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Categorization of sounds

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Abstract

Four experiments were conducted to test between Decision-Bound, Prototype, and Distribution theories for the categorization of sounds. Sounds varying in either resonance frequency or duration were used as stimuli. Different experimental conditions were created by varying the variance and overlap of two stimulus distributions used in a training phase and varying the size of the stimulus continuum used in the subsequent test phase. When resonance frequency was the stimulus dimension, the pattern of categorization-function slopes was in accordance with the Decision-Bound theory. When duration was the stimulus dimension, however, the slope pattern gave partial support for the Decision-Bound and Distribution theories. A new categorization model combining aspects of Decision-Bound and Distribution theories is introduced which gives a superior account of the slope patterns across the two stimulus dimensions.

The categorization of sounds plays an important role in everyday life. On a daily basis we categorize sounds in our environment as belonging to such basic events as a telephone ringing, a baby crying or the doors of a train slamming shut. The correct categorization of sounds may even be of vital importance, such as the hooting of an approaching car. Finally, the recognition of the sounds and words of spoken language is a form of auditory categorization which occupies a significant portion of most people's waking hours.

Despite its importance, auditory categorization has received relatively little attention in the psychological literature. An overwhelming majority of studies on perceptual categorization has been devoted to the categorization of simple visual stimuli, such as line segments of variable lengths and orientations. Three distinct theories of visual categorization have featured most prominently in the recent literature. Prototype theory (Rosch, 1973; Smith & Minda, 2000) assumes that stimuli are categorized based on their similarity to category prototypes stored in memory. A category prototype is generally defined as the average, or most typical, member of a category. Exemplar theory (Nosofsky, 1986), on the other hand, denies the explicit use of category prototypes. In its extreme formulation, Exemplar theory assumes that categorization is based on a comparison of the stimulus to all previously categorized exemplars of all categories. Finally, Decision-Bound theory (Ashby & Perrin, 1988) assumes that categorization is based on the comparison of the perceptual effect of a stimulus to category boundaries stored in memory.

Explicit connections between the fields of speech perception and visual categorization have been sparse. Nevertheless, the hypotheses for the categorization of phonemes that have been proposed over the years are similar to those for visual categorization, albeit more qualitative and mathematically less well developed.

One of the most popular research methodologies in speech perception is the phoneme categorization experiment. In phoneme categorization experiments listeners are presented with

naturally produced or synthetic speech sounds and are asked to assign the sounds to phonetic categories. In the most widely employed version of the phoneme categorization experiment, synthetic stimuli are used in which one or more acoustical parameters of interest, such as formant frequencies or silence durations, are systematically varied in a number of discrete steps of equal size to form a stimulus continuum.

Researchers from Haskins laboratories pioneered the use of stimulus continua for investigating speech perception, showing among other things that the perceived phoneme is generally influenced by many acoustic parameters distributed over a wide temporal window. Since these landmark studies, stimulus continua have been employed to investigate many basic aspects of speech perception, such as the unit of recognition (Nearey, 1997), dependencies in the categorization of successive phonemes (Massaro & Cohen, 1983; Smits, 2001), the influence of speaking rate on phonetic categorization (Volaitis & Miller, 1992), and the relative weights of various acoustic cues to particular phonetic distinctions (Ainsworth, 1968).

Despite the popularity of the phoneme categorization paradigm, we still do not fully understand how phonetic categories are represented and what listeners actually do in phoneme categorization experiments. How do we categorize speech sounds? The present study takes a first step in answering this question, focusing on the categorization of synthetic non-speech sounds.

In the past, several hypotheses concerning the representation and categorization of speech sounds have been proposed. Fueled by the "categorical perception" controversy, early speech perception experiments were mainly analyzed and discussed in terms of the boundaries between phonetic categories (e.g., Liberman, Harris, Hoffman & Griffith, 1957). The suggestion was made that what listeners do in phonetic categorization experiments is evaluate on which side of the relevant phonetic boundary the perceptual effect of the incoming stimulus is located. This hypothesis can be viewed as a phonetic implementation of Decision-Bound

theory mentioned earlier.

It has also been hypothesized that phoneme categories may be represented by prototypes (e.g., Oden & Massaro, 1978; Kuhl, 1991). In the context of speech perception, Prototype theory assumes that listeners in phonetic categorization experiments compute the similarity of an incoming stimulus to each of the relevant category prototypes and categorize the stimulus on the basis of these similarities.

More recently, Nearey and Miller and colleagues support a more elaborate view of phonetic category representation which contains more information than just that found for prototypes. Miller (1994) claims that representations of phonetic categories are essentially graded. This claim is based on the finding that category members vary in their perceived category goodness. Miller's position must be interpreted as mainly contrasting with the classical categorical perception concept, where members of the same category are thought to be perceptually entirely equivalent. In principle, graded category structure may derive from a basic prototype representation, as Miller (1984) acknowledges, where members close to the prototype are judged better exemplars than members further away from the prototype. Miller does suggest however, that phonetic categories actually incorporate distributional information. Nearey and colleagues (Nearey & Assman, 1986; Assman, Nearey & Hogan, 1982; Andruski & Nearey, 1992; Hillenbrand & Nearey, 1999) take a more quantitative stance. Using the Normal A-Posteriori Probability (NAPP) model, they modeled listeners' representations of vowel categories as multidimensional Gaussian distributions and showed that a-posteriori vowel probabilities based on their model gave very good predictions of listeners' categorization for a given set of vowel stimuli. Henceforth, we will indicate the class of theories which assume that phonetic categories are represented as distributions (of some form) as the Distribution theory.

Finally, a contemporary hypothesis concerning phonetic categorization simply denies the

existence or involvement of a sublexical layer in human speech recognition, instead assuming that words are represented by many, possibly all, previously encountered exemplars of the word (Johnson, 1997a, b; Goldinger, 1997). Henceforth this categorization theory will be indicated as the Exemplar theory. From this perspective, phonemes are not explicitly represented at all and what listeners exactly do in phonetic categorization tasks is not of central importance in understanding how human speech recognition works. Although it is logically possible to formulate an exemplar theory of speech perception with a sublexical layer containing phoneme exemplars, such a theory has, to our knowledge, not been proposed.

Despite twenty years of experimenting, the issue of the basic mechanisms underlying perceptual categorization has not been resolved. In speech perception research, the number of experiments addressing the basic mechanisms in phonetic categorization is small as compared to research on visual categorization (see, e.g., Maddox & Ashby, 1998; Nosofsky, 1998). While there is currently no consensus, neither in the fields of speech perception nor of general perceptual categorization, theories of general perceptual categorization have the advantage that they are mathematically fully developed and the subject of intense experimental evaluation. The present research therefore attempts to apply some of the methods and models of the visual categorization literature to the problem of phonetic categorization.

A major problem hindering a direct transfer of the methods to the speech domain is that we as experimenters do not have any control over the "training corpus" that participants have been exposed to. Throughout their lives, while hearing other people speak, adult listeners have heard large numbers of instances of the phonemes in their language. Both the basic categorization mechanism employed by listeners, as well as a number of system "parameters" (boundary locations, prototype locations, or distribution covariance matrices) may be based on this - unknown - training corpus. This poses two problems. First, the training corpus will differ among listeners, and second, we cannot freely manipulate the training corpus to test certain

theoretical predictions.

One methodological approach capable of overcoming the difficulties stemming from the lack of control over the training corpus is to study the categorization of non-speech sounds.

The present study employs this methodology.

Our experimental approach employs the method of Externally Distributed Stimuli (EDS). We built on the idea of Lee & Zentall (1966) that variation of the training distributions should cause different categorization theories to predict different patterns of categorization function slopes. At the same time, however, we wanted to create an experimental situation which is similar to that of the phonetic categorization experiment. This led us to adopt a methodology with quite distinct training and test phases. In the experiments reported below, the EDS method was used for training the participants, who received feedback after every trial. In the test phase, on the other hand, a stimulus continuum was used and no feedback was given, thus mimicking the standard phonetic categorization task.

The stimuli used in the present study differ in a number of regards from natural speech sounds. First, they are non-speech sounds that resemble speech sounds in certain crucial aspects. We believe that the use of non-speech is warranted because it is the best way to control for differences in participants' previous exposure to speech. Second, our stimuli differ in only a single dimension while natural speech varies along many dimensions (including frequency, duration, and amplitude). While we acknowledge these differences, we adopt the present strategy of studying simple auditory stimuli because, relative to visual categorization, phonemic categorization is as yet not well understood. Only when an account of the categorization of relatively simple auditory stimuli has been developed can research begin to address the categorization of more complex signals that will increasingly resemble speech sounds. The current study should therefore be considered a first step towards understanding the process of phonetic categorization.

The remainder of the paper is organized as follows. First, we present the general methodology for all four reported experiments. Next, the categorization theories are defined mathematically and their predictions of listeners' categorization functions are derived. Subsequently, four experiments are presented which test the theories. Quantitative model-based analyses are then described including a new categorization model. Finally, the results are discussed and interpreted within the context of speech perception.

General method

In all experiments reported below we trained listeners on a categorization problem involving two categories, A and B. Categories A and B were defined by overlapping one-dimensional Gaussian probability-density functions pdf_A and pdf_B , characterized by means μ_A and μ_B and standard deviations σ_A and σ_B . On a given trial in the training phase, a stimulus was randomly drawn from pdf_A or pdf_B and played to the listener. He or she had to label the stimulus as either A or B, after which visual feedback was given on the correct response. After completing the training phase, listeners entered the test phase. Here they performed the same task, but this time without getting feedback.

As indicated in the introduction, the methodology that we used for distinguishing between the four models of categorization had two essential features. First, using the EDS technique of Lee and Zentall (1966), four different training conditions were used. These were created by orthogonally combining two levels of variance and two levels of overlap of pdf_A and pdf_B . The left-most column of Figure 1 gives a graphical representation of the four training conditions. Within conditions, σ_A and σ_B were always equal. In conditions 1, 2, 3, and 4, the distance $\Delta\mu$ between means μ_A and μ_B was set to 5, 10, 10, and 20 just-noticeable differences (jnds), respectively, on the associated psychological dimension. Standard deviations σ_A and σ_B were 3.704 jnds in conditions 1 and 2, and 7.407 jnds in conditions 3 and

4. As a result, the overlap of pdf_A and pdf_B was large in conditions 1 and 3 and small in conditions 2 and 4, with theoretically optimal classification rates (using a noise-free boundary-based classification rule) of 75.5% in conditions 1 and 3, and 91.8% in conditions 2 and 4. Table 1 summarizes the numerical parameters of the four training conditions.

Probability-density functions pdf_A and pdf_B were represented by 110 stimuli each. Analogous to Lee and Zentall (1966), parameter values were sampled in such a way that the interval between any pair of consecutive parameter values corresponds to a constant probability interval on the cumulative distribution function associated with the pdf of the category.

The second feature of our method was that in the test phase we used a stimulus continuum to scan subjects' categorization across a relevant section of the psychological dimension ψ under study. The test phase was therefore similar to the common phonetic categorization experiment employing a phonetic continuum. In the test phase, the same stimulus continuum was used across all four training conditions. Thus, any differences in the resulting categorization functions in the four conditions would be due to differences in training only. The test continua consisted of 11 stimuli with equidistant parameter values, whose lowest and highest values coincided with means μ_A and μ_B in condition 4.

The combination of the four distribution-based training conditions and the subsequent fixed test continuum allowed us to experimentally distinguish between the categorization theories. As shown below, the theories predict different patterns of categorization function slopes across the four conditions.

Theoretical predictions

Prototype theory

According to the Prototype theory, the only information about the categories that is stored is the location of the category prototypes. Assuming Gaussian similarity functions (e.g.,

Nosofsky, 1986), the probability $p(A|S_i)$ of assigning stimulus S_i , defined by parameter value ψ_i , to category A is a logistic function (for mathematical derivations, see Appendix A). The slope s of this logistic function is proportional to the distance between the means of the pdfs used in the training phase. Therefore the Prototype theory predicts that the slopes of the categorization functions in conditions 2 and 3 are twice the slope in condition 1, while the slope in condition 4 is four times bigger than the slope in condition 1, i.e.

$s_4 = 2s_3 = 2s_2 = 4s_1$. This is graphically represented in the second column of Figure 1. The top panel, associated with condition 1, has the shallowest categorization curves, while the bottom panel (condition 4) has the steepest. Condition 2 and 3 have equal slopes of intermediate values.

Distribution theory

The Distribution theory assumes that subjects' category representations not only include category means but also measures of spread. When the category distributions are approximately normal, subjects are assumed to model the categories by normal distributions, estimating for each category a mean and a standard deviation (for the unidimensional case). As was the case for the Prototype theory, $p(A|S_i)$ is a logistic function of ψ_i (see Appendix A). The categorization function's slope s is proportional to the distance between the means of the training pdfs divided by their variance. As a result, condition 3 is predicted to have the shallowest categorization functions, while condition 2 will have the steepest, with a slope that is four times that for condition 3. The categorization functions for conditions 1 and 4 are predicted to be identical, with slopes that are two times bigger than the slope in condition 3. In short, $s_2 = 2s_1 = 2s_4 = 4s_3$.

Exemplar theory

The Exemplar theory claims that categories are represented by the complete set of training items, while in the Distribution theory the categories are parametric abstractions of the training items. Both theories assume a response selection mechanism based on a relative goodness rule, although some recent versions of exemplar models used a deterministic response rule (Nosofski & Zaki, 2002).

Irrespective of the values of sensitivity parameter k and Minkowski metric (the power used in the distance function, see e.g., Ashby & Maddox, 1993) in the Exemplar theory, the predicted qualitative pattern of slopes across the four conditions for the Exemplar theory is expected to be identical to the pattern predicted by the Distribution theory: smallest slope in condition 3, largest in condition 2, and intermediate in conditions 1 and 4. Consequently, the predicted response patterns for the Distribution and Exemplar theories are expected to be so similar that they cannot be distinguished experimentally in the present set of experiments. Henceforth, we will therefore pool the Distribution and Exemplar theories under the heading Distribution theory. It should be noted, however, that over the years the exemplar model has been implemented in a variety of ways. Some of these implementations might lead to behavior that is different from that of the distribution models used in this paper.

