Development and Implementation of a VHF High Power Amplifier for the Multi-Channel
Coherent Radar Depth Sounder/Imager System

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B.Sc. Electrical Engineering
University of Kansas, 2009

Submitted to the graduate degree program in Electrical Engineering and Computer Science and
the Graduate Faculty of the University of Kansas in partial fulfillment of the requirements for the
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Development and Implementation of a VHF High Power Amplifier for the Multi-Channel
Coherent Radar Depth Sounder/Imager System

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Date approved: 31 May 2013
Abstract

This thesis presents the implementation and characterization of a VHF high power amplifier developed for the Multi-channel Coherent Radar Depth Sounder/Imager (MCoRDS/I) system. MCoRDS/I is used to collect data on the thickness and basal topography of polar ice sheets, ice sheet margins, and fast-flowing glaciers from airborne platforms. Previous surveys have indicated that higher transmit power is needed to improve the performance of the radar, particularly when flying over challenging areas.

The VHF high power amplifier system presented here consists of a 50-W driver amplifier and a 1-kW output stage operating in Class C. Its performance was characterized and optimized to obtain the best tradeoff between linearity, output power, efficiency, and conducted and radiated noise. A waveform pre-distortion technique to correct for gain variations (dependent on input power and operating frequency) was demonstrated using digital techniques.

The amplifier system is a modular unit that can be expanded to handle a larger number of transmit channels as needed for future applications. The system can support sequential transmit/receive operations on a single antenna by using a high-power circulator and a duplexer circuit composed of two 90° hybrid couplers and anti-parallel diodes. The duplexer is advantageous over switches based on PIN-diodes due to the moderately high power handling capability and fast switching time. The system presented here is also smaller and lighter than previous implementations with comparable output power levels.
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1.0

0.4

0.3

0.2

0.1

0.0

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1 Introduction

1.1 Motivation

The National Science Foundation (NSF) established the Center for Remote Sensing of Ice Sheets (CReSIS) in 2005 as a NSF Science and Technology Center [1]. The mission of CReSIS is:

To improve understanding of the processes causing rapid changes to outlet glaciers and ice streams through targeted data collection campaigns combined with theoretical development and data interpretation, and to incorporate this understanding into numerical ice sheet models [2].

The data required to determine relevant boundary conditions and improve numerical ice sheet models includes ice thickness, bedrock topography, and basal conditions. Several techniques have been developed to obtain the required data sets, including ice cores, drilled to the bottom of the ice sheet; seismic techniques, gravimetry, and radar measurements. Radar measurements have several advantages over other techniques, including spatial and temporal resolution, along with the ability to cover wide areas.

The Multi-Channel Coherent Radar Depth Sounder/Imager (MCoRDS/I) is an instrument developed at CReSIS to enable routine measurements of ice thickness and bed topography from an airborne platform [3]. The data collected with MCoRDS/I is used to produce three-dimensional (3-D) images of the bed topography while providing information about the internal ice structure the ice surface to the base.
One of the primary targets of interest for the MCoRDS/I system is the fast flowing glacier areas and ice sheet margins. These targets are particularly challenging for radar sounding because of surface clutter combined with a higher attenuation through ice. These two factors combined can result in masking weak radar returns from the bed. Advanced signal and array processing techniques (such as minimum variance distortionless response (MVDR) algorithm) have been utilized with success on radar data to reduce the effect of clutter on many such areas [4-6]. MCoRDS/I has been flown over very wide areas on board of different airborne platforms. About 80% of the data used to generate an improved ice-bed map for the Greenland ice sheet has been collected with MCoRDS/I or one of its predecessors [7]. Bed maps for important outlet glaciers in Greenland and Antarctica have also been generated using MCoRDS/I data. With its highest power configuration, however, there are performance
limitations that have precluded the system from sounding a limited extent of some of these glaciers, producing small gaps in the data coverage.

Figure 1.1: Location of data shown in Figure 1.2 on Byrd glacier. Image produced by Dr. Jilu Li.
Figure 1.2: MCoRDS/I data from Byrd Glacier Antarctica 2011 showing the disappearing bed return through lossy ice. Image produced by Dr. Jilu Li.

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Figure 1.2 shows an example of an echogram produced with data collected over Byrd glacier in Antarctica in 2011. For comparison, a less lossy area, outside of the channel is shown in Figure 1.4. With a total of about 500-W of peak power distributed across six transmit antennas\(^1\) and flying almost 90 m above the ice surface, there was still a gap of a few km along the deepest part of the glacier channel. Results like these suggest that increasing the illumination power by a significant factor (4 to 10 times) could help enhance the performance of the radar to a point where the gaps in the data are further reduced. An alternative approach being explored to reduce such gaps is the use of lower operating frequencies [8].

\(^1\) 1200 Watts combined across 7 antenna elements is the maximum amount of peak power that the system can produce in its current configuration.
The goal of this thesis is to demonstrate a power amplifier circuit (and ancillary components), capable of producing approximately 1 kW of RF power over at least 30 MHz of bandwidth at a center frequency of 195 MHz. The combined use of multiple amplifiers with such capability will push the boundary of output power of the MCoRDS/I system to enhance its performance.

1.2 Previous Work

The power amplifiers used in the transmit section of previous renditions of the CReSIS radar depth sounders have traditionally consisted of off the shelf linear amplifier units [9-12] that were very large, heavy, inefficient, and expensive. These off the shelf systems were able to reach power levels above 1000 W, but it was not practical to use these on individual channels due to their size and cost. In addition, previous versions of the radar were designed to operate with a single transmit channel. The signals from the high-power module were split to each element in the transmit antenna array. Windowing of the power across antenna elements was accomplished by using attenuators [9]. When the waveform generator was later upgraded to support multiple channels, the power amplifier system was moved to lower power units, one for each antenna element [3, 6]. This allowed the amplitude and phase of the signal fed to each antenna be controlled individually to achieve digital beam forming and steering.

There have also been efforts to develop more efficient systems at CReSIS in the past. These in house developed systems have investigated using higher efficiency modes of operation using Class E amplification [13]. There have also been efforts to develop compact modules to be used with the Meridian Uninhabited Aircraft System (UAS) MCoRDS system [14]. While both
of these efforts have been successful, the output from these prototype amplifiers are 3.5 W and 150 W, respectively. Solutions at the 300-W level have been implemented successfully using COTS modules from Polyfet devices [15], yet, successfully imaging the bed of a limited extent of some outlet glaciers remains difficult in spite of the increased power.

