tr>
<td>$K_2^0f_0(1370)$</td>
<td>$1.8 \pm 0.1^{+0.2+0.2}_{-0.1-0.6}$</td>
<td>$85 \pm 4^{+3+3}_{-1-1}$</td>
<td>9.9 $\pm 1.1^{+2.4+1.4}_{-1.1-1.3}$</td>
</tr>
<tr>
<td>$K_2^0(1430)^- \pi^+ \times [K_2^0(1430)^- \rightarrow K^0\pi^-]$</td>
<td>$2.0 \pm 0.1^{+0.1+0.5}_{-0.2-0.1}$</td>
<td>$3 \pm 4 \pm 4^{+4-5}$</td>
<td>7.3 $\pm 0.7^{+0.4+0.31}_{-0.9-0.7}$</td>
</tr>
<tr>
<td>$K_2^0(1430)^+ \pi^- \times [K_2^0(1430)^+ \rightarrow K^0\pi^-]$</td>
<td>$1.0 \pm 0.1 \pm 0.1^{+0.3}_{-0.1}$</td>
<td>$155 \pm 7^{+1+7}_{-4-24}$</td>
<td>1.1 $\pm 0.2^{+0.3+0.6}_{-0.1-0.3}$</td>
</tr>
<tr>
<td>$K^<em>(1680)^- \pi^+ \times [K^</em>(1680)^- \rightarrow K^0\pi^-]$</td>
<td>$5.6 \pm 0.6^{+0.7+0.2}_{-0.4-4.0}$</td>
<td>$174 \pm 6^{+10+13}_{-3-19}$</td>
<td>2.2 $\pm 0.4^{+0.5+1.7}_{-0.3-1.5}$</td>
</tr>
</tbody>
</table>

The components $K^0\pi^+\pi^-$ nonresonant.

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Another class of systematic uncertainties arise from our choices for the decay model for $D^0 \to K_0^* \pi^+ \pi^-$. We consider the Zemach formalism [24], rather than the standard helicity model, which enforces the transversality of intermediate resonances, and we vary the radius parameter [25] for the intermediate resonances and for the $D^0$ between zero and twice their standard value of 0.3 and 1 fm, respectively. These variations to the standard fit are the largest contribution to our modeling systematic errors. Additionally, we allow the masses and widths for the intermediate resonances to vary within their known errors [19–21].

We also consider uncertainty arising from which resonances we choose to include in our fit to the Dalitz plot. We compared the result of our standard fit to a series of fits where each of the possible resonances were included one at a time. We also considered a fit including all possible resonances. We take the maximum variation of the amplitudes and phases from the standard result compared to the results in this series of fits as a measure of the uncertainty due to our choice of included resonances.

The $\sigma(500)$ has been reported by E791 in $D^+ \to \pi^- \pi^+ \pi^+$ decays [22]. The parameters of the $\sigma(500)$ are sensitive to the choice of decay model, discussed previously. Replacing the nonresonant contribution in our standard fit with a $K_0^*\sigma(500)$ component yields an amplitude of $0.57 \pm 0.13$ and phase of $214 \pm 11$ with a mass of $m_{\sigma} = 513 \pm 32(\text{stat.})$ MeV and width $\Gamma_{\sigma} = 335 \pm 67(\text{stat.})$ MeV for the $\sigma(500)$ consistent with E791 results [22] ($m_{\sigma} = 478^{+24}_{-23} \pm 17$ MeV and $\Gamma_{\sigma} = 324^{+12}_{-10} \pm 21$ MeV). While we find this suggestive that there is a $K_0^*\sigma(500)$ contribution, we are unable to definitively confirm this because of the known shortcomings of our description of the scalar resonances. The systematic uncertainty does include the difference between the standard fit which does not include the $\sigma(500)$, and the fits allowing it. On the other hand, we find no evidence for a scalar $K^- \to K_0^* \pi^-$, the isospin partner to the $K^0$, suggested by E791 [23] in charm decays.

We also do separate standard fits for $D^0$ and $\bar{D}^0$ tags to search for $CP$ violating effects. We see no statistically significant difference between these two fits. A more general study would consider a $CP$ violating amplitude for each component observed in our standard fit.

In conclusion, we have analyzed the resonant substructure of the decay $D^0 \to K_0^* \pi^+ \pi^-$ using the Dalitz technique. We observe ten contributions including a wrong sign $D^0 \to K^*(892)^+ \pi^-$ amplitude with a significance of 5.5 standard deviations. This decay arises from a double Cabibbo suppressed decay or $D^0 - \bar{D}^0$ mixing. We measure $[B(D^0 \to K^*(892)^+ \pi^-)]/[B(D^0 \to K^*(892)^- \pi^+)] = (0.5 \pm 0.02^{+0.05}_{-0.03})\%$, and the relative phase between the two decays to be $(189 \pm 10 \pm 3^{+15}_{-12})^\circ$, consistent with 180°. We consider $D^0$ and $\bar{D}^0$ tags separately, and see no $CP$ violating effects.

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