Decision-Bound theory

Finally, the predictions for the Decision-Bound theory are straightforward. During training, subjects are assumed to learn the position of the optimal boundary between categories A and B. This boundary is subsequently used in the categorization of the test stimuli. If the psychological effect of a stimulus falls to the left of the boundary, the stimulus is labeled A, otherwise it is labeled B.

Under the Decision-Bound theory, the slopes of the categorization functions are determined by perceptual noise only. As the test phase is identical for the four conditions, the

perceptual noise is also identical, which leads to the prediction that the slopes of the categorization functions are equal across the four conditions.

Note that the Decision-Bound theory predicts cumulative normal (probit) categorization functions, rather than the logistic ones predicted by Prototype and Distribution theories. The two are, however, very similar and difficult to distinguish experimentally. The right-most column of Figure 1 gives the predicted categorization functions for the four conditions assuming that the standard deviation of the pdf associated with the perceptual noise equals 3.704 jnds in all four conditions.

Stimulus considerations

The experimental paradigm defined above was applied to two auditory dimensions that are known to be of major importance in the categorization of speech sounds: frequency of a spectral prominence or "formant" and duration. For example, in the categorization of the English vowels / ε / and / æ /, as in the words "bed" and "bad", respectively, both vowel duration and frequency of the first formant $F1$ are known to play a role with / ε / having shorter duration and lower $F1$ than / æ / (e.g., Mermelstein, 1978; Whalen, 1989).

Although we expressly used speech-like dimensions in our stimuli, at the same time we endeavored to prevent the subjects from explicitly using speech sounds as reference categories. The reason for this is that the experimental paradigm for distinguishing between the various theories was based on the systematic variation of the training distributions. If subjects would nevertheless adopt categorization strategies involving speech categories ("respond A if it sounds like / ε / and B if it sounds like / æ /"), our experiments would not measure what they were intended to measure.

We solved this problem by using a synthetic inharmonic tone complex as the base signal from which the experimental stimuli were derived. The inharmonic base signal sounded very

different from speech, whose source is a mixture of a harmonic signal and noise. After taking the experiment, subjects typically described the sounds as computer sounds, organs, or horns.

The experimental stimuli were created by filtering the base signal, thus creating the spectral prominence, and truncating the filtered signal to a desired duration. In Experiments 1 and 2 the frequency of the spectral prominence was varied, with all stimuli having the same duration. In Experiments 3 and 4 the duration of the stimuli was varied, keeping the formant frequency constant.

Experiment 1

Method

Participants. Sixty-seven students at Nijmegen University were recruited as participants for Experiment 1. All reported normal hearing and had Dutch as their native language.

Stimuli. As mentioned earlier, all stimuli were derived from a single “base signal”. This base signal was constructed by adding sinusoids with exponentially spaced frequencies. The base signal $B(t)$ is defined by

$$B(t) = A \sum_{n=0}^N \sin(2\pi f_0 F^n t) \quad (1)$$

where A is a constant amplitude factor, $f_0 = 500$ Hz is the frequency of the lowest partial, $F = 1.15$ is the frequency ratio of two successive partials, t represents time, and $N = 17$ is the number of partials. The 17 partials constituting the base signal spanned a frequency range of 500 Hz to 4679 Hz.

Next, the base signal was filtered by a single resonance or formant, implemented as a second order Infinite Impulse Response (IIR) filter. The bandwidth of the filter was .2 times the filter’s resonance frequency. Finally, the stimulus was truncated to the desired duration,

applying linear 5 ms ramps at onset and offset to avoid clicks.

In Experiment 1, the frequency of the formant was varied, while stimulus duration was kept constant at 150 ms. Perceptual representation of frequencies, be it pure tone frequencies or formant frequencies, is often modeled by the Equivalent Rectangular Bandwidth scale (ERB, Glasberg & Moore, 1990). The ERB scale, obtained through detailed psychoacoustic experiments, is designed such that pure tones differing a fixed number of ERBs produce excitation patterns whose maxima have a fixed distance along the basilar membrane. We accordingly applied the earlier defined training-testing scheme (Figure 1) to the formant frequency expressed in ERBs. We chose to vary the formant frequency roughly within the natural region of the second formant in speech.

On the basis of formant-frequency discrimination data for isolated stationary vowels, Kewley-Port and Watson (1994) estimated the Weber fraction for discrimination of formant frequencies at .015 in the frequency region of the second formant. From this, it follows that at 1500 Hz 1 jnd corresponds to 23 Hz, or .12 ERB. Using the jnd of .12 ERB for formant frequency and the earlier defined pdf means and standard deviations expressed in jnds (see Table 1), we defined pdf_A and pdf_B for the four training conditions along the ERB axis, with midpoint $\frac{1}{2}(\mu_A + \mu_B)$ at 18.7 ERB, which corresponds to 1500 Hz. Table 2 lists the resulting means and standard deviations, expressed in ERB and Hz, for pdf_A and pdf_B in conditions 1 to 4.

The stimulus continuum for the test phase contained 11 stimuli. The formant frequencies of these stimuli were obtained by equidistant sampling of the ERB scale across the interval $[\mu_{A4}, \mu_{B4}]$ (means of pdf_A and pdf_B in training condition 4), resulting in the following formant frequencies: 1288, 1329, 1370, 1412, 1455, 1500, 1546, 1593, 1641, 1690, 1741 Hz. The same test continuum was used in all four experimental conditions.

In order to estimate the discriminability of the stimuli in the test continuum, we carried

out an AX (same different) discrimination experiment. This experiment is described in the Appendix. The results showed that the average discriminability of two consecutive stimuli corresponded to a d' of 1.0. This value was constant across the stimulus continuum, except for the pair 7-9, which had a higher d' than the other pairs.

Procedure. All participants first completed a training phase, after which they entered the test phase. In the training phase, two blocks of stimuli were presented, each containing all 220 training stimuli in a different randomized order. Different randomizations were used for different participants. Participants were seated in a soundproof booth in front of a computer screen. They were asked to assign sounds to either of two categories. On a given trial a stimulus was presented binaurally through Sennheiser headphones, after which the participant categorized the stimulus by pressing either of two response buttons labeled A and B. After the button press the correct response was shown on the screen for 800 ms. The next stimulus was presented 700 ms after offset of the visual feedback. Before the start of training, participants were told that it would be impossible to score 100% correct, even towards the end of the training phase. Training was preceded by five familiarization trials involving stimuli drawn randomly from the 220 training stimuli. The task for the participant was the same.

The training phase was followed by a short break, after which participants entered the test phase. Here subjects were presented with 5 blocks of stimuli, each containing a different randomized ordering of 4 repetitions of each of the 11 test stimuli. Participants were asked to respond as quickly as possible without sacrificing accuracy. 1.5 s after a button press the next stimulus was played. No feedback was given on the correct response. After completing the experiment, participants filled out a short questionnaire asking them (1) to describe their categorization strategy, (2) whether the sounds were similar to any sound they know, and (3) whether they thought the stimuli sounded at all like speech sounds. The entire experiment (training and test phase) took approximately 40 minutes.

Results

Training. Pilot experiments indicated that a fraction of listeners had not grasped the task after completion of the training phase. We defined the following objective criterion for eliminating the data of such participants from the data set: A participant's data was only used for further analysis if he or she got at least 34 out of the last 55 training stimuli correct (corresponding to performing above chance level at the $p = .05$ level). Nineteen out of 67 participants did not pass the training criterion, and their results were discarded. This left 12 participants per condition who did pass the criterion. For each participant the training data were divided into eight consecutive blocks of 55 trials and performance (percent correct) was calculated for each block. Average performance for blocks 1 to 8 in each of the four training conditions is plotted in Figure 2.

Figure 2 shows evidence of learning over the course of training. The average improvement from the first to the last training blocks was 15.3 percentage points. An analysis of variance (ANOVA; $MSE = 178$) on the difference in performance for blocks 8 and 1 with independent variable Condition showed that this improvement was significant ($F(1, 44) = 63.6, p < .0005, \eta^2 = .59$). There was no significant effect of condition ($F(3, 44) = 1.7, n.s.$), so the improvement was equal across the four conditions.

Participants picked up on the task reasonably quickly. Average performance during the first training block was already 10.6 percentage points above chance level (50%). An ANOVA ($MSE = 193$) on the difference in performance in block 1 and chance level, with independent variable Condition, showed this difference to be significant, $F(1, 44) = 28.2, p < .0005, \eta^2 = .39$. Condition did not have an effect on this measure ($F(3, 44) = 2.0, n.s.$).

Finally, participants performed significantly below theoretically optimal performance (TOP, 75.5% in conditions 1 and 3, 91.8% in conditions 2 and 4) during the final training

block. This was shown by an ANOVA ($MSE = 28.6$) on the difference between TOP and block 8 performance, $F(1, 44) = 97.3, p < .0005, \eta^2 = .69$, Condition having a significant effect ($F(3, 44) = 4.2, p = .01, \eta^2 = .22$). A posthoc Student-Newman-Keuls test showed that performance was further removed from TOP in condition four compared to conditions one and three. However, the average deviation from optimal performance was only 7.6%, and was probably mainly due to noise in the categorization process rather than premature termination of training.

Testing. The four panels in Figure 3 present categorization functions of all twelve individual participants for the test continuum in each of the four experimental conditions of Experiment 1.

Figure 3 leaves no doubt that all participants had learned how to do the task. Stimuli with low formant frequencies (low stimulus numbers) were given predominantly A responses, while B responses were preferred for stimuli with high formant frequencies (high stimulus numbers). Figure 3 also suggests that all participants behaved very similarly, both within and across conditions.

To test for differences in categorization function slopes between conditions, we carried out the following analyses. First, logistic regression (LR, e.g., Agresti, 1990) analyses were performed on the data of each individual subject. In these analyses the following model was fitted to the data of each participant.

$$\ln \frac{p(A|\psi_i)}{p(B|\psi_i)} = s(\psi_i - M) \quad (2)$$

where $p(A|\psi_i)$ is the probability of responding A to stimulus S_i characterized by value ψ_i of the perceptual representation (in this case ERB rate) of the relevant stimulus parameter (formant frequency). s and M represent the slope and midpoint of the categorization function,

respectively. Model (2) was fitted to the data of each participant minimizing the deviance G^2 (Agresti, 1990).

The LR analyses produced a slope s and a midpoint M for each participant. To test for differences in mean categorization function slopes in the four conditions, a one-way ANOVA was carried out on dependent variable slope with independent variable Condition.

The ANOVA ($MSE = .095$) showed that the mean categorization slopes in conditions one through four were not significantly different ($F(3, 44) = 1.7$, n.s., $\eta^2 = .11$). Because the Prototype theory predicted a slope ratio of 4 between conditions 4 and 1, we carried out an Anova directly comparing the slopes of these two conditions. No significant difference was found ($F(1, 22) = 1.3$, n.s., $MSE = .14$, $\eta^2 = .054$). The ratio of the mean slopes of conditions 4 and 1 was .85, deviating strongly from the ratio of 4 predicted by the Prototype theory. Distribution theory predicted a ratio of 4 between the slopes in conditions 2 and 3. An Anova ($MSE = .051$) comparing the slopes of conditions 2 and 3 yielded a marginally significant result ($F(1, 22) = 3.8$, $p = .065$, $\eta^2 = .15$). The ratio of the mean slopes for conditions 2 and 3 was 1.2.

These results do not provide conclusive support for any theory. The non-significance of the differences between the mean slopes of all four conditions is in agreement with Decision-Bound theory, but this is a null-result. The marginal significance of the difference between the mean slopes of condition 2 and 3 gives partial support for the Distribution theory, but the experimental slope ratio of 1.2 strongly deviates from the expected ratio of 4. The only firm conclusion we can make based on these results is that they are in disagreement with Prototype theory.

Questionnaire. Out of the 48 participants who passed the training criterion, 46 described their categorization strategy essentially as “choose A if the sound is low/dull, choose B if it is high/sharp.” The remaining two participants both described their strategy as choose “A if it

sounds like ‘oh’, choose B if it sounds like ‘eh’”. We compared the results of this subject during the test phase to those of other participants in the same condition, and they were very similar.

In response to question two, more than half of the participants said that the sounds did not remind them of any sound they know. Typical answers of the other participants were “computer sounds,” “organ,” and “horn.” Apart from the two subjects mentioned above, nobody mentioned speech sounds, phonemes, vowels or anything similar in their answers to questions 1 or 2.

When, finally, participants were explicitly asked if they thought the sounds were speech-like (question 3), 34 out of 48 responded no. One of the remaining 14 said all sounds were like ‘aa’, one said all were like ‘ee’, the other twelve mentioned that category A sounded like ‘oh’ or a similar vowel and B like ‘ih’ or a similar vowel, but added that this similarity had not occurred to them until they were explicitly asked in question three (except for the two subjects who had already reported the similarity to speech in question one). Based on these results we concluded that we had generally been successful in preventing participants from using speech sounds as reference categories in Experiment 1.

Discussion

The results of Experiment 1 fully contradicted Prototype theory and gave partial support for Decision-Bound theory and Distribution theory. Although the support for Decision-Bound theory seems strongest, it is based on essentially a null-result. In pursuit of positive effects in support of the Decision-Bound theory, we ran a second experiment in which the training was identical to that of Experiment 1, but in which the test continua were changed.

The rationale of Experiment 2 is based on Durlach and Braida's (1969) theory of perceptual noise in Decision-Bound theory. Durlach and Braida hypothesized that the total variance of perceptual noise has three components: sensory variance associated with irreducible sensory (neural) noise, trace variance associated with comparisons of two consecutive sounds (as in discrimination tasks), and context variance associated with the noisy comparison of a stimulus to 'perceptual anchors', e.g., the edges of the continuum used in a categorization experiment. In identification and categorization tasks, trace variance is assumed to be zero, in which case the total perceptual variance σ^2 is the sum of sensory and context variance:

$$\sigma^2 = \beta^2 + H^2W^2 \quad (3)$$

where β^2 is the sensory variance, H is a constant, and W is the width of the test continuum expressed in psychophysical units. Eq. (3) predicts that if W is small, i.e., in the order of magnitude of a few jnd, context noise is small and therefore perceptual noise is dominated by sensory noise. If, on the other hand, W is large, i.e., the continuum spans many jnds, context noise dominates.