1.2.1 Current Configuration

The MCoRDS/I system currently operates at 180 to 210 MHz with 250 watts per element after losses. MCoRDS/I utilizes Peripheral Component Interconnect Extensions for Instrumentation (PXI) a chassis from National Instruments (NI) to handle digitization, data storage and control functions. This system also provides the graphical user interface (GUI) to allow for operator control and visualization of unprocessed plot of return power as a function of range (A-scope) and a scrolling echogram. The 8-channel direct digital synthesis (DDS) waveform generator (WFG) described in [16], generates the 180 – 210 MHz chirp pulse used by the radar system. The waveform generator also generates the digital control signals required by other sub-systems. The transmitter power amplifier driver module filters the output from the WFG and provides additional amplification to drive the power amplifiers. After this stage is the current 300 W amplifier modules followed by transmit/receive switch and filters before going to the antenna port.
The received signal passes through the transmit/receive (T/R) switch, which feeds it to the Low Noise Amplifiers (LNAs). From the LNAs, the signal goes through the variable-gain receiver module where it is filtered and further amplified. The gain of the variable gain stage module is controlled by the NI PXI chassis [17]. Finally, a set of 16 independent 14-bit A/D converters with 500 MHz of analog bandwidth and a sampling rate of 250 MS/ in the NI PXI system are used to
digitize the received signal. The data is streamed into a redundant array of independent disks (RAID) for storage.

The current power amplifier combines the transmitter power amplifier section and T/R switch module into one chassis. The circuitry for each transmit/receive channel is mounted on a “slice plate” or “slice” that serves as a heat-sink for the power amplifier. This setup is given in more detail by the block diagram shown in Figure 1.6 showing the components for each individual slice.

![Figure 1.6: Block diagram of the current power amplifier slice configuration [18].](image)

The transmit power amplifier contains 7 slices that are identical to the one shown in the above block diagram. This allows each antenna element to have its phase and amplitude controlled, independent of the others.

1.2.2 Link Budget
The link budget for the current MCoRDS/I configuration is discussed in [17]. This budget calculates power of the radar pulse returning from the ice surface. This calculation is useful for determining the maximum power that will occur at the input to the receiver, but does not aid in calculating the power returned from the bed. To find how much power is expected from the bedrock return, the attenuation through the ice must be accounted for. The loss through ice in Greenland varies from 23.3 dB/km, one way, for the ice margins to 10 dB/km, one way, in the central ice sheet [19, 20]. The received power from the bed can be calculated as [21]

\[
P_r = P_t \left( \frac{\lambda}{4\pi} \right)^2 \frac{G_t G_r T_{\text{air-ice}}^2}{\left( h + Z/n_{\text{air-ice}} \right)^2 L_{\text{ice}}^2} |\langle R_{\text{ice-bed}} \rangle|^2
\]

where \( h \) is the height above the ice, \( Z \) is the ice thickness, \( L_{\text{ice}} \) is the one way attenuation through ice, \( n_{\text{air-ice}} \) is the refraction index of the air-ice interface, \( T_{\text{air-ice}}^2 \) is the transmission coefficient of the air-ice interface, \( G_t \) is the gain of the transmit antenna, \( G_r \) is the gain of the receive antenna, \( |\langle R_{\text{ice-bed}} \rangle|^2 \) is the spatially averaged reflectivity of the ice-bed interface, \( \lambda \) is the wavelength at the operating frequency (195 MHz in this case) and \( P_t \) is the transmitted power.

Results for the received power calculation for the MCoRDS/I radar during nominal operation are shown in Table 1.1 for the current 300 W setup and the 1-kW configuration proposed by this thesis. Although the calculations apply to any of the airborne platforms where the system is typically deployed, Table 1.1 focuses on the case of 7 transmit antenna elements used in the P-3 Airborne Science Laboratory from the National Aeronautics and Space Administration (NASA). Furthermore, Table 1.1 uses a specular bed for the value of \( |\langle R_{\text{ice-bed}} \rangle|^2 \). Although this calculation does not represent the worst-case scenario, it is
sufficient to illustrate the problem caused by lossy ice and the benefit of increased transmit power. These calculations show that the lossy ice, at the edge of the ice sheet, significantly reduces the return power of the radar signal. By simply increasing the transmit power, the received signal could be improved. The improvement in received signal power will result in an overall improvement in the signal to noise ratio (SNR).

Table 1.1: P-3 MCoRDS/I link budget with current and proposed configuration flown onboard the NASA P-3 Airborne Science Laboratory.

<table>
<thead>
<tr>
<th>Transmitter Power Per Element [dBm]</th>
<th>54.760</th>
<th>60.000</th>
</tr>
</thead>
<tbody>
<tr>
<td>Number of Elements --</td>
<td>7</td>
<td>7</td>
</tr>
<tr>
<td>Transmit/Receive Array Gain dBi</td>
<td>15.450</td>
<td>15.450</td>
</tr>
<tr>
<td>λ m</td>
<td>1.538</td>
<td>1.538</td>
</tr>
<tr>
<td>$\varepsilon_{\text{ice}}$ --</td>
<td>3.168</td>
<td>3.168</td>
</tr>
<tr>
<td>$\eta_{\text{air-ice}}$ --</td>
<td>1.780</td>
<td>1.780</td>
</tr>
<tr>
<td>$T_{\text{air-ice}}$ --</td>
<td>0.480</td>
<td>0.480</td>
</tr>
<tr>
<td>h m</td>
<td>457.2</td>
<td>457.2</td>
</tr>
<tr>
<td>Z m</td>
<td>2300</td>
<td>2300</td>
</tr>
<tr>
<td>$</td>
<td>\langle R_{\text{ice}}-\text{bed} \rangle</td>
<td>^2$ dB</td>
</tr>
<tr>
<td>$L_{\text{ice Central}}$ dB/km</td>
<td>10.000</td>
<td>10.000</td>
</tr>
<tr>
<td>$L_{\text{ice Margin}}$ dB/km</td>
<td>23.300</td>
<td>23.300</td>
</tr>
<tr>
<td>$P_r$ Central dBm</td>
<td>-90.839</td>
<td>-85.599</td>
</tr>
<tr>
<td>$P_r$ Margin dBm</td>
<td>-152.019</td>
<td>-146.779</td>
</tr>
</tbody>
</table>

The minimum discernable signal (MDS) for MCoRDS/I is around -150 dBm. From the results of the calculations, shown in Table 1.1, it can be seen that the current, lower output power configuration would not be sufficient in sounding the bed for the given parameters. The increased power solution does exceed the MDS for the MCoRDS/I system.