In our experiments we aim to 'sample' a one-dimensional psychophysical space using a test continuum. As long as context noise is negligible, the variance of the perceptual noise is not influenced by the width of the test continuum. Consequently, if we would make the width of the continuum progressively smaller, the resulting categorization function would become more and more shallow. For example, if a given width W_1 would produce a categorization function which runs from 25% to 75%, a test continuum width $W_2 = 0.5W_1$ would produce a shallower function running from, roughly, 37% to 63%. In conclusion, as long as W is small, the categorization function $P(A|S_i)$ (the probability of choosing A as a function of stimulus number i) depends on the value of W , with a smaller W leading to a shallower function.

In the other extreme case, when W is large, perceptual noise is dominated by context noise and sensory noise is negligible. In this case, halving the width of the test continuum will also halve the standard deviation of the perceptual noise. Paradoxically, the halved test continuum will sample an area with ‘halved’ noise and the categorization function $P(A|S_i)$ will be unaltered. Thus, as long as W is large, $P(A|S_i)$ does not depend on the value of W .

Imagine that, over the course of many experimental sessions, we would sample the same one-dimensional perceptual space using a set of test continua with widths ranging from close to zero to many jnds. For the very small width the resulting categorization function would be basically flat and with increasing W the categorization function would become steeper. However, rather than becoming ‘infinitely’ steep for very large W , the slope would approach a certain asymptotic value, which cannot be transgressed by further increasing W .

In the context of the present experiments it is unclear where exactly on the scale of dominant sensory noise to dominant context noise we are. However, as long as sensory noise plays a significant role we can use a manipulation of the width of the test continuum to produce a positive effect of experimental condition on the slope of $P(A|S_i)$.

Figure 4 presents theoretical categorization functions $P(A|S_i)$ for Experiment 2 as predicted by the three categorizations theories. The two conditions of experiment 2 were new versions of conditions 2 and 3 in the previous experiment, and are indicated as conditions 5 and 6. The test continuum in condition 5 was half as wide as it was in condition 2, whereas in condition 6 it was twice as wide as it was in condition 3, as indicated by the horizontal bars in the left-most panels of Figure 4.

Given our choice of test continuum widths in the new experiment, Prototype theory (second column in Figure 4) predicts categorization function slopes in conditions 5 and 6 to be identical to those in the old conditions 1 and 4, respectively: $s_4 = s_6 = 4s_5 = 4s_1$. As mentioned earlier, Distribution theory (third column) predicts equal categorization slopes in

conditions 1, 5, 6, and 4. For Decision-Bound theory we can only make a qualitative prediction at this point because the value of constant H is unknown. The prediction is $s_5 < s_1 = s_4 < s_6$. For the purpose of Figure 4 (fourth column), it was arbitrarily assumed that sensory noise had a variance equal to variance σ^2 of the stimulus distributions in condition 1, while context variance was assumed to equal σ^2 in conditions 1 and 4, $\frac{1}{4}\sigma^2$ in condition 5, and $4\sigma^2$ in condition 6.

Method

Experiment 2 consisted of two conditions, indicated as conditions 5 and 6. Condition 5 and 6 employed the same training as conditions 2 and 3 of Experiment 1, respectively. The width of the test continuum in condition 5 was half the original width, covering the interval $[\mu_{A2}, \mu_{B2}]$. In condition 6 the test continuum was twice as wide as the original one, covering the interval $[1\frac{1}{2}\mu_{A4} - \frac{1}{2}\mu_{B4}, 1\frac{1}{2}\mu_{B4} - \frac{1}{2}\mu_{A4}]$. In all cases the number of stimuli in the test continuum was 11, as before.

Participants. Thirty-two students at Nijmegen University were recruited as participants for Experiment 2. All reported normal hearing and had Dutch as their native language.

Stimuli. The training stimuli of conditions 5 and 6 were identical to those of conditions 2 and 3 of Experiment 1, respectively. The test continua of conditions 5 and 6 both contained 11 stimuli. The formant frequencies of the stimuli for condition 5 were obtained by equidistant sampling of the ERB scale across the interval $[\mu_{A2}, \mu_{B2}]$, resulting in the following formant frequencies: 1391, 1412, 1434, 1455, 1478, 1500, 1523, 1546, 1569, 1593, 1617 Hz. For condition 6, the equidistant sampling was done on the interval $[1\frac{1}{2}\mu_{A4} - \frac{1}{2}\mu_{B4}, 1\frac{1}{2}\mu_{B4} - \frac{1}{2}\mu_{A4}]$, resulting in the following formant frequencies: 1103, 1174, 1249, 1329, 1412, 1500, 1593, 1690, 1793, 1902, 2016 Hz.

Procedure. The procedure of Experiment 2 was identical to that of Experiment 1, except

that no questionnaires were taken, because the questionnaires of Experiment 1 had convinced us that speech-based strategies were extremely rare.

Results

Training. Eight participants did not pass the training criterion. Their results were discarded. This left twelve subjects in each of the two conditions of Experiment 2.

Figure 5 presents average performance for blocks 1 to 8 in conditions 5 and 6. Unsurprisingly, the learning curves of Figure 5 are similar to those of Figure 2. The average improvement from the first to the last training blocks in conditions 5 and 6 is 12.1%. An ANOVA ($MSE = 47.3$) on the difference in performance for blocks 8 and 1 with independent variable Condition showed that this improvement was significant ($F(1, 22) = 74.5, p < .0005, \eta^2 = .77$). There was no significant effect of Condition ($F(1, 22) = .013, n.s.$), so the improvement was equal for the two conditions.

Again learning started quickly. Average performance during the first training block was 13.5 percentage points above chance level. An ANOVA ($MSE = 49.9$) on the difference in performance in block 1 and chance level, with independent variable Condition, showed this difference to be significant, $F(1, 22) = 87.4, p < .0005, \eta^2 = .80$. Condition had a significant effect on this measure ($F(1, 22) = 13.6, p = .001, \eta^2 = .38$). Unsurprisingly, block 1 performance was better for condition 5 than condition 6.

Finally, participants again performed significantly below TOP (91.8% in condition 5 and 75.5% in condition 6,) during the final training block, as shown by an ANOVA ($MSE = 44.9$) on the difference between TOP and block 8 performance ($F(1, 22) = 34.2, p < .0005, \eta^2 = .61$), Condition having a significant effect ($F(1, 22) = 5.0, p = .04, \eta^2 = .18$). Performance in the final block was closer to TOP in condition 6 than in condition 5. However, average performance in the final block was only 8.0%, below TOP.

Testing. The two panels in Figure 6 present categorization functions $P(A|S_i)$ of all twelve individual participants for the test continuum in conditions 5 and 6 of Experiment 2. Comparison of Figure 6 to Figure 4 reveals that listener performance is more variable in conditions 5 and 6 than in conditions 1 to 4. The heightened variability in condition 5 is not surprising, given the smaller test continuum width. For the variability in condition 6, on the other hand, we have no explanation. We do note, however, that most of the variability is caused by two participants (the plus sign and the right-pointing triangle in Figure 6B) who for unknown reasons deviate somewhat from the rest. We did not have any objective criterion to remove these participants.

A one-way Anova ($MSE = .080$) shows that on average the categorization functions are significantly steeper in condition 6 than in condition 5 ($F(1, 22) = 4.3, p = .050, \eta^2 = .16$). This pattern of categorization-function slopes is compatible with the Decision-Bound theory.

An ANOVA ($MSE = .090$) including all six conditions (1 to 4 for Experiment 1 and 5 and 6 for Experiment 2) shows a significant effect of condition on categorization-function slope ($F(5, 66) = 6.35, p < .0005, \eta^2 = .33$). A Student-Newman-Keuls post-hoc test reveals that categorization functions in condition 5 are on average significantly shallower than conditions 1 through 4, and condition 6 is shallower than condition 1. This general pattern is in reasonable, though not perfect, agreement with the Decision-Bound theory.

Discussion.

In Experiments 1 and 2, six conditions were run investigating the categorization of sounds varying in formant frequency. The pattern of categorization-function slopes was in reasonable agreement with the Decision-Bound theory of categorization. First of all, we found no difference in the slopes across the four conditions of Experiment 1, as predicted by the Decision-Bound theory. Second, as also predicted by this theory, the slope in condition 5 was

significantly shallower than those in conditions 1 through 4. Condition 6 proved somewhat problematic. Whereas Decision-Bound theory predicts the steepest slope in condition 6, it was in fact not significantly different from that of any other condition except condition 1, compared to which it was shallower.

Theoretically, the expected increase in slope for condition 6 is smaller than the expected decrease in slope for condition 5 because, with increasing stimulus range, the slope increases progressively less than would be expected if performance were limited by sensory noise alone. It is therefore expected that a difference between condition 5 and conditions 1 to 4 will reach significance earlier than the difference between condition 6 and conditions 1 to 4. Therefore, we consider the "asymmetry" in the slope pattern not to be in disagreement with the Decision-Bound theory. The shallower slope of condition 6 compared to condition 1 remains in disagreement with the Decision-Bound theory, however. Nevertheless, the Decision-Bound theory explains the data better than the rival Prototype and Distribution theories, although the latter received weak support from the marginally significant difference between the slopes of conditions 2 and 3.

By varying the frequency of a resonance or formant, we have varied an acoustic parameter which is generally viewed as very important for speech perception. Another such parameter is duration. To be able to draw general conclusions about the categorization mechanisms underlying speech perception, we thought it necessary to test whether the Decision-Bound mechanism that we found for formant-frequency categorization would apply to the categorization of duration. We therefore decided to run the same set of experiments again, using similar stimuli, but this time varying stimulus duration, while keeping formant frequency constant.

Method

The methodology of Experiment 3 was identical to that of Experiment 1, except for the stimuli.

Participants. Fifty-three students at Nijmegen University were recruited as participants for Experiment 3. All reported normal hearing and had Dutch as their native language.

Stimuli. In Experiment 3, stimulus duration was varied, while the frequency of the formant was kept constant at 1500 Hz, which was the midpoint between the means μ_A and μ_B in Experiment 1.

The perceptual representation of duration has received much less attention in the psychophysical literature than that of frequency. Abel (1972) investigated duration discriminability of pure tones and noise bursts as a function of duration. The study showed that for durations from 40 ms to 640 ms discrimination closely followed Weber's law, with a Weber fraction of approximately .1. We carried out a pilot duration categorization experiment using this Weber fraction. The results showed that the stimuli in the duration continuum were much easier to discriminate than those in the formant frequency continuum. Further pilot experiments indicated that assuming a Weber fraction of .05 for duration discrimination resulted in comparable discriminability of the formant frequency and duration stimuli. Based on these results, we defined psychological duration D , expressed in unit [d], as

$$D = 10 \log T \quad (4)$$

where T is physical duration, expressed in ms. One jnd for duration corresponds to .5 d. Using Eq. (4), we defined pdf_A and pdf_B for the four training conditions along the D axis, with midpoint $\frac{1}{2}(\mu_A + \mu_B)$ at 50.11 d, which corresponds to 150 ms. Table 3 lists the resulting means and standard deviations expressed in d and ms for pdf_A and pdf_B in conditions 1 to 4.

As in Experiment 1, the stimulus continuum for the test phase contained 11 stimuli. The

durations of these stimuli were obtained by equidistant sampling of the D scale across the interval $[\mu_{A4}, \mu_{B4}]$, resulting in the following durations: 91.0, 100.5, 111.1, 122.8, 135.7, 150.0, 165.8, 183.2, 202.5, 223.8, 247.3 ms. The same test continuum was used in all four experimental conditions.

The discriminability of the duration stimuli was tested in the same discrimination experiment as the formant frequency stimuli (see the Appendix). The average discriminability of two consecutive stimuli on the duration continuum corresponded to a d' of .8, which was not significantly different from the d' for formant frequency discrimination (1.0). Again discriminability was constant across the test continuum.

Procedure. The procedure of Experiment 3 was identical to that of Experiment 1.

Results

Training. Four out of 53 participants did not pass the training criterion, and one subject responded randomly during the test phase, having misunderstood the instructions. Their results were discarded. This left 12 participants per condition. Figure 7 presents average performance across the eight training blocks.

Learning was so quick that subjects were already performing close to ceiling during the first block of training. The average improvement from the first to the last training blocks was only 5.5 percentage points. An ANOVA ($MSE = 78.4$) on the performance difference for blocks 8 and 1 with independent variable Condition showed that this improvement was significant ($F(1, 44) = 18.7, p < .0005, \eta^2 = .30$). There was no effect of condition ($F(3, 44) = .9, n.s.$).

Participants' learning was extremely fast. The average performance during the first training block was already 23 percentage points above chance level (50%). An ANOVA ($MSE = 63.1$) on the difference in performance in block 1 and chance level, with independent

variable Condition, showed this difference to be significant ($F(1, 44) = 386, p < .0005, \eta^2 = .90$). Condition proved to have a significant effect on this measure ($F(3, 44) = 15.6, p < .0005, \eta^2 = .52$), and a posthoc Student-Newman-Keuls test showed, not surprisingly, that block 1 performance was higher in conditions 2 and 4 than in the other two conditions.

Finally, participants performed significantly below TOP (75.5% in conditions 1 and 3, 91.8% in conditions 2 and 4) during the final training block. This was shown by an ANOVA ($MSE = 26.8$) on the difference between TOP and block 8 performance ($F(1, 44) = 56.3, p < .0005, \eta^2 = .56$), Condition having no significant effect ($F(3, 44) = .98, n.s.$). The average deviation from optimal performance was only 5.6%.

Testing. The four panels in Figure 8 present categorization functions of all twelve individual participants for the test continuum in each of the four experimental conditions of Experiment 3.

Figure 8, like the results for formant-frequency categorization (Figure 3), shows relatively little variability between subjects within conditions. A and B responses were preferred for short stimuli (low stimulus numbers) and long stimuli (high stimulus numbers), respectively.