1.3 This Work
This thesis presents the implementation and characterization of an amplifier for the MCoRDS/I system developed using a 1-kW amplifier pallet and reference design from Freescale Semiconductor, Inc. The modifications needed to use a highly non-linear amplifier for ice sounding radar are presented. The amplifier and ancillary components were integrated with a set of low-noise switching power supplies to support transmit/receive operation using a compact chassis. In addition, a T/R duplexer design commonly used in nuclear magnetic resonance (NMR) spectroscopy for magnetic resonance imaging (MRI), is evaluated for use in an ice-penetrating radar application.

This thesis presents the development, implementation and characterization of an amplifier for the MCoRDS/I system developed using a 1-kW amplifier pallet and reference design from Freescale Semiconductor, Inc. The modifications needed to use a highly non-linear amplifier for ice sounding radar are presented. The amplifier and ancillary components were integrated with a set of low-noise switching power supplies to support transmit/receive operation using a compact chassis. In addition, a T/R duplexer design, commonly used in nuclear magnetic resonance (NMR) spectroscopy, for magnetic resonance imaging (MRI), is evaluated for use in an ice-penetrating radar application. A single-channel prototype T/R system was constructed and characterized. The system can be easily extended to multiple channels.

1.4 Thesis Outline

The thesis is organized in seven chapters outlined as follows. Introductory information, such as previous work that this thesis builds upon and the motivation behind this work is given
in chapter 1. In chapter 2, background theory on concepts used in this thesis is presented. Chapter 3 introduces the 90° hybrid coupler based duplexer circuit and describes the theory of operation. Additional development work to make the 90° hybrid coupler a practical T/R module is presented in chapter 4. Chapter 5 documents the characterization of the prototype amplifier developed for this thesis. The digital predistortion system developed to allow shaping of the output amplitude is described and characterized in chapter 6. Chapter 7 presents the conclusions from this thesis and provides recommendations for future work.

2 Background

In this chapter, an overview of some basic definitions and concepts related to power amplifiers and duplexers will be presented as a framework.

2.1 Power Amplifier Class Definitions

There are four modes of operation of RF power amplifiers that are considered to be the classical configurations: Class A, Class B, Class AB and Class C. There are also more advanced techniques of amplifier design that can be lumped into high efficiency modes. The high efficiency modes of operation are the most actively researched today. A detailed overview of the four classical modes of operation will be presented in this chapter. A brief overview of the higher efficiency modes will also be given, as there are numerous techniques that do not apply directly to the work presented in this thesis.
2.1.1 Class A

An amplifier is considered to be operating in Class A when it conducts for the entire 360 degrees of the input signal. This mode results in the least amount of distortion when compared to an ideal amplifier as it fully reproduces the input signal at the output. This near perfect linearity of the device comes at the price of efficiency. The theoretical maximum efficiency of a Class A amplifier is 50% [23], where efficiency, \( \eta_0 \), is defined as [24]:
\[ \eta_0 = \frac{P_{rf, out}}{P_{dc}} \]  

(2.1)

with \( P_{rf, out} \) being the output RF power and \( P_{dc} \) being the DC power at the operating point of the amplifier. For a Field-Effect-Transistor (FET)-based amplifier, the 50% efficiency value assumes the knee voltage, or gate voltage, at which the drain current becomes constant, is zero. A device with a knee voltage of zero is not realizable in practice, and therefore the 50% efficiency value is only theoretical. The actual realized efficiency is often much less than 50% and makes this configuration problematic for situations where available DC power is limited.

### 2.1.2 Class B

The amplifier’s efficiency can be improved by lowering the DC-bias point of the amplifier, which reduces the conduction angle. This is seen in the Class B amplifier. The Class B amplifier conducts for 180 degrees of the input signal cycle resulting in higher efficiency, with a theoretical maximum of 78.5%. The drawback to the Class B amplifier is harmonic distortion [25]. By lowering the bias point of the amplifier, more distortion, as compared to Class A amplifiers, is produced to where half of the input signal appears clipped at the output. This sharp transition results in spurious signals being produced.

### 2.1.3 Class AB

The Class AB amplifier is the middle ground between the Class A and Class B configurations. This type of amplifier is often implemented as two transistors in the so-called push-pull configuration. In the push-pull amplifier configuration, two parallel transistors are fed 180 degrees out of phase. When each transistor is biased in Class AB, the sum of the push-pull circuit conducts for more than 180 degrees but less than 360 degrees. There is a small discontinuity when the signal reaches the threshold voltage of the device, causing a short off
period. While there is some off time in this configuration, the distortion is much less than Class B while still obtaining efficiency improvements from Class A. Efficiency values can be expected to be between 50% and 78.5%, depending on how close the amplifier is biased to Class A or Class B.

2.1.4 Class C
Reducing the conduction angle further than in Class B, less than 180 degrees of the input cycle, the Class C amplifier becomes more efficient. Again, this increased efficiency comes at a cost of linearity. Due to its highly nonlinear properties, the Class C amplifier is usually reserved for applications with a constant envelope, such as FMCW radars.

Class C amplifiers can reach 100% efficiency as the conduction angle is reduced to zero. Most practical implementations of a Class C amplifier will realize 50% to 75% efficiency [26]. The efficiency gain for Class C is accomplished by not conducting while the input signal is below the gate threshold of the transistor. Due to the nonlinearity of conducting less than 90 degrees of the input signal, the output must be filtered in some way. The trade off with Class C operation is the amplification of the amplitude is not linear. Since most AM systems are very sensitive to amplitude distortion, the Class C amplifier is not commonly used in cases where the wave is anything other than CW.

2.1.5 High Efficiency Modes
Higher efficiency modes of amplifier operation are an area of active amplifier research. The power requirements of battery powered cellular handsets have driven this topic. Examples of these high efficiency modes of operation are Class D and Class E. These classes of amplifiers rely on using the transistor as a switch, generating square waves. The harmonic frequencies
that make up the square wave are passed through a tuned output network so only a sine wave remains. Both can practically realize 90%, or better, efficiency [22-25, 27]. These modes will not be discussed further as they are beyond the scope of this thesis.