As for Experiment 1, we calculated slope and midpoint for each categorization curve by means of logistic regression, and subjected the slope values to a one-way ANOVA with independent variable Condition. The analysis ($MSE = .14$) showed a significant effect of Condition, $F(3, 44) = 4.6, p = .007, \eta^2 = .24$. A post-hoc Student-Newman-Keuls test revealed that the mean categorization function slope was significantly smaller in condition 3 than in condition 2, as predicted by the Distribution theory. The ratio of mean slopes for conditions 2 and 3 was 1.7, which is smaller than the predicted ratio of 4.

Questionnaire. All participants spontaneously described categories A and B as short versus long, respectively. When asked what sounds the stimuli reminded them of, none of the

participants mentioned speech sounds. As in Experiment 1, typical answers were computer sound, organ, and horn. When participants were explicitly asked whether the stimuli sounded at all like speech, five mentioned a single vowel, while four participants mentioned a vowel pair. From these responses we concluded that none of the subjects explicitly used a categorization strategy involving speech sounds.

Experiment 4

Analogous to Experiment 2, we also decided to test categorization of duration by means of two continua that varied in width.

Method

The methodology of Experiment 4 was identical to that of Experiment 2, except for the stimuli.

Participants. Twenty-five students at Nijmegen University were recruited as participants for Experiment 4. All reported normal hearing and had Dutch as their native language.

Stimuli. The training stimuli used in conditions 5 and 6 of Experiment 4 were identical to those of conditions 2 and 3 of Experiment 3. The eleven-member test continuum of condition 5 had a range that was half that of the test continuum of Experiment 3. The stimulus durations were 116.8, 122.8, 129.1, 135.7, 142.7, 150.0, 157.7, 165.8, 174.3, 183.2, 192.6 ms. The eleven-member test continuum of condition 6 had twice the range of the test continuum of Experiment 3, with stimulus durations of 55.2, 67.4, 82.3, 100.5, 122.8, 150.0, 183.2, 223.8, 273.3, 333.8, 407.7 ms.

Procedure. The procedure of Experiment 4 was identical to that of the previous experiments, except that no questionnaires were taken.

Results

Training. One of the 25 participants did not pass the training criterion. Her results were discarded, leaving 12 participants per condition. Figure 9 presents average performance across the eight training blocks.

As expected, Figure 9 closely resembles Figure 7 in all respects. The average improvement from the first to the last training blocks was only 6.5 percentage points, which proved significant ($MSE = 118$, $F(1, 22) = 8.7$, $p = .008$, $\eta^2 = .28$). There was no effect of Condition on this improvement ($F(1, 22) = 1.2$, n.s.). Average performance during the first training block was 20 percentage points above chance level (50%). As in Experiment 3, the difference in performance in block 1 and chance level was significant ($MSE = 85.1$, $F(1, 22) = 115$, $p < .0005$, $\eta^2 = .84$). This difference was significantly larger in condition 6 than in condition 5 ($F(1, 22) = 24.4$, $p < .0005$, $\eta^2 = .53$). Also like in Experiment 2, participants performed slightly (6.9 percentage points) but significantly below TOP during the final training block ($MSE = 32.5$, $F(1, 22) = 35.1$, $p < .0005$, $\eta^2 = .62$). There was no effect of Condition on this difference, however ($F(1, 22) = 1.2$, n.s.).

Testing. Figure 10 presents individual categorization functions in conditions 5 and 6 of Experiment 4.

Like before, the slopes of each of the individual categorization functions of conditions 5 and 6 were subjected to a one-way ANOVA ($MSE = .12$) with independent variable Condition. The analysis showed that the categorization functions in condition 6 were significantly steeper than those in condition 5 ($F(1, 22) = 5.7$, $p = .03$, $\eta^2 = .21$). This result is in agreement with the Decision-Bound theory.

A combined analysis of the data of Experiments 3 and 4 (conditions 1 through 6; $MSE = .13$) confirmed that mean slopes were different across conditions, $F(5, 66) = 5.5$, $p < .0005$, $\eta^2 = .29$. A post-hoc Student-Newman-Keuls test revealed that the average categorization-function slope in condition 5 was significantly shallower than the slopes in

conditions 1, 2 and 4. In addition, the slope of condition 2 was significantly steeper than that of condition 3. The overall pattern found for the combined analysis lies between the patterns expected for the Distribution and the Decision-Bound theories.

Discussion

Experiments 3 and 4 tested the basic mechanism underlying the categorization of sounds varying in duration. The results showed evidence for two theories of categorization. In Experiment 3 we found that categorization-function slopes were larger in condition 2 than in condition 3, while the slopes for conditions 1 and 4 were in between. This pattern of slopes is in agreement with the Distribution theory. In Experiment 4, however, the slope was steeper in condition 6 than in condition 5, which is in agreement with the Decision-Bound theory. Thus, the combined results give partial support for two theories. The only theory that remains unsupported is the Prototype theory.

The combined results of the four experiments raise two important questions. First of all, how can the partial support for two theories be interpreted? A possibility is that aspects of the Distribution and Decision-Bound theories should be combined. Second, why do we find different results for duration and formant frequency? The results for stimuli varying in formant frequency supported the Decision-Bound theory, whereas the results for duration are in partial agreement with the Decision-Bound and Distribution theories. Both questions are addressed in the next sections.

Model analyses

The data analyses presented above concentrated on the qualitative patterns of categorization slopes across conditions. The Prototype, Distribution, and Decision-Bound models are, however, mathematically fully developed and allow for quantitative testing. Apart from a small

number of free parameters, each of the models can predict quantitative data for each of the six experimental conditions used in the experiments. In particular, such quantitative analyses may shed some light on the interesting but unsatisfactory finding that the duration stimuli seem to have been categorized by a mixture of Decision-Bound and distribution strategies.

Method

The model analyses were performed on individual data only. The reason for this choice is that the slope of pooled categorization curves is very sensitive to variation in the curve midpoint in the individual data. That is, summing two steep categorization curves with widely separated midpoints yields a shallow categorization curve. As the categorization function slope is the dependent parameter in our experiments, we thought such harmful effects of data pooling should be avoided.

To get optimal fits, we used the individual midpoints of the categorization functions estimated by the individual logistic regressions in our model analyses. Before calculating the goodness of fit for each individual subject, the predicted categorization function was shifted to coincide with that subject's midpoint.

The absence of sensory noise in Prototype or Distribution models can be viewed as either a basic assumption or an approximation for super-threshold categorization problems. Because we designed our stimuli such that test continuum neighbors were moderately confusable, the approximation may not apply, and we have to allow for the possibility that perceptual noise played a role even if the listeners in our experiments used a Prototype or Distribution-based categorization mechanism. We therefore fitted "expanded" versions of the Prototype and Distribution models which incorporated perceptual noise. In the case of the Prototype model, we only added context noise, because the addition of sensory noise was mathematically equivalent to a decrease in the decay of similarity, i.e., a lower value of parameter k .

For each class of model, a series of fits was made with increasing numbers of free parameters associated with (depending on the model class) the two kinds of perceptual noise and the decay of similarity. Using a overdispersion-based technique (e.g., McCullagh & Nelder, 1989), we determined for each model class which extra free parameters significantly improved the fit. The comparison of models of different classes was less straightforward, however. When models are not hierarchically related, i.e., none of the models is a special case of any other model, formal statistical testing is impossible. Recent studies comparing non-hierarchical models have used the AIC (Akaike, 1974) as a measure of goodness-of-fit (e.g., Ashby, Maddox & Bohil, 2002). For repeated measures data such as in our experiments, however, the AIC is generally found to ‘underpunish’ the addition of free parameters. In addition, any measure of goodness of fit is noisy, so if the difference in model performance is small, one should be cautious in selecting the ‘winning’ model. We therefore based the between model class comparisons not only on goodness-of-fit and number of free parameters, but also on the extent to which each of the models were able to replicate global trends in the data.

All models were fitted to experimental data using a general-purpose nonlinear minimization technique. Parameter values were found which minimized the deviance G^2 . Separate model fits were made for the formant frequency data (Experiments 1 and 2) and the duration data (Experiments 3 and 4). Given a stimulus dimension (frequency or duration), we used the simplifying assumption that a single set of parameters applied to all participants. Alternatively, one may assume that participants’ parameter values were sampled from a distribution, whose mean and spread is constant across conditions. Even if one would know the appropriate distribution (which we don’t) this assumption would make the model fitting procedure much more complex and it would probably lead to the same conclusions. Therefore, a single fit was made of each model to all data for each stimulus dimension, i.e., the data of all

72 participants in all 6 conditions.

Results

Addition of perceptual noise to the Prototype model did not significantly improve the fit for either stimulus dimension. The fit for the Distribution model, on the other hand, improved with the addition of both sensory and context noise for formant frequency as well as duration. Removing either sensory or context noise from the Decision-Bound model always significantly worsened the fit.

Table 4 presents the details of the analysis results. We included the results of the Distribution theory without perceptual noise in the Table to allow for comparison of the three standard models. The last row labeled 'NENA' refers to a new model defined in the next section. First of all, the results confirm that of the three models we tested, the Prototype theory provides the worst account of the data. Both for the formant frequency and the duration continua, the Prototype model gives the worst fit, with G^2 values that are much larger than those for the other two models.

Compared to the standard version of the Distribution model, the Decision-Bound model gives the best fit for both stimulus dimensions. This result is interesting because the experimental results of Experiment 3 suggested that listeners used a Distribution-based categorization method for the duration dimension. The present model analyses show that, although the duration data show a significant qualitative pattern in accordance with the Distribution theory, the Decision-Bound theory still provides the best quantitative account of the results (although the difference is small and possibly not meaningful). However, when the Distribution model is augmented to allow for perceptual noise, its fit improves significantly for both stimulus dimensions. For the formant data, G^2 is reduced by 11%. Despite this reduction, the augmented Distribution model still does worse than the Decision-Bound model. For the

duration data, on the other hand, G^2 is reduced by 13%, and the resulting fit is better than that of the Decision-Bound model.

Recall that Eq. 3 expressed the decomposition of the total variance of the perceptual noise into two components: sensory variance (β^2) and context variance (H^2W^2). The fourth row of Table 4 gives the values of β in the Decision-Bound models for the two stimulus dimensions, expressed in psychophysical units (ERB and d, respectively). If we convert these into number of stimulus steps (on the continua of conditions one through four), we find that the β for the formant-frequency and duration dimensions are 1.2 and 1.1 stimulus steps, respectively. The similarity of the two values shows that the step sizes we used for the continua on the two stimulus dimensions were well-chosen, because the discriminabilities of successive steps on the two continua are comparable.

For the manipulation of experiment 2 to yield a positive prediction for the decision-bound models, sensory variance needed to be non-negligible. Using the estimated parameter values we can check whether the test continuum widths were chosen appropriately. The values of the coefficient H for formant frequency and duration are .21 and .19, respectively. From these values and the values for β we estimate the ratio of the standard deviations of context and sensory noise at 1.8 for the formant-frequency dimension and 1.7 for the duration dimension. On the one hand, these values show that sensory variance and context variance were in the same order of magnitude for both stimulus dimensions and it was reasonable to expect a measurable difference in categorization-function slopes for conditions 5 and 6. On the other hand, because the contribution of context noise is bigger than that of sensory noise, the slope difference would not be expected to be very large.

We now turn to the parameter estimates for the augmented Distribution models. For both stimulus dimensions the power parameter k equals roughly 2. This would indicate that similarity does not decay proportionally to the category likelihood, but faster, namely

proportionally to the squared likelihood. If we compare the parameters coding the perceptual noise in the Distribution models and the Decision-Bound models, we find that the sensory noise (parameter β) is roughly equal in the two models, whereas the context noise (H) is smaller in the Distribution models than in the Decision-Bound models (ratio of 0.5 for formant frequency and 0.3 for duration).

These parameter values can be interpreted as follows. A power parameter k of 1 is compatible with a similarity function proportional to the category likelihood, followed by a response selection process governed by Luce choice rule (Luce, 1963). On the other hand, if k would approach infinity, the simple Distribution model would become a noise-free Decision-Bound model, because the ratio of the similarities to the two categories would be either zero or infinity (e.g., Ashby & Maddox, 1993). Analogously, the augmented Distribution model with infinite k would become a standard (i.e., noisy) Decision-Bound model, and would be governed by perceptual noise and deterministic response selection. (Note, however, that a very large value of k leads to similarity values close to zero for all categories. Although such values are of course mathematically possible, they are conceptually incompatible with one of the core assumptions of the Distribution model, which is the similarity calculation.) The parameter values show that, at least for the duration data, the truth lies somewhere in the middle. Sensory noise is roughly equal in the Decision-Bound models and the augmented Distribution models. k in the augmented Distribution models is larger than 1, so the models approach the Decision-Bound models somewhat. Thus, our model analyses suggest that the categorization mechanism employed by our listeners has aspects of both Distribution and Decision-Bound theories.

Figure 11 presents the mean slopes of the observed and modeled categorization functions across all six conditions of both stimulus dimensions. The solid lines give the slopes of the categorization functions derived from the experimental data. The vertical line segments

indicate plus or minus one standard error. The dashed and dotted lines represent the slopes expected by the Decision-Bound and augmented Distribution models and a third model to be discussed later. (Note that the models were optimized to fit the raw data, not the slope values.)

Figure 11 first of all reconfirms that the observed mean categorization-function slopes for the two stimulus dimensions are of the same order of magnitude. This tallies with our earlier finding that the best-fitting perceptual-noise variance was of similar size for the two stimulus dimensions.

Second, the figure provides us with extra means of evaluating the goodness of fit of the theories to the data, this time not the raw data but the slopes. We first focus on the formant-frequency data (panel A). There are two ways in which we can judge the fit: first we can simply examine how close the expected slopes are to the experimental ones. If we judge a model fit to be satisfactory when it falls within plus or minus two standard errors of the data, we find that neither theory on its own gives a satisfactory account of the data for either stimulus dimension. The Decision-Bound theory, which provided the best fit to the raw data, only matches the observed slopes for conditions 5 and 6. The augmented Distribution theory matches the observed slopes in conditions 2, 4, 5, and 6, but deviates very strongly in conditions 1 and 3. Second, we can judge how well each of the models replicates the overall slope patterns. For formant frequency, the overall pattern is that slopes are equal across all conditions except condition 5 for which the slope is smaller. This pattern is replicated more closely by the Decision-Bound theory than by the augmented Distribution theory.