2.2 Figures of Merit

There are several figures of merit to quantify the performance of RF power amplifiers relevant to radar performance. In this chapter, a summary of the most commonly used figures of merit (gain, bandwidth, efficiency, distortion, etc.) will be given.

2.2.1 Gain

There are several approaches to defining the gain of an amplifier. Gain can be defined as the transduce power gain, the available power gain or the maximum gain available. It is important to understand which definition of gain is being used when talking about the gain of an amplifier. The most useful definition for this application is the transducer gain. This is given by Equation (2.2) as[27]:

$$G_T = \frac{\text{power delivered to the load}}{\text{power available from the source}}$$  \hspace{1cm} (2.2)

This definition of transducer gain will be used throughout this work, unless otherwise noted, and will be referred to as “gain”. The transducer gain provides the amount of small signal gain achieved at the output of the amplifier device compared to the small signal at the input of the amplifier.

The other two measurements of gain: the maximum available power gain and the available power gain are given in Equations (2.3) and (2.4) respectively[27].
\( G_A = \frac{\text{power available from the network}}{\text{power available from the source}} \) \hspace{1cm} (2.3)

\( G_P = \frac{\text{power delivered to the load}}{\text{power delivered to the network}} \) \hspace{1cm} (2.4)

The definition of maximum available power gain, shown in Equation (2.3), includes the DC power that is available from the network, along with the RF power. Available power gain is the ratio of RF power delivered to the load and the sum of the DC and RF power input into the amplifier. The relationship between output RF power and input DC and RF power is shown in Equation (2.4). The inclusion of DC power makes these metrics difficult to obtain from measurements. Additionally, they depend on the efficiency of the amplifiers.

### 2.2.2 Bandwidth

There are key metrics of amplifier design that determine the bandwidth of a power amplifier. Examples of these key metrics are gain, power added efficiency, output power, input match and output match. The metrics that make up the bandwidth definition will depend on the requirements of the design. We will define bandwidth as the upper and lower frequencies at which the gain or output power drops by 3 dB.

### 2.2.3 Power Added Efficiency (PAE)

The power added efficiency (PAE) of an amplifier differs in the standard definition of amplifier efficiency, as shown in Equation (2.1), in that the RF power input into the amplifier is taken into account. The PAE is defined in Equation (2.5)[27].

\[ PAE = \frac{\text{output signal power} - \text{input signal power}}{\text{DC power}} \] \hspace{1cm} (2.5)
This metric is useful in finding the efficiency for each stage in a cascaded design. The harmonic power must be included in the output signal power in order to obtain an accurate PAE measurement.

### 2.2.4 Harmonic Power

Ideally, an amplifier is a linear device. It is practically impossible to create a perfectly linear amplifier. For this reason, nonlinear effects must be taken into account in the design. The nonlinear amplifier can be described by the Taylor series\[26\]. This series, in terms of the input and output voltages of the amplifier \((v_i \text{ and } v_o, \text{ respectively})\), is shown in Equation (2.6).

\[
v_o = a_0 + a_1 v_i + a_2 v_i^2 + a_3 v_i^3 + \cdots \tag{2.6}
\]

With the coefficients:

\[
a_0 = v_o(0) \tag{2.7}
\]

\[
a_1 = \frac{dv_o}{dv_i} \bigg|_{v_i=0} \tag{2.8}
\]

\[
a_2 = \frac{d^2v_o}{dv_i^2} \bigg|_{v_i=0} \tag{2.9}
\]

When a single tone, Equation (2.10), is applied to the input of the amplifier, it can be shown that frequency products (harmonics) at multiples of the original (fundamental) tone are produced.

\[
v_i = V_0 \cos \omega_0 t \tag{2.10}
\]

Substituting (2.10) into (2.6) is shown in Equation (2.11), where terms out to the third harmonic are shown.
\[ v_o = \left( a_0 + \frac{1}{2} a_2 V_0^2 \right) + \left( a_1 V_0 + \frac{3}{4} a_3 V_0^3 \right) \cos \omega_0 t \]

\[ + \frac{1}{2} a_2 V_0^2 \cos 2\omega_0 t + \frac{1}{4} a_3 V_0^3 \cos 3\omega_0 t + \cdots \]  

Equation (2.11) shows that the signal at the output of the amplifier is composed of the fundamental frequency, \( \omega_0 \), as well as higher order terms. The amplitude of the harmonic signals is a function of the input amplitude and the Taylor series coefficients. It can be shown that the Taylor series coefficients are related to the nonlinearity of the amplifier. For this reason, the more nonlinear the amplifier is, the larger the harmonic signals will be. The metric for the harmonic amplitude is often described as dBc, decibels referenced to the carrier, \( f_0 = 2\pi \omega_0 \), amplitude.

In relatively narrowband systems, harmonic signals produced by the amplifier must be suppressed to prevent interference to other users of the radio spectrum. The most direct way of accomplishing this is to filter the harmonic frequencies. The downside to this method is that power was taken away from the desired signal to produce these harmonics. This results in a lower output power of the desired frequency and a lower efficiency of the amplifier. Another method that is often employed by high efficiency mode amplifiers[23], is to feed the harmonics back into the input of the amplifier in such a way that the harmonic frequencies are canceled while the power at the fundamental frequency is retained.

### 2.2.5 Intermodulation Distortion (IMD)

Intermodulation Distortion is another metric of amplifier linearity. Intermodulation Distortion occurs when two or more closely spaced tones are used as the input signal to the amplifier. Ideally, only the two tones should be seen at the output of the amplifier. Due to the
effects of nonlinear components in the amplifier, additional frequency components are generated, as described in Section 2.2.4. These same equations used in Section 2.2.5 can be applied to the two tone case by substituting Equation (2.12) into Equation (2.6)[23].

\[ v_i = V_0 (\cos \omega_1 t + \cos \omega_2 t) \]  \hspace{1cm} (2.12)

This substitution will result in additional frequency components appearing at frequencies close to the desired input tones. In nearly all cases, these will fall within the pass band of the amplifiers output matching network as well as the output filtering circuit. This will result in a distorted signal. The frequencies produced can be calculated by Equation (2.13) and the output spectrum is illustrated in Figure 2.2.

\[ \omega_o = m\omega_1 + n\omega_2 \]  \hspace{1cm} (2.13)

Where \( m,n=0,\pm1, \pm2, \pm3,\ldots \). The sum \(|m|+|n|\) is the order of the intermodulation product[23].

![Figure 2.2: Illustration of the output signal spectrum showing intermodulation products][23]

The intermodulation products closest to the fundamental frequencies will be of the third-order. For this reason, the third-order intermodulation product (IM3) is used as a common metric of the linearity of the amplifier, along with the harmonic power.
2.2.6 Noise Figure

Thermal noise is generated by the thermal agitation of charge carriers and is one of the most dominant contributors to the overall noise in RF amplifiers. The random motion of the charge carriers produces noise at all frequencies with the same power density. The power of the noise produced is expressed by the noise power $P_N$, given as [22-25, 27-29],

$$P_N = kTB \ [W]$$  \hspace{1cm} (2.14)

where $k$ is the Boltzmann’s constant $(1.38 \times 10^{-23} \text{ J/K})$; $T$ is the operating temperature of the device in Kelvin. For room temperature, $T$ is equal to 290 K as per IEEE standards; and $B$ is the bandwidth of the system in Hz. Thermal noise is commonly quantified in terms of an equivalent noise temperature. The relationship between noise power and noise temperature is defined as:

$$T = \frac{P_N}{k} \ [K]$$  \hspace{1cm} (2.15)

A power amplifier is commonly composed of multiple stages to achieve the required gain and output power. Each amplification stage will not only amplify the signal but also amplify the noise present at its input and add in the noise generated within each stage. A common figure of merit to quantify the amount of noise power produced by a system is the noise factor. When the noise factor is expressed in dB, the figure of merit is referred to as figure (NF) of the system. As different stages are cascaded together the noise factor of the system can be expressed as (2.16)
\[
F = F_1 + \frac{F_2 - 1}{G_1} + \frac{F_3 - 1}{G_1 G_2} + \cdots + \frac{F_N}{G_1 G_2 \cdots G_{N-1}} \tag{2.16}
\]

Where \(F_N\) is the noise factor of the \(N\)th stage \(N\) and \(G_N\) is the gain of the \(N\)th stage. From this equation, it can be seen that the noise factor of the system is strongly dependent on the noise factor and gain of the first stage.

Small signal devices, such as low-noise amplifiers (LNA), are optimized to have a low NF. The NF is a function of the DC-bias settings as well as the impedance presented to the active devices within each stage. The matching and bias levels are designed in such a way that this requirement is satisfied. RF power amplifiers are designed so the best impedance match and maximum power output are achieved. RF power amplifiers are not optimized for minimum noise, and thus noise figures exceeding 10 dB are not uncommon [30, 31].

2.2.7 Mean Time To Failure

The mean time to failure (MTTF) is a metric to quantify how long a semiconductor device can operate reliably before failing. Devices typically have failure times on the order of years under normal operating conditions. Devices can be expected to last between 10 and 100 years [27]. MTTF can be shorter if the devices are subject to extreme operating conditions such as transients, extreme thermal cycling, or ESD events. The failure rate, \(\lambda\), which is defined as \(1/\text{MTTF}\), is plotted in Figure 2.3 [32]. The failure rate of a device fits what is known as the “bathtub” curve, where most failures occur in a very short period of time or toward the end of the operational lifetime [24]. Assuming the specified junction temperature of the device is not exceeded, it is safe to assume that if a device does not fail within the first few minutes or seconds, it will last up to the wearout period. In between the early failure and wearout periods,
there will be random failures. These random failures occur at a much lower rate than the failure mechanisms at the beginning and end of life.

Figure 2.3: Plot of a typical failure rate as a function of time for a semiconductor device [32].

The designed lifetime is determined at a specific junction temperature. By decreasing the rated junction temperature, the device life can be extended and inversely, shortened by exceeding the specified junction temperature. The relationship of junction temperature to the lifetime of the device can be expressed by the Arrhenius model shown in Equation (2.17) [27]:

\[ \text{MTTF} = C e^{\frac{E_a}{kT_j}} \]  

(2.17)

where C is a constant, \( E_a \) is the activation energy [eV], k is Boltzmann’s constant, and \( T_j \) is the junction temperature. Equation (2.17) shows that the MTTF decreases exponentially with temperature.
2.2.8 Thermal Resistance

During normal operation, the junction of the transistor is heated as power is dissipated on the device. The amount of power dissipated is calculated by Equation (2.18) [33].

\[ P_{\text{diss}} = \left( \text{RF input power} + \text{DC power} (I_D \times V_D) \right) - \left( \text{RF output power} + \text{RF reflected power} \right) \]  

The dissipated power is released as heat. The released heat causes a temperature increase in the device because of thermal resistance to conduction, radiation, or convection. Thermal resistance is the opposition to the dissipation of heat. The analog to thermal resistance in electronics is the resistor; therefore it can modeled as such. The thermal resistance of a solid using conduction to dissipate heat is described as

\[ R_{\text{th}} = \frac{h}{K_{\text{th}}(W)(L)} \left[ ^{\circ}\text{C}/\text{W} \right] \]  

where \( h \) is the height of the conducting solid, \( W \) is the width of the heat source, \( L \) is the length of the heat source, and \( K_{\text{th}} \) is the thermal conductivity of the conducting solid.

\[ R_{\text{th}} = \frac{h}{K_{\text{th}}(W + 2h)(L + 2h)} \left[ ^{\circ}\text{C}/\text{W} \right] \]  

For the case where the area of the heat source is smaller than the heat sink, Equation (2.20) incorporates the 45 degree thermal spreading angle through the solid.
Continuing with the electronics analogy, the temperature difference across a thermal resistance can be modeled as a voltage. The power dissipated as heat is modeled as a current source. From this, it can be seen that as the thermal resistance builds, so does the temperature differential for a constant power dissipation.

\[
\Delta T = P_{\text{diss}} R_{\text{th}} \quad [\degree \text{C}]
\]

Equation (2.21) can be expanded to include the total heat dissipation system when \( R_{\text{th}} \) is the total thermal resistance. The absolute temperature of a device, such as the transistor junction, can be calculated by adding in the ambient temperature:

\[
T_D = (P_{\text{diss}} R_{\text{th}}) T_A \quad [\degree \text{C}]
\]

where \( T_D \) is the temperature of the device and \( T_A \) is the ambient temperature.