For duration, the Decision-Bound theory matches the observed slopes in conditions 1, 3, 5, and 6, whereas the augmented Distribution theory matches the observed slopes in conditions 2, 4, 5 and 6. Here, however, the replication of the overall slope pattern plays a decisive role in the evaluation. The Decision-Bound model does not, and cannot replicate the overall slope pattern, where the slope in condition 2 is steeper than in condition 3. The augmented

Distribution theory does replicate the overall pattern, although the variation in the experimental slopes is stronger than in the actual data.

NENA: A new model of categorization

Figure 11 shows that neither model fits the overall slope patterns. Even the augmented Distribution theory, which includes a power parameter for flexibility in the decay of similarity and incorporates both types of noise of the Decision-Bound theory, does not provide a satisfactory account of the categorization-function slopes across the two stimulus dimensions. Below, we propose a new model of categorization that may explain the present results more fully. First, however, we reexamine our results in terms of the necessary components of any categorization theory, i.e., stimulus encoding, category representation and response selection.

Concerning stimulus encoding, i.e., the manner in which the stimulus is mapped on to a point in perceptual space, our model analyses give strong support for an important role of perceptual noise. The decision-bound theory, in which perceptual noise plays a pivotal role, gave a superior account of the frequency data. Furthermore, the fits of the Distribution model improved considerably for both stimulus dimensions when perceptual noise was added to the model. Note that, in the context of exemplar models, noisy stimulus encoding has been proposed for confusable one-dimensional stimuli (e.g., Ennis, 1988).

Concerning category representation the results speak equally clearly. As both the distribution and the decision-bound theories support category representation in the form of distributions, our results give strong support for the distribution representation. Listeners do not just store the mean or best representative of a set of category members, they also include information on the spread of the category in their representation. We reiterate that the present research cannot decide on whether this distribution is parametric (e.g., Gaussian) or nonparametric (e.g., fully exemplar-based).

Concerning the decision process, our data are less clear. There is evidence of both a deterministic and a stochastic decision process. A potential approach to modeling such a mixture of processes is criterial noise. Ashby and Maddox (1993) discuss how criterial noise, i.e., noise in the location of the decision bound, may be incorporated into decision-bound models. We assumed that, if a decision-bound model with criterial noise would apply, listeners would search during training for a boundary position which optimizes their percent-correct rate. If the percent-correct rate (which is determined by the likelihood ratio of the two training distributions) changes rapidly with the boundary estimate, listeners will quickly approach an accurate boundary location, whereas if the percent-correct rate would be relatively insensitive to the boundary estimate, it would take listeners long to find an accurate boundary location. We therefore thought it reasonable to assume that the standard deviation σ_B of the criterial noise would be inversely proportional to the change of the percent correct rate P_c during training with changing boundary location B :

$$\sigma_B \sim \frac{dB}{dP_c} \quad (5)$$

The proportions of $\frac{dP_c}{dB}$ for conditions one through four were 4:2:2:1, respectively. This means that the proportions of the standard deviations of the criterial noise would be 1:2:2:4, respectively. Thus, if listeners used a decision-bound mechanism in which criterial noise played a significant role, the pattern of categorization-function slopes would be steep-intermediate-intermediate-shallow for conditions 1 through 4, respectively, i.e., the opposite of the prototype pattern. This prediction only makes the decision-bound model move away from the observed slope pattern. Therefore, the addition of criterial noise to the decision-bound model cannot explain the observed results either.

On the basis of the above considerations we constructed a new hybrid model with the

following properties. Concerning category representation, we assume that categories are represented by distributions. These distributions are learned through previous exposure, as in the training phase of our experiments. The distributions are either parametric or non-parametric. For the purpose of the present study we assume they are parametric and have the form of normal distributions characterized by a mean and variance. Concerning the processing issue, we assume that the stimulus encoding is stochastic, i.e., there is perceptual noise. As in the Decision-Bound theory this noise is normal with zero mean and a variance with two components: trace variance and context variance. After stimulus encoding, the stimulus is represented as a point $\tilde{\psi}$ on a psychological axis, where the 'tilde' sign indicates that a noise component is present. Next, the stimulus is mapped onto category similarity (or "activation") values for each of the two categories in a manner similar to the Distribution model. In contrast to the Distribution model, however, this calculation is assumed to be stochastic. Mathematically, first the value of the distribution at the stimulus location is calculated. We can indicate this value as $A(\tilde{\psi})$, where A represents the category distribution or 'activation function' of the category. Next the logarithm $\log A(\tilde{\psi})$ is taken, to which normal noise with mean zero is added, resulting in a value $\widetilde{\log A(\tilde{\psi})}$. Next, the exponent is calculated, resulting in the noisy activation value $\exp \widetilde{\log A(\tilde{\psi})}$, or, more compactly, $\tilde{A}(\tilde{\psi})$. We chose to add normal noise to the logarithm of the activation instead of to the 'raw' activation for two reasons. First of all, adding normal noise to $\log A$ leads to Luce choice rule, whereas adding it to A does not (Albert and Chib, 1993). Second, conceptually, adding normal noise to an activation value (or similarity) is incorrect, because it can lead to values below zero. As a final step, the category is selected which has the largest activation value. The latter choice process is deterministic. We call the hybrid model NENA, short for Noisy Encoding Noisy Activation, reflecting the essential components of the model.

The NENA model is a true hybrid. On the one hand, it contains perceptual noise and

deterministic choice, like the decision-bound model. On the other hand, an essential step in the model is a category-activation calculation, comparing the incoming stimulus to the distribution of training stimuli, as in the distribution model. As such, the decision bound does not play an explicit role in the categorization process. If the noise in the activation calculation (henceforth “activation noise”) is zero, the model is a standard decision-bound model. If the perceptual noise is zero, and the shape of the activation noise is such that it leads to a response behavior which is mathematically equivalent to Luce choice rule, the model is equivalent to the distribution model. By varying the amounts of perceptual and activation noise, it should be possible to obtain satisfactory fits to the data for both dimensions using a single model.

The NENA model has three free parameters: β and H coding sensory and context noise, respectively, and α representing the standard deviation of the activation noise, i.e., the Gaussian noise added to the logarithm of the category similarities. Unfortunately, analytical solutions linking stimulus values to response probabilities do not exist, so we had to resort to Monte Carlo techniques to fit the hybrid model to our data. To obtain reliable model estimations, we generated 300,000 random values for each stimulus in each of the 6 conditions and then used a minimization procedure to find the parameter values that produced the lowest value of G^2 .

For formant frequency the best-fitting model had a G^2 equal to 1630. This value is very close to that of the Decision-Bound Theory (1631) obtained earlier. Apparently, “adding” a Distribution Theory component to the model has not resulted in an improvement in goodness of fit. The similarity of the two models is further corroborated by the fact that the best-fitting values of β and H of the hybrid model are identical to those for the Decision-Bound Theory (1.2 stimulus steps and 0.21, respectively, see Table 4). The value of α is 0.010, i.e., almost zero. Thus, the hybrid model does not account for the slight Distribution Theory-like trend in the slope data discussed earlier.

The best-fitting NENA model for duration has $G^2 = 1431$. The fit is therefore somewhat worse than that of the augmented Distribution model (1373), but better than that of the Decision-Bound model. The best-fitting values of the model parameters are $\beta = 1.1$, $H = 0.13$, and $\alpha = 0.62$. If we compare these to the values for the Decision-Bound model ($\beta = 1.1$, $H = 0.19$), we see that the context noise parameter has decreased. Effectively, the NENA model assigns a significant portion of the total noise in the process to the similarity calculation, leaving less for the perceptual encoding. This tallies with the finding that α is larger for duration than for formant frequency (0.62 versus 0.01, respectively). Finally, we note that the summed G^2 for the two dimensions is smaller for the NENA model (3060) than for both the Decision-Bound Theory (3167) and the augmented Distribution theory (3257), although the advantage is small.

The dash-dotted line in Figure 11 gives the categorization function slopes of the NENA model. For formant frequency, the slope values predicted by the NENA model are not noticeably different from those predicted by the Decision-Bound Theory. For duration, on the other hand, the NENA model predicts slope values which truly combine aspects of the Distribution Theory and Decision-Bound Theory. The pattern of slope values exhibits both the (weakened) Distribution Theory-like pattern for conditions 1 to 4, and the context-noise effects for conditions 5 and 6.

In sum, we have formulated a hybrid model of categorization which gives a reasonable account of our experimental results for both the formant-frequency and the duration dimensions through a combination of aspects of the decision-bound and distribution theories of categorization. We do note, however, that some discrepancies between data and model predictions remain.

The present study addressed the question how listeners categorize sounds. In four experiments we trained listeners to categorize synthetic sounds from two overlapping distributions. Subsequently, listeners categorized stimuli from a test continuum without receiving feedback. The crucial manipulations in the experiments were variation of the variance and overlap of the two distributions as well as the width of the test continuum. Prototype, Distribution and Decision-Bound theories of categorization made different predictions about the slopes of the categorization functions in the various conditions.

When we applied the methodology to the formant frequency dimension, we found a pattern of slopes that was in reasonable agreement with the Decision-Bound theory. When we subsequently applied the exact same methodology to a duration dimension, however, the results were in partial correspondence with both the Decision-Bound and Distribution theories. Subsequent model-based analyses confirmed the discrepancy between the two dimensions: for the formant-frequency dimension the Decision-Bound model gave the best quantitative account of the data, whereas the Distribution model fitted the duration data best. NENA, a new, hybrid model of categorization, was formulated which combines stochastic stimulus encoding with stochastic category activation. The new model gave a better combined account of the data across the two stimulus dimensions than any of the other models, although some discrepancies between model and data persisted.

In our discussion of the experimental data we asked the question why different categorization mechanisms seem to operate for the two stimulus dimensions. At present we cannot provide an explanation for this difference. There is, however, a theoretical perspective which may guide future research into this matter. S. S. Stevens and colleagues introduced the concepts of *prothetic* and *metathetic* scales (e.g., Stevens & Galanter, 1957). A prothetic scale is a psychological scale to which, at a physiological level, an "additive" mechanism applies, i.e., increasing a value on a prothetic scale is equivalent to adding more of the same. Examples

of prothetic scales are brightness, loudness and, in the present study, duration. A longer sound simply has "more duration" than a shorter sound, and is presumably encoded at a physiological level by a stronger or longer firing of basically the same neurons. In contrast, a "substitutive" mechanism applies for metathetic scales such as (visual) position and pitch, and presumably timbre-like magnitudes like formant frequency. A pure tone with a higher pitch does not simply have "more frequency" than one of a lower pitch. Instead, it essentially stimulates different fibers in the auditory nerve. Empirically, the difference between the two scales is evidenced by the fact that for metathetic scales the jnd measured in subjective units is constant across the scale (e.g., the jnd for pitch expressed in mels is the same for low and high tones), whereas the same does not hold for prothetic scales (the jnd for loudness expressed in sones is smaller at the low end of the scale than at the high end).

We hypothesize that either the storage of category representations, or the comparison of a stimulus to a category is noisier for prothetic categories such as duration than for metathetic categories such as formant frequency. According to this hypothesis, other prothetic auditory dimensions, such as loudness, should pattern with duration on a similar categorization task, whereas metathetic dimensions, such as pitch or dynamic timbre (formant transitions), should pattern with formant frequency. This is a topic for future research.

Finally, we return to the ultimate purpose of this research, which is to learn about the representations and processes underlying speech perception. As mentioned in the introduction, four theories of phonetic categorization can be distinguished: Decision-Bound, Prototype, Distribution, and Exemplar theories. Although they make fundamentally different claims about various aspects of categorization, it has proved extremely difficult to experimentally distinguish between the four alternatives. We know of only two studies which explicitly attempt to do so within the context of phonetic perception. Samuel (1982) contrasted the Decision-Bound and Prototype accounts of phonetic categorization using selective adaptation

in a /ga/-/ka/ categorization task. The experimental results showed that more adaptation was obtained using adaptors near the /ga/ prototype than for adaptors nearer to or further away from the /ga/-/ka/ boundary. Samuel (1982) interpreted this as evidence in support of a Prototype theory of phonetic categorization. The study was not conclusive, however. First, the evidence is not only in agreement with a Prototype theory, but also with Distribution and Exemplar theories, which, being less topical at the time, were not explicitly tested. Furthermore, because the adaptation paradigm itself is not well understood and subject of dispute (see Remez, 1987), the evidence should be considered as relatively indirect.

A second study which explicitly contrasted theories of phonetic categorization was published by Nearey & Hogan (1986), who reanalyzed a set of production and perception data for the three-way voicing contrast in Thai stop consonants collected by Lisker & Abramson (1970). Lisker & Abramson measured Voice-Onset Time (VOT) on a set of naturally produced instances of the three voicing categories. Next, they constructed a synthetic stimulus continuum varying in VOT and asked listeners to categorize the stimuli according to voicing. Lisker and Ambramson noted the striking similarity of the cross-over points in the production and perception data. Hoping to be able to use the data to distinguish between competing categorization theories, Nearey & Hogan (1986) fitted two formal categorization models to the data. The first was a Decision-Bound model which assumed noisy stimulus encoding and boundary locations which were (near) optimal given the production data. The second was a Distribution-based model which assumed that the incoming stimulus was compared to the categories represented by the probability-density functions (pdfs) of the production data, followed by a choice based on Luce choice rule (Luce, 1963). Both models fit the data well, and the difference in goodness-of-fit was too small to warrant selection of one over the other. At present, it remains undecided which of the four categorization theories applies to phonetic categorization.