### 2.3 Power Amplifier Linearization

The linearization of a power amplifier is an important design aspect when trying to realize practical amplifiers. Practical amplifiers have nonlinearities that can produce distortion in both amplitude and phase. These non-ideal components need to be corrected in order to achieve the maximum efficiency and the most faithful reproduction of the input signal.

For advanced radar imaging, the MCoRDS/I system requires that the range sidelobes be suppressed by at least 50 dB. It has been shown by [34] that to accomplish this suppression of range sidelobes, windowing the amplitude of the transmit waveform with a suitable profile must occur. The effects of nonlinearities and frequency-dependent behavior in the power...
amplifier need to be compensated to achieve the required level of range sidelobe suppression. Without compensation, the envelope of the transmit waveform will exhibit strong amplitude modulation, which will result in performance degradation.

Common techniques for correction of non-linear behavior include feedforward, feedback and pre-distortion. In the feedforward linearization technique, the input and output signals are compared and the IMD products are amplified by an error amplifier and fed back into the signal path. This is done in a way that the IMD products cancel and only the input signal remains [27]. Feedback in amplifiers can be used to correct gain variations with frequency. In the feedback linearization technique, the output of the amplifier is fed back into the input of the amplifier through a tuned network. This network adjusts the gain of the desired frequency ranges to flatten the output of the amplifier [24].

2.3.1 Pre-Distortion
Signal pre-distortion is used to compensate for nonlinearities and can be realized using analog or digital techniques. The goal of pre-distortion is to modify the input signal to cancel out any nonlinearities produced at the output of the power amplifier. An example to illustrate how this technique works is presented in Figure 2.4. The input signal with the pre-distortion, \( \beta(V_i) \), is applied to the amplifier with the transfer function, \( F(\alpha) \), to produce a linear output signal.

![Illustration of the pre-distortion technique](image)

Figure 2.4: Illustration of the pre-distortion technique[35].
2.3.1.1 Analog Pre-Distortion

Traditional methods in analog pre-distortion include using diodes or variactor diodes to produce second- and third-order transfer functions. As an example of such circuits, the schematic diagram of a second-order and third-order pre-distortion circuit can be seen in Figure 2.5 and Figure 2.6, respectively. In the first case of Fig. 2.4, the diode biasing point and the value of the parallel capacitor can be adjusted to match the distortion of the amplifier.

![Schematic diagram of a series diode pre-distorter](image)

Figure 2.5: Circuit diagram of a series diode pre-distorter [35].

In the second example shown in Figure 2.6, the circuit generates third-order distortion that cancels out the third-order IMD products. The matching and biasing circuits are left out of the schematic in this example for clarity. There are other practical considerations for this design but they are beyond the scope of this work.
2.3.1.2 Digital Pre-Distortion

Digital pre-distortion (DPD) utilizes digital signal processing (DSP) techniques to accomplish the same tasks as its analog counterpart. There are several advantages to DPD over analog techniques, the first being the same advantage of any DSP system over its analog counterpart. Once analog values are measured and digitized, the operations performed can be considered ideal; there are no longer any issues with electronic components aging or tolerance variations in component values. In addition, the point at which the pre-distortion is implemented can be moved from RF down to baseband. This greatly relaxes the requirements for the digital to analog converter (ADC). Adaptive algorithms can also be implemented easier in the digital domain.

Some distortion effects can change with time. One example of a distortion mechanism that changes with time is amplifier memory effects. When the output of an amplifier is dependent not only on the input, but the past output of the amplifier, it is said to exhibit memory. For time varying situations like memory, an adaptive DPD algorithm can be applied.
Figure 2.7 shows a block diagram of a typical DPD system implementation. The chapter to the left of the Digital to Analog Converter (DAC) and ADC blocks are realized in software. If the DAC is capable of directly generating an RF signal, the modulation and up-conversion (Mod & Upconv) block can be omitted. The same is true for the ADC. If the ADC is fast enough to directly sample the RF signal, the demodulation and down-conversion (Demod & Downconv) can be omitted as well. Once the coupled RF output from the PA is digitized, it is used in the Adaptation Algorithm. This algorithm compares the signal coming out of the PA to the input signal, $V_i$. Since a linear amplifier should increase the amplitude of the input signal, and change nothing else, $V_i$ is used as the reference, or ideal signal. The reference signal is compared to the output RF signal and corrections are placed in the lookup table. From the lookup table, the gain and phase of the input to the DAC is adjusted so the output from the PA will be the same, with respect to gain and phase, as the reference signal.

### 2.4 Duplexer Circuits

A duplexer is a circuit that enables the sharing of a single antenna for transmit and receive operations. There are several methods commonly used to accomplish this. The most
common techniques in the context of radar applications are the use of T/R switches and ferrite circulators. Other duplexer circuits, designed with RF techniques that vary according to the frequency of operation, can also be used.

2.4.1 T/R Switch
The T/R switch allows a transmitter and receiver to share the same antenna and transmission path by changing which input port on the switch is connected to the output. For power levels exceeding 100 Watts, this is normally accomplished by a mechanical relay or by PIN-diodes. The ability to handle high power in these types of switches comes at the expense of relatively slow switching speeds. Switching speeds are normally quantified by measuring the time for the RF to reach 90% at the maximum output, after the TTL signal has reached 50% of its maximum, or above. Inversely, the turnoff time is determined by measuring how long the RF output takes to reach 10% of maximum, from when the TTL reaches 50% or below. Fast switching speeds in the order of 1-2 μs are required for the MCoRDS/I system, while switching speeds on the order of 10 μs are typical for off-the shelf switches capable of handling 2 kW of power. Another disadvantage of PIN diode switches is that they require high operating voltages and produce large video feed through signals.

2.4.2 Ferrite Circulators
Ferrite circulators can also be used as a duplexer. Circulators can be configured to allow for simultaneous transmit and receive using a single antenna. The disadvantage to using this type of devices is that they possess narrow bandwidth and finite isolation in the reverse direction. In addition, power that is reflected from the antenna will be sent to the receiver, so a suitable blanking switch and limiting device need to be used to protect the receiver.
2.4.3 Diplexer circuits

Diplexers can be used as duplexing devices as well. A diplexer provides a constant impedance at its input and can direct a signal, depending on the signal’s frequency, to different outputs [36]. A diplexer can be implemented using discrete components, forming high pass and low pass filters. If high enough frequencies are used, where 90° hybrid splitters are practical, the diplexer can be implemented as shown in Figure 2.8.

![Figure 2.8: Diplexer implemented with 90° splitters and bandpass filters [36].](image)

The diplexer uses two 90° splitters and two identical bandpass filters. When signals are rejected by the bandpass filter, the reflected power exits the bandstop output. Signals that are allowed to pass through the bandpass filter are recombined and exit the bandpass port of the second 90° splitter. This method of duplexing a signal relies on Frequency Division Multiple Access (FDMA) principals, where the two signals have different frequencies, but allows for transmit and receive at the same time. Although the FDMA scheme is not applicable to radar systems, some of the concepts from diplexers will be used later in the duplexer system proposed by this thesis.
3 Duplexer Circuits

3.1 Overview of T/R Switch Technologies

For pulsed radar applications, the time it takes for a radar to transition from transmit to receive is known as the switching time. The pulse duration along with the switching time makes up the blind range. The blind range is defined in Equation (3.1), where $c$ is the speed of light in m/s, $\tau$ is the duration of the pulse, and $t_{\text{switch}}$ is the time the T/R switch takes to transition from transmit to receive.

$$R_{\text{blind}} = \frac{c \tau}{2} + c t_{\text{switch}} \text{ [m]}$$  \hspace{1cm} (3.1)

From this Equation, it can be seen that $t_{\text{switch}}$ directly affects the length of pulse allowed by a set blind range. In RF switches, $t_{\text{switch}}$ is commonly quantified from 50% of the TTL control line high to 90% RF for turning on and 50% TTL control line low to 10% RF for turn off. For the specific example of the MCoRDS/I system, the blind range must be no larger than 500 meters, the nominal survey altitude for surveys [4].

In the past, CReSIS has used PIN-Diode switches to implement fast switching T/R modules. As discussed in Section 2.4, there are tradeoffs in power handling for fast switch times when using PIN-diodes. The tradeoffs associated with using these switches with the MCoRDS/I system have made us consider other potential alternatives.

The balanced duplexer described in [37, 38] operates using many of the same principals used in the diplexer implemented with 90° splitters, described in Section 2.4.3. In this application, the bandpass filters are replaced with anti-parallel diode pairs, using 1N4148
devices. Now, instead of rejecting frequencies, low voltage signals are allowed to pass (cross-diodes off) while high power signals are reflected. These voltage levels directly correspond to power level within the 50 ohm system. Figure 3.1 shows the schematic for this design. This method was borrowed from Nuclear Magnetic Resonance (NMR) imaging, more commonly known as Magnetic Resonance Imaging (MRI), technology. The figure refers to a “probe”, while this port would be connected to the antenna in our application.

![Figure 3.1: Balanced duplexer design [37]. In our application the probe is replaced by the transmit/receive antenna.](image)

The quadrature hybrid (QH) ports are defined in Figure 3.2. When the transmitter or, in the context of this thesis, amplifier output exceeds the threshold voltage of the antiparallel diodes between the two QH couplers, they are forward biased and begin to conduct. This presents a short to ports 2 and 3 on the QH. This short causes the incoming RF to complexly reflect back into the QH, exiting port 1. This operates in the same fashion as a traditional T/R switch, without the need for a control signal, relying only on the amplitude of the transmit signal to forward bias the diodes.
When the output of the transmit amplifier is below the voltage required to forward bias the anti-parallel diode pairs, the output from the power amplifier, incident on port 4 of the first QH, is passed through to the 50 ohm load. This increases isolation from the amplifier and receiver. Additionally, any leakage during transmit goes into the 50 ohm load as well, protecting the sensitive receiver.

This design is limited by the power handling capability of the QH devices and the current handling ability of the diodes. The switching time of the balanced duplexer is set by the response time of the diodes used. For the 1N4148 device, the diode switching time is 4 ns [39], resulting in a 4 ns T/R switch time of the balanced duplexer. The diodes can handle 450 mA repetitive peak forward current and 100 V repetitive peak reverse voltage. Given these specifications, operation should not exceed 50 dBm, although [37] mentions higher operation. To test this configuration, a prototype duplexer was assembled in the laboratory using high power hybrids from Innovative Power Products (IPP-2269 [40]). The insertion loss and isolation between different ports was measured with a network analyzer for low power condition. For high power conditions, our laboratory tests confirmed the 50 dBm limit quoted by [37]. The duplexer in this configuration worked for transmit powers of up to 1 kW for short amounts of
time, but the high transmit power resulted in excessive heating in the diodes to an unusable level for extended operation.

3.1.1 Narrowband Implementation with Transmission Lines

The primary failure mechanism with semiconductor devices is exceeding the junction temperature. This holds true with the 1N4148 diode. One method to reduce the heating of the diode is to reduce the current flow. One method to accomplish the reduction in current without sacrificing power is to use quarter-wave transmission lines between the QH and diode pairs [38]. With the quarter-wave transmission line sections the short created by the diodes appears as an open at the QH. This results in a full reflection with no current flow.

4 T/R Module

4.1 Initial Design

The initial design for the T/R module originally consisted of the duplexer described in chapter 3. Since the power capability of the balanced duplexer as described in [37] was limited to 100 Watts. The results from higher power levels into this circuit are presented in chapter 5.9.2.

4.2 Final Design

A circulator was selected for the high power path of the T/R module. There are two drawbacks to using a circulator alone as a T/R module. This first is the insertion loss of the device. For the selected circulator, insertion loss is 0.7 dB. At 60 dBm output from the amplifier, this results in 149 W of power loss through the device. The second disadvantage is any reflected power from the antennas will be sent to the receiver. The antennas on the P-3 array are designed to have a
-10 dB worst case match. At 60 dBm output, this results in 50 dBm, or 100 W reflected power into the receiver. This power level would result in the destruction of the receiver.

To deal with the reflected power from the antenna, the duplexer described in [37] was employed. The input and output ports of the duplexer circuit were changed slightly to fulfill its new role as an isolation switch. The topology of the circulator/duplexer based T/R switch can be seen in Figure 5.3. Limiters were added to the low power output of the duplexer to reduce the leakage from the circuit.

5 1-kW Prototype Amplifier for MCoRDS/I

The implementation and characterization of a high-power amplifier prototype capable of producing power levels close to 1 kW will be discussed in this Chapter. A detailed description of the measurement setup and results will be given.