Although our study is intended as a first step towards solving this issue, we have to be cautious about generalizing our results to phonetic categorization. Many differences between our stimuli and those in phoneme categorization can be identified. Specifically, our stimuli consisted of non-speech signals designed to resemble speech in crucial regards (duration and formant frequency). Recent research inspired by the current study sheds some light on these issues. Using training and testing protocols very similar to those in our study, Goudbeek, Smits, Swingley, & Cutler (accepted) directly compared the acquisition of auditory and phonetic categories by adults. In the non-speech condition, Dutch listeners categorized stimuli that simultaneously varied in duration and resonant frequency. In the speech condition, American listeners categorized stimuli that consisted of variants around the midpoints of three Dutch high front vowels that do not occur in English, and that differ in duration and/or frequency of the first formant. In terms of the speed of learning and the proportion of subjects that eventually learned to do the task, the results for the non-speech and speech stimuli were highly similar, indicating that findings based on non-speech stimuli generalize to speech, at least within the experimental context used in these studies. This is of interest given the ongoing debate in the phonetic literature about the extent to which the perception of speech engages general auditory mechanisms or mechanisms that specifically evolved for the processing of speech (e.g., Liberman & Mattingley, 1985; Remez et al., 1994). The finding that the current methodology obtains the same results for speech and non-speech justifies its use as a valid means of studying phonemic categorization.

A final consideration when using multidimensional stimuli involves the acoustic variability that is a hallmark of natural speech. When using stimuli that more closely mimic the degree of variability found in speech (for example, variation in speaker, phonetic context, and speaking rate), the variability itself may affect the categorization mechanisms employed. Recently, a number of exemplar models of speech perception have been proposed (Goldinger,

1997; Johnson, 1997a, b). Rather than conceptualizing speech perception as a process wherein a more abstract representation is created from the myriad of highly variable and idiosyncratic tokens, some contemporary theories have emphasized the retention of detailed voice information in episodic representations. Goldinger and colleagues (Goldinger, 1997, 1998; Goldinger and Azura, 2004; Goldinger, Azura, Kleider, and Holmes, 2003) provide evidence for the existence of detailed episodic memory traces of spoken words in lexical access processes. An examination of speakers' recognition accuracy and listeners' imitation judgments show sensitivity to previously encountered instances. Indexical aspects of speech are stored in memory and can be used later in perception and production. In a similar vein, Johnson (1997) presents an exemplar-based model for vowel identification, taking into account aspects of talker variability that affect human vowel perception performance. Five acoustic parameters (F0, F1-F3, and vowel duration) were used as input to the model. The model's overall correct vowel identification was 80% human listeners' ability to identify vowels (Ryalls and Lieberman, 1982). Variability in speech that distinguishes speakers is retained in the set of exemplars. Both sets of data suggest that categorization takes place by reference to detailed auditory exemplars that preserve speaker-specific information, data most compatible with exemplar or distribution theories.

It is at this point difficult to predict to what extent the results of the present study will generalize to the categorization of multi-dimensional speech sounds. This constitutes an topic for future research. We will therefore merely use our results to formulate a number of hypotheses about phoneme categorization that may be tested in future experiments employing different stimuli and tasks.

Concerning the representation issue, the present results lead us to hypothesize that speech sounds are represented neither by prototypes nor by boundaries (rules) separating the speech sounds, but instead by distributions. These distributions capture the natural variation of

speech sounds, as encountered by the listener. Of course, speech sounds being acoustically multidimensional, these distributions will be multidimensional too, in contrast to the unidimensional distributions of our experiments. On the basis of our results we cannot decide whether the distributions are parametric, i.e., economical summary descriptions, perhaps in the form of Gaussian probability-density functions, or non-parametric, perhaps in the form of multiple exemplars of previously heard sounds.

Concerning the processing issue, our results led us to propose a new model combining aspects of the Decision-Bound and Distribution models. In this model, the stimulus encoding is stochastic, as in the Decision-Bound model. Next a similarity calculation is made, as in the Distribution model, albeit stochastic. Finally, a deterministic choice is made, as in the Decision-Bound model. However, as the choice was based on a comparison of (noisy) activation levels, a Decision-Bound as such did not play an explicit role in the choice process. We hypothesize that the phoneme categorization process has these same three components. Although the deterministic decision process is particular to the phoneme-categorization task and need not operate in the process of recognizing words or larger units, we hypothesize that the other two components are also active in the everyday recognition of running speech.

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Appendix A

Derivation of predictions of basic models

Prototype theory

Assuming Gaussian similarity functions (e.g., Nosofsky, 1986), the probability $p(A|S_i)$ of assigning stimulus S_i , defined by parameter value ψ_i , to category A is given by

$$p(A|S_i) = \frac{\eta_A(\psi_i)}{\eta_A(\psi_i) + \eta_B(\psi_i)} \quad (6)$$

$$= \frac{\exp -k(\psi_i - \mu_A)^2}{\exp -k(\psi_i - \mu_A)^2 + \exp -k(\psi_i - \mu_B)^2} \quad (7)$$

$$= \frac{1}{1 + \exp -2k(\mu_A - \mu_B)[\psi_i - \frac{1}{2}(\mu_A + \mu_B)]} \quad (8)$$

where $\eta_A(\psi_i)$ is the similarity of ψ_i to category A , and k is a sensitivity parameter (e.g., Ashby & Maddox, 1993). Of course, $p(B|S_i) = 1 - p(A|S_i)$. $p(A|S_i)$ is a logistic function of ψ_i . The function's inflection point, which corresponds to the value of ψ_i where $p(A|S_i) = \frac{1}{2}$, is located at $\psi_i = \frac{1}{2}(\mu_A + \mu_B)$, i.e. halfway between the two means. The slope s of the logistic function, defined as the absolute value of the coefficient of ψ_i in the exponent of Eq. (8), equals $2k(\mu_A - \mu_B)$. Thus the slope of the categorization function is proportional to the distance between the means of the pdfs used in the training phase. For the purpose of Figure 1 k was set to 0.25; this value was chosen such that the categorization functions were comparable to those for the other theories.

Distribution theory

The similarity $\eta_A(\psi_i)$ of a given stimulus S_i to category A is assumed to be equal to the “unnormalized” likelihood $p(\psi_i|A)$ that the stimulus was produced by the particular category:

$$\eta_A(\psi_i) = p(\psi|A) \cdot \sigma\sqrt{2\pi} \quad (9)$$

$$= \exp -\frac{k}{2\sigma^2}(\psi_i - \mu_A)^2 \quad (10)$$

where k is a sensitivity parameter. The term “unnormalized” refers to the assumption that self-similarity equals unity, i.e., $\eta_A(\mu_A) = 1$, which has the effect that the similarity function is generally not a probability density function because its integral differs from one.

Finally it is assumed that response probabilities are calculated from similarity functions via Luce’s choice rule. This leads to the following expression for $p(A|S_i)$:

$$p(A|S_i) = \frac{\eta_A(\psi_i)}{\eta_A(\psi_i) + \eta_B(\psi_i)} \quad (11)$$

$$= \frac{\exp -\frac{k}{2\sigma^2}(\psi_i - \mu_A)^2}{\exp -\frac{k}{2\sigma^2}(\psi_i - \mu_A)^2 + \exp -\frac{k}{2\sigma^2}(\psi_i - \mu_B)^2} \quad (12)$$

$$= \frac{1}{1 + \exp -\frac{k(\mu_A - \mu_B)}{\sigma^2}[\psi_i - \frac{1}{2}(\mu_A + \mu_B)]} \quad (13)$$

As was the case for the Prototype theory, $p(A|S_i)$ is a logistic function of ψ_i with inflection point at $\frac{1}{2}(\mu_A + \mu_B)$. The categorization function’s slope s is now equal to $\frac{k}{\sigma^2}(\mu_A - \mu_B)$, i.e., it is proportional to the distance between the means of the training pdfs divided by their variance. For the purpose of Figure 1 the value of k was set to 1.

Appendix B

Discrimination of test continua

Method

Participants. Eight students at Nijmegen University were recruited as participants. All reported normal hearing and had Dutch as their native language. None participated in the categorization experiments reported in the main article.

Stimuli. Stimulus numbers 1, 3, 5, 7, 9 and 11 of the formant frequency and duration continua were used. We did not use all stimuli to limit the size of the experiment.

Procedure. We adopted a same-different (AX) paradigm. On a given trial two stimuli were played after each other with a inter-stimulus interval of 300 ms. The two stimuli were either the same, or different, in which case they were two steps apart on the stimulus continuum (e.g., stimulus 3 and 5). Participants were seated in a soundproof booth in front of a computer screen. Stimuli were presented binaurally through Sennheiser headphones. After hearing a pair of stimuli, participants were required to indicate whether they thought the stimuli were the same or different by pressing one of two appropriately labeled buttons. After the button press, the correct answer was displayed briefly on the screen, and a new trial was initiated.

The experiment consisted of two parts: a subexperiment testing formant-frequency discrimination and one testing duration discrimination. Half the subjects started with formant-frequency discrimination, the other half with duration discrimination. After twenty practice trials subjects were presented with five blocks of 40 trials each. Every 'different' pair was presented four times in each block, twice in ascending order (e.g., 3-5) and twice in descending order (5-3). The 'same' pairs (e.g., 3-3) were each presented four times per block, except for the pairs 1-1 and 11-11, which were presented twice per block. Thus, the probabilities of being presented with a same or different pair were equal. Within blocks,

stimuli were pseudo-randomized, with different randomizations for different participants.

After the five experimental blocks, participants had a short break, in which it was explained to them that they were to do the experiment again, but this time the sounds would differ from each other in another way. They then started on the second subexperiment in which the stimuli varied along the other stimulus dimension. The procedure of the second subexperiment was identical to that of the first, including the practice trials.

Results

For unknown reasons, one of the participants performed below chance level on the duration stimuli and above chance, but still worse than the other seven participants for the formant frequency stimuli. This participant's data were removed. Using Table A5.4 (differencing model) of Macmillan and Creelman (1991), d' values were calculated for each stimulus pair for each participant. Figure A.1 presents means and standard deviations of d' for the two stimulus continua.

The results of the discrimination experiment tell us, first of all, that the stimuli of both continua were moderately confusable. Average d' s for a two-step distance along the formant-frequency and duration continua were 1.9 and 1.5, respectively. Assuming that d' s are additive along a one-dimensional continuum, average d' for the discrimination of two consecutive stimuli are 1.0 and 0.8 for the formant frequency and duration continua, respectively, i.e., two consecutive stimuli are on the border of being discriminable. Average d' s for the discrimination of the endpoint stimuli were 9.7 and 7.7, respectively, i.e., endpoint stimuli were highly discriminable.

We ran an Anova with dependent variable d' , pair number and stimulus dimension as fixed factors, and subject as random factor. Stimulus dimension did not prove significant ($F(1, 6) = 3.3$, n.s., $MSE = .841$), which means that average d' s were the same for the

formant frequency and duration continua. Pair number also did not reach significance ($F(4, 24) = 1.9$, n.s., $MSE = .621$), meaning that d' was constant across pairs. Of the possible interaction terms, only pair number by stimulus dimension reached significance ($F(4, 24) = 3.2$, $p < .05$, $MSE = .461$, $\eta^2 = .35$). Individual T-tests for the difference in discriminability between formant frequency and duration for each of the stimulus pairs showed that the interaction was due to stimulus pair 7-9, which was the only pair for which d' was significantly different for the two dimensions ($t(6) = -3.6$, $p < .02$).

In addition to the Anova, we ran separate linear regressions for the formant-frequency and duration data with d' as the dependent variable and pair number as the independent variable. For neither dimension did the factor pair number reach significance. This shows that there is no linear trend in d' , giving further support for the constancy of discriminability of both continua.

From the discrimination experiments we draw the following conclusions. First, the two stimulus continua we used in our categorization experiments were of equal discriminability. Both cover the same number of just-noticeable differences. Second, consecutive stimuli are confusable, whereas continuum endpoints are highly discriminable. Finally, discriminability is almost constant across both continua, which means that stimuli on both continua are almost equidistant in the perceptual sense. The only exception to this rule is stimulus pair 7-9 in the formant-frequency series, which is slightly more discriminable than the other pairs.

Author notes

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Table 1: Training distributions of Experiment 1. Columns 2 and 3 give the distances $\Delta\mu$ between the means of the two training pdfs and their standard deviations σ expressed in the number of jnds. Column 4 gives the theoretically maximum classification rates (“max rate”) of an optimal, noise-free classifier, for training conditions 1 to 4. Columns 5, 6, and 7 give the predicted ratios of the categorization function slopes in the four conditions for the Prototype, Distribution, and Decision-Bound-based categorization theories.

Condition	$\Delta\mu$	σ	max rate	slope ratios		
	(jnds)	(jnds)	(%)	Prototype	Distribution	decision bound
1	5	3.704	75.45	1	2	1
2	10	3.704	91.82	2	4	1
3	10	7.407	75.45	2	1	1
4	20	7.407	91.82	4	2	1

Table 2: Means and standard deviations of pdf_A and pdf_B in the four training conditions of Experiment 1 (formant frequency categorization). Columns 2, 3 and 4 give means and standard deviations expressed in ERB (standard deviations in column 4 hold for both pdfs), while columns 5 to 8 give means and standard deviations expressed in Hz.

Condition	$\mu_A(\text{ERB})$	$\mu_B(\text{ERB})$	$\sigma(\text{ERB})$	$\mu_A(\text{Hz})$	$\mu_B(\text{Hz})$	$\sigma_A(\text{Hz})$	$\sigma_B(\text{Hz})$
1	18.49	19.10	.44	1446	1559	78	84
2	18.19	19.40	.44	1393	1619	76	87
3	18.19	19.40	.87	1398	1625	153	174
4	17.58	20.01	.87	1295	1750	143	186

Table 3: Means and standard deviations of pdf_A and pdf_B in the four training conditions of Experiment 3 (duration categorization). Columns 2, 3 and 4 give means and standard deviations expressed in d (standard deviations in column 4 hold for both pdfs), while columns 5 to 8 give means and standard deviations expressed in ms.

Condition	$\mu_A(\text{d})$	$\mu_B(\text{d})$	$\sigma(\text{d})$	$\mu_A(\text{ms})$	$\mu_B(\text{ms})$	$\sigma_A(\text{ms})$	$\sigma_B(\text{ms})$
1	48.86	51.36	1.79	134.5	172.7	24.2	31.1
2	47.61	52.61	1.79	118.7	195.7	21.4	35.2
3	47.61	52.61	3.58	124.5	205.2	45.5	74.9
4	45.11	55.11	3.58	96.9	263.5	35.4	96.2

Table 4: Results of model analyses. Parameters k , β , and H model the similarity gradient, the standard deviation of the sensory noise, and the coefficient of the stimulus range in the context variance, respectively. SN and CN are abbreviations of sensory noise and context noise, respectively.

Model	formant frequency		duration	
	parameter values	G^2	parameter values	G^2
Prototype	$k = 1.1$	2402	$k = .076$	2029
Distribution	$k = .91$	2124	$k = 1.1$	1577
Distrib., PN	$k = 2.0, \beta = .36 \text{ ERB}, H = .10$	1884	$k = 1.9, \beta = 1.3 \text{ d}, H = .059$	1372
Dec.-Bound	$\beta = .29 \text{ ERB}, H = .21$	1631	$\beta = 1.1 \text{ d}, H = .19$	1536
NENA	$\beta = .29 \text{ ERB}, H = .21, \alpha = .010$	1630	$\beta = 1.1 \text{ d}, H = .13, \alpha = .62$	1431

Figure captions

Figure 1. Training probability-density functions and predicted categorization functions for the four experimental conditions of Experiments 1 and 3. The four panels in the left-most column represent probability density (pd) on psychological dimension ψ in conditions 1 to 4. μ_{C_i} indicates the mean of the pdf for category C in condition i . The small horizontal lines above the panels represent the width of the test continua. The panels in columns 2, 3, and 4 indicate categorization functions on testing, as predicted by the Prototype, Distribution, and Decision-Bound theories of categorization. $p_{A,B}$ is short for $p(A|S_i)$ and $P(B|S_i)$.

Figure 2. Average training performance in Experiment 1 (formant frequency categorization) as a function of training block. Different symbols and line types refer to different experimental conditions (1-4, see text). The isolated symbols to the right of block 8 indicate theoretically optimal performance.

Figure 3. Categorization functions of individual subjects in the four experimental conditions of Experiment 1 (formant frequency categorization).

Figure 4. Training probability-density functions and predicted categorization functions $p(A|S_i)$ and $P(B|S_i)$ for conditions 5 and 6 of Experiments 2 and 4. Otherwise as Figure 1.

Figure 5. Average training performance in conditions 5 and 6 of Experiment 2 (formant frequency) as a function of training block. Different symbols and line types refer to different experimental conditions (see legend). The isolated symbols to the right of block 8 indicate theoretically optimal performance.

Figure 6. Categorization functions of individual subjects in conditions 5 and 6 of Experiment 2 (formant frequency).

Figure 7. Average training performance in conditions 1 to 4 of Experiment 3 (duration) as a function of training block. Different symbols and line types refer to different experimental conditions (see legend). The isolated symbols to the right of block 8 indicate theoretically optimal performance.

Figure 8. Categorization functions of individual subjects in the four experimental conditions of Experiment 3 (duration).

Figure 9. Average training performance in conditions 5 and 6 of Experiment 4 (duration) as a function of training block. Different symbols and line types refer to different experimental conditions (see legend). The isolated symbols to the right of block 8 indicate theoretically optimal performance.

Figure 10. Categorization functions of individual subjects in conditions 5 and 6 of Experiment 4 (duration).

Figure 11. Predicted and observed mean categorization-function slopes in conditions 1 to 6 for formant frequency (panel A) and duration (panel B). Solid lines give observed slopes, with vertical bars representing ± 1 standard error. Dashed, dotted, and dash-dotted lines give theoretical slopes as predicted by the Decision-Bound theory (DBT), Distribution theory (DT), and the NENA model, respectively.

Figure A.1. Discriminability, expressed as d' , as a function of stimulus pair for the formant frequency and duration continua.

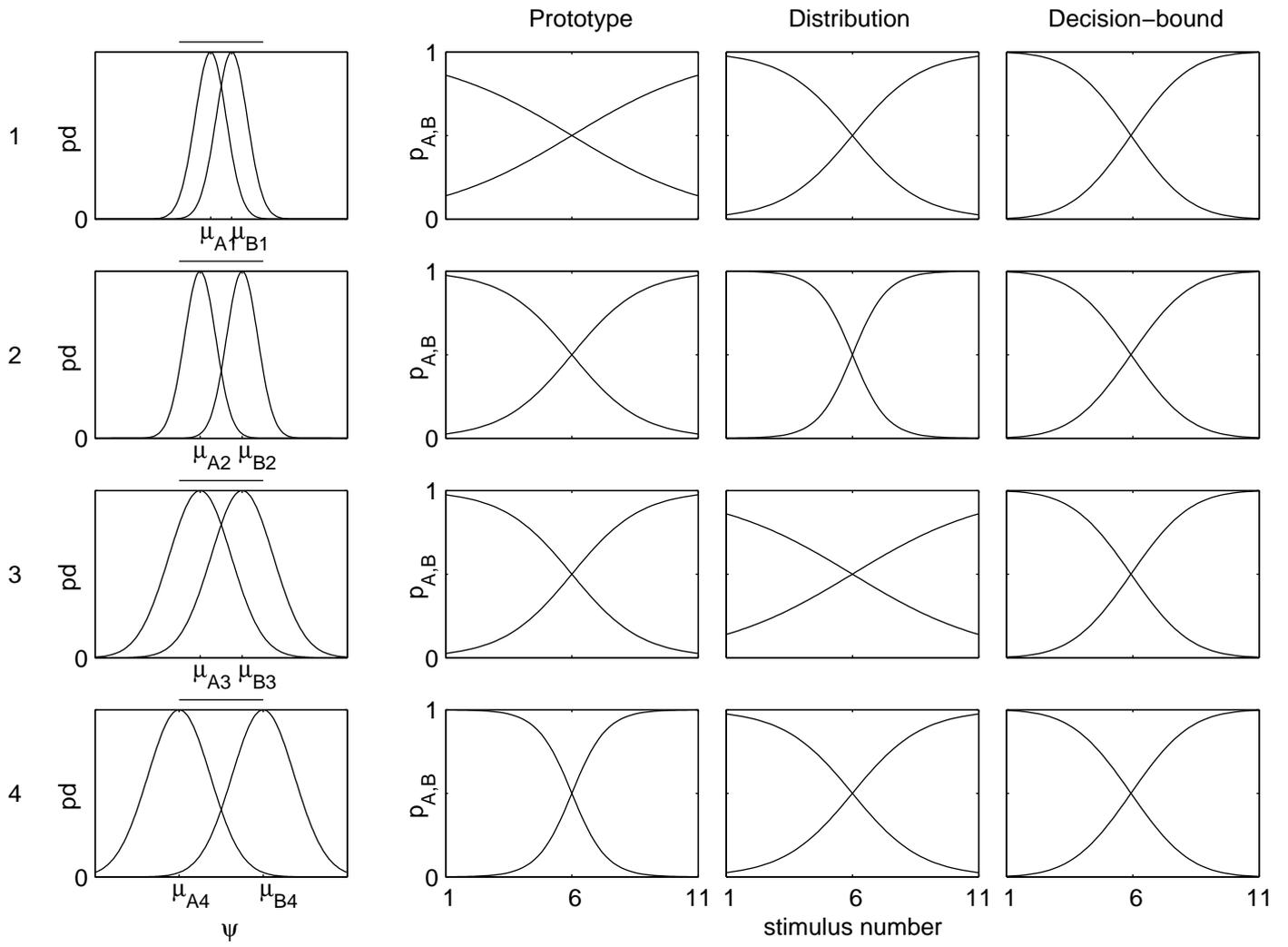


Figure 1

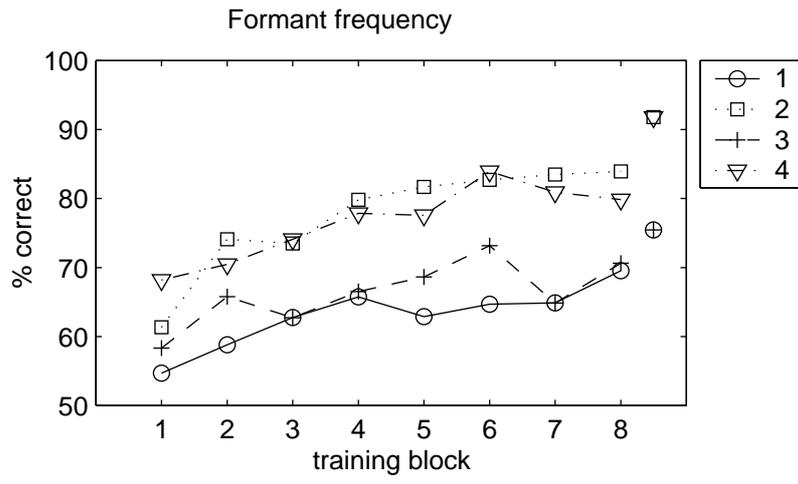


Figure 2

Formant frequency

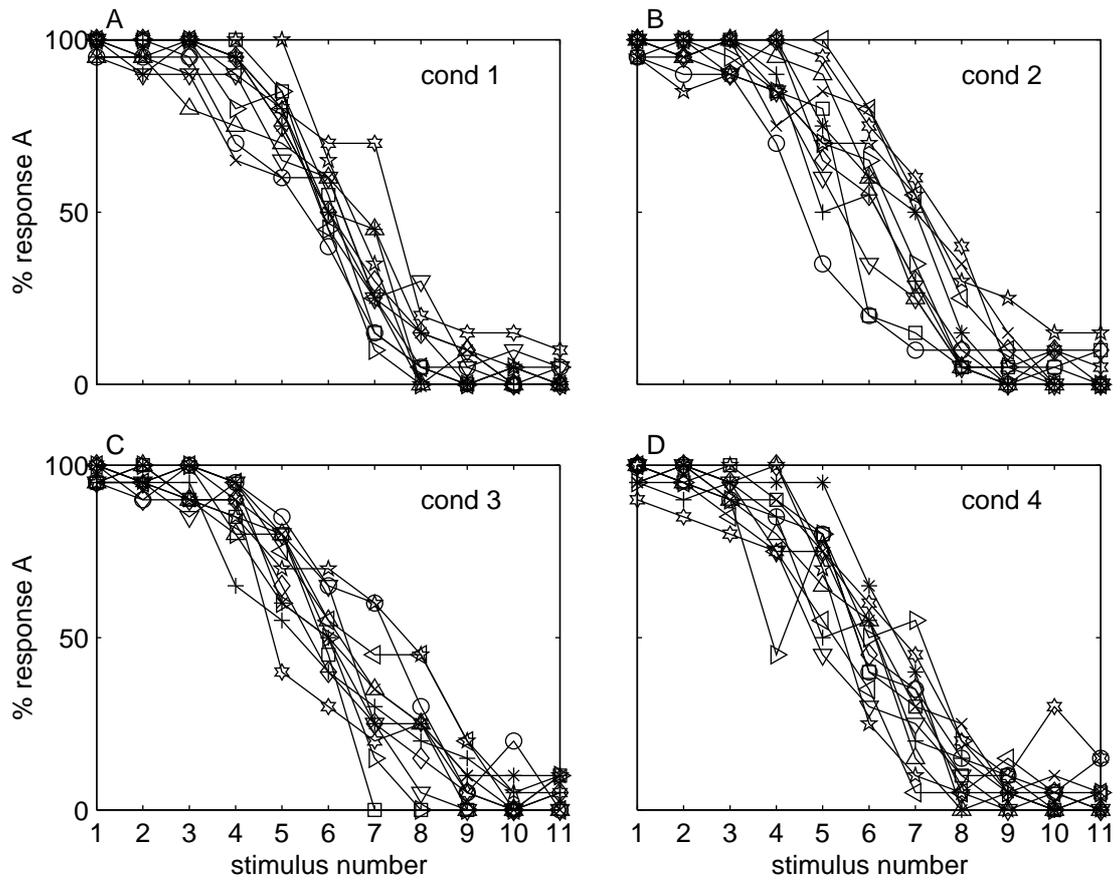


Figure 3

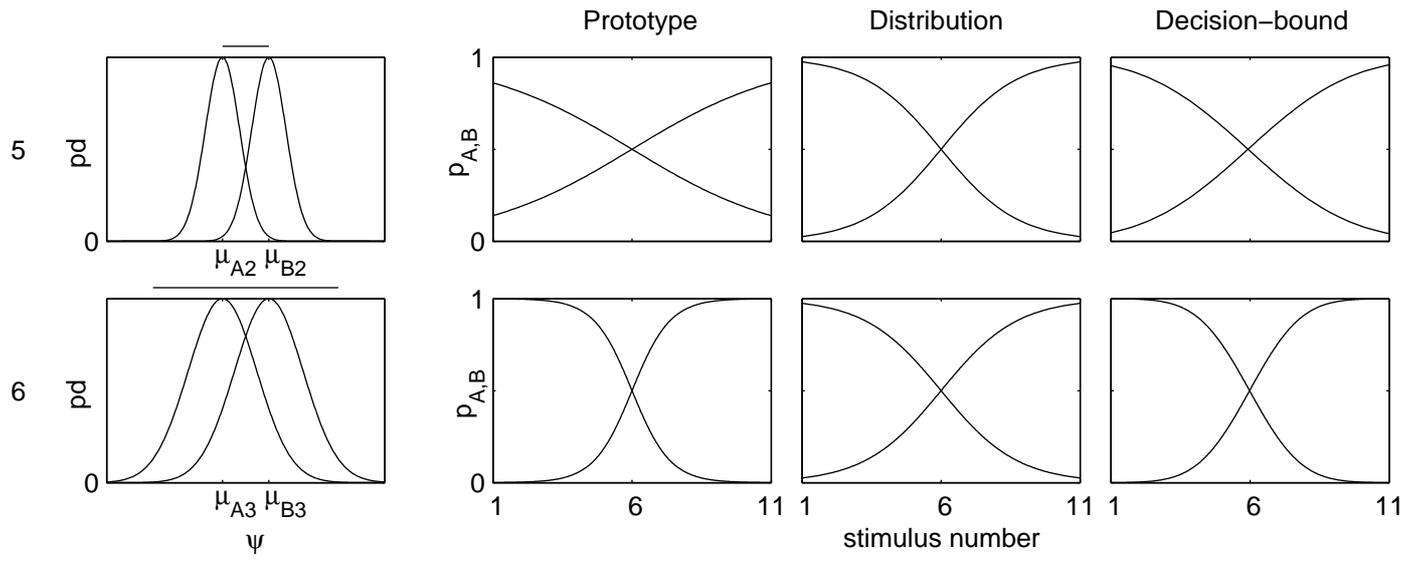


Figure 4

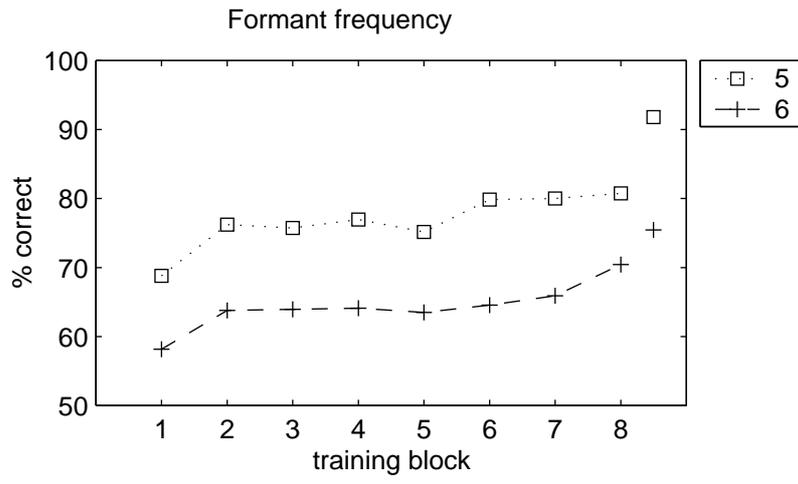


Figure 5

Formant frequency

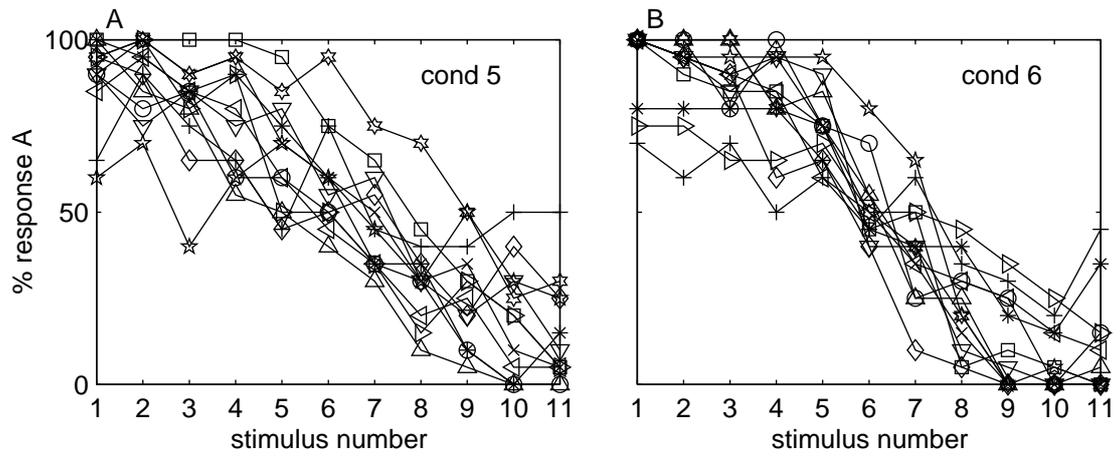


Figure 6

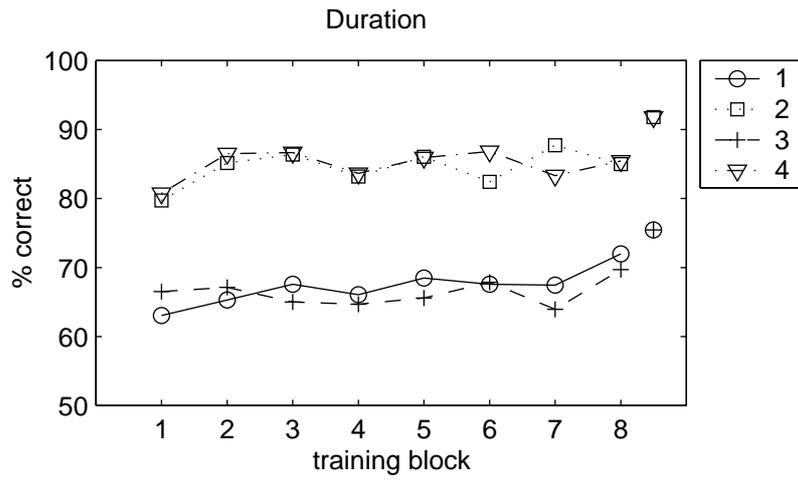


Figure 7

Duration

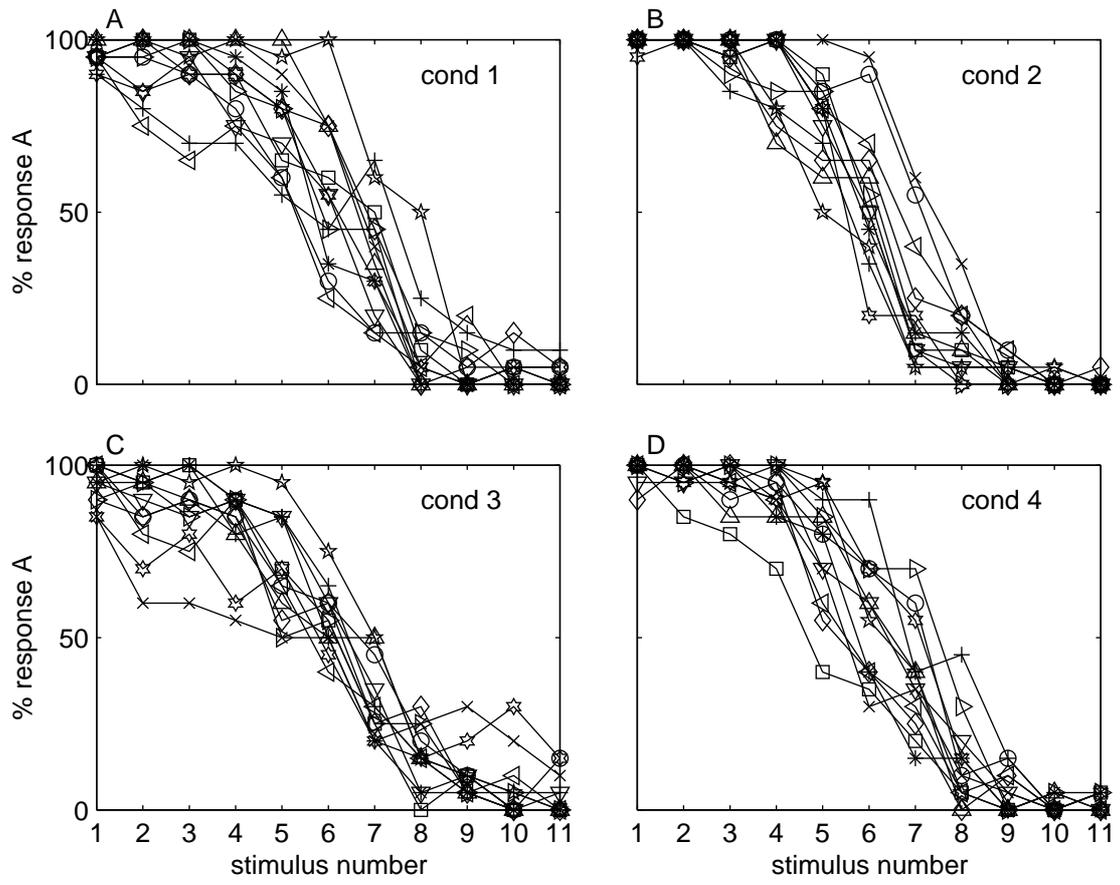


Figure 8

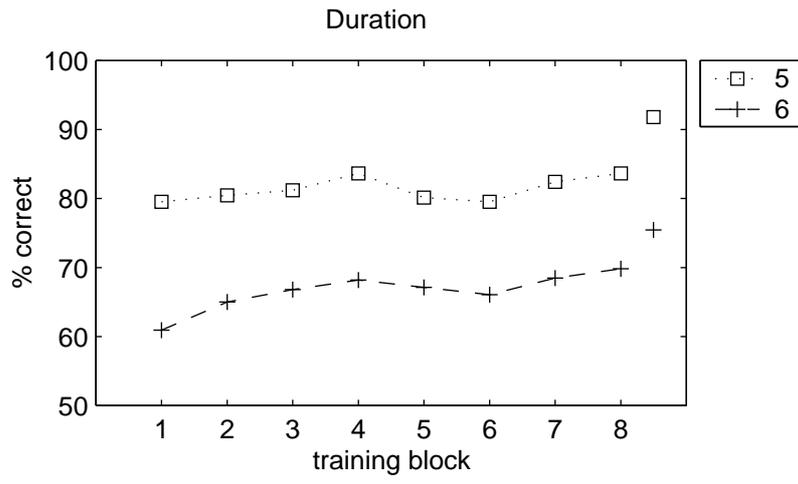


Figure 9

Duration

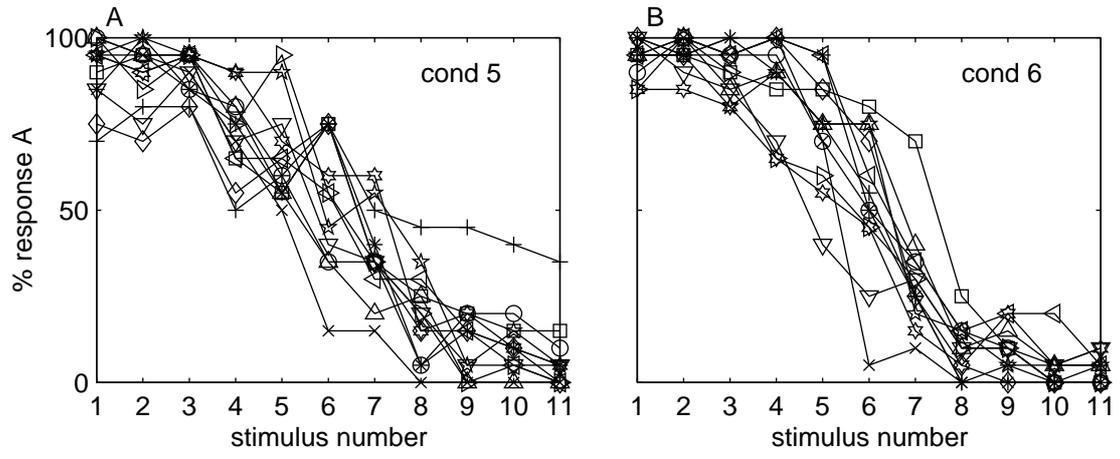


Figure 10

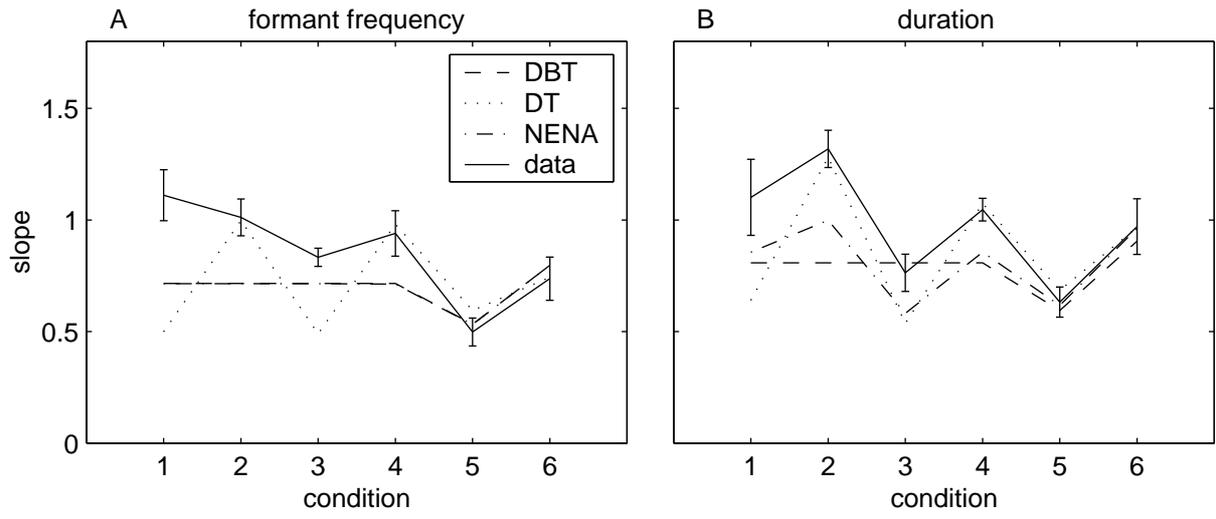


Figure 11

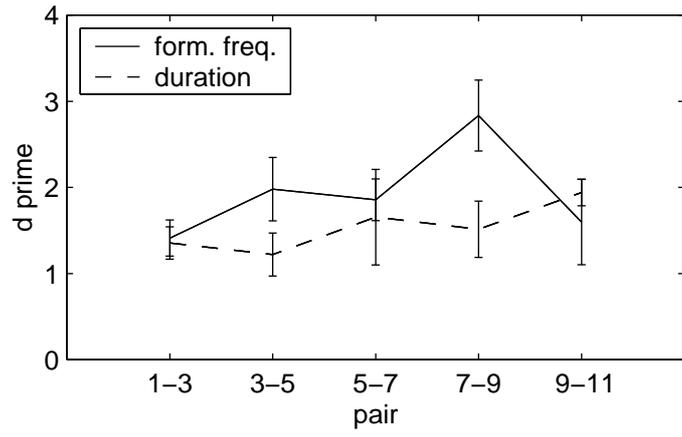


Figure A.1