5.1 Amplifier Design Overview

The design of the amplifier system began with defining the requirements of the amplifier system. A summary of these requirements is listed in Table 5.1.

<table>
<thead>
<tr>
<th>Requirement</th>
<th>Specification</th>
</tr>
</thead>
<tbody>
<tr>
<td>Power Output</td>
<td>1000 W</td>
</tr>
<tr>
<td>Frequency Response</td>
<td>180-210 MHz</td>
</tr>
<tr>
<td>Gain</td>
<td>&gt;60 dB</td>
</tr>
<tr>
<td>Gain Flatness</td>
<td>+/- 1 dB</td>
</tr>
<tr>
<td>Gain linearity</td>
<td>+/- 1 dB</td>
</tr>
<tr>
<td>Efficiency</td>
<td>&gt;70%</td>
</tr>
<tr>
<td>Pulse Droop</td>
<td>&lt; 10%</td>
</tr>
<tr>
<td>Distortion, harmonic</td>
<td>&lt; -40 dBc</td>
</tr>
<tr>
<td>Distortion, inter-modulation</td>
<td>&lt; -20 dBc</td>
</tr>
<tr>
<td>Operating temperature</td>
<td>-40 to 100 C</td>
</tr>
</tbody>
</table>
Two of the key initial constraints in previous implementations of amplifiers for the MCoRDS/I system were that the amplifier be linear and that the amplifier be turned off fast enough, by removing the gate bias, during receive. The amplifier is turned off during receive to eliminate noise produced by the amplifier and to reduce the average DC power consumption. When an amplifier is on and no signal is present, it still amplifies noise incident at the input port. In addition, the amplifier itself generates noise; this also appears at the output. The implementation of the gate bias switching circuit is described in [14, 41]. Switching the gate voltage on and off quickly is not trivial due to the resistive-capacitive (RC) time constant formed in the input capacitance and the resistance of the input network to the gate. Another drawback to the switching method is the circuit is constantly drawing current, reducing the amplifiers overall efficiency.

Another factor that drives the need for a gate bias switching circuit is the requirement that the amplifier be linear. To accomplish a truly linear amplifier, a Class A configuration must be used. The gate is biased so the entirety of the input signal is conducted. By biasing the amplifier this way, low amplitude signals, such as noise, are above the threshold and are also amplified. These signals can be lowered below the threshold by lowering the bias point to below the threshold voltage. This takes the amplifier out of Class A operation and puts it in Class C mode. The Class C amplifier advantage is being off for half of the signal cycle and off when no signal is present. This improves efficiency and has the same effect as switching the gate bias off. Since the MCoRDS/I system is sensitive to external noise sources, added noise
from the amplifier cannot be tolerated. The efficiency requirement is driven mostly by the DC power available in the aircraft where the system has been deployed, as well as volume and weight. Although highly efficient design is beneficial in general, this constrain becomes particularly important for a multi-channel system like MCoRDS/I. Previous implementations of high-power amplifier required combining more than one power amplifier chassis of fair size and weight to produce the required power. For instance, the configuration described in [11] required a set of two amplifiers to obtain 800 W of total peak power at 150 MHz and another set of two amplifiers to produce 1.6 kW at 450 MHz. The system used a passive network to feed the antenna array, resulting in a maximum of 300 W per antenna element after losses, and did not allow controlling the phase and amplitude of the signal fed to each antenna element. The most recent configuration of MCoRDS/I features about 250-Watts of peak RF power per channel using individual power amplifier modules. With a maximum of seven channels, a total of about 1750 W of total peak power is achieved with this system [4]. With the implementation presented here, the goal is to enable single channel modules with up to 1 kW of peak output power per channel.

As mentioned above, another requirement for the MCoRDS/I system is the linearity of the power amplifier. As discussed in chapter 2.2.5, multiple signals cause intermodulation issues. For an amplifier used in communications systems, for instance, where multiple carriers or multiple frequency components can be produced by a single transmitter at any given time, the linearity of a Class C amplifier would be sub-optimal. Fortunately, for the case of the narrow-band MCoRDS/I radar, only one tone is present at the input at any given time. This means that only the harmonics of the fundamental tone are produced by a class-C amplifier
and the requirements for low IMD are relaxed. Any harmonics produced by the single tone are filtered by the output matching network and harmonic-rejection band pass filter, which is already present in the transmit/receive path. With the above considerations regarding narrow-band pulse operation, efficiency and linearity, the class-C amplifier is a viable choice for the power amplifier for the MCoRDS/I system. The gain of RF amplifiers is always affected by some type of frequency dependence. Because of its non-linear behavior, Class C amplifiers also exhibit a gain that depends on the amplitude of the input signal. It is possible to correct the non-linear gain by adjusting input signal amplitude to produce the required output from the amplifier. This process is also a form of pre-distortion.

Initial investigations proved that the design and test of a 60 dBm, 1000 watt amplifier is not a trivial process. It requires the purchase of specialized test equipment for high power measurements. Errors incurred during the testing phase can destroy active devices ($200-300 range per device), resulting in increased development costs. With this in mind and to reduce development time, a commercial off the shelf (COTS) or semi-COTS solution was considered. Choosing a semi-COTS solution also allowed us to direct our efforts toward the optimization of the radar performance.

The frequency range of the MCoRDS/I system is 180 to 210 MHz. This is within the VHF TV Broadcast band. Out of the available products, the Freescale VHF Digital TV Broadcast Reference Design [42] was selected. This design uses the Freescale MRFE6VP61K25H transistor [43]. Along with its gain and output power, the device was also selected for its ruggedness. The transistor can withstand a load mismatch greater than 65:1 [43]. By using a device this
rugged, damage and destruction of the amplifier can be avoided during cases of operator failure. Figure 5.1 shows the schematics of the design as taken from the Reference design [42].

The amplifier is comprised of four main sections: input matching, drain bias, gate bias circuit, and output matching. The gain bias circuit contains a voltage regulator that uses a transistor (Q1) with a similar temperature coefficient as the [42] transistor. The voltage regulator circuit adjusts the gate bias voltage to maintain the same quiescent current. This keeps the gain and the bias level stable as the transistor heats up. The use of a low bias level is important to reduce the noise produced and is critical to the operation of the system. This circuit starts at $V_{GS}$ and continues through L1, where L1 serves at the RF choke.

Input matching is accomplished by coax 1-3, C8-C15, L3 and the microstrip sections connecting them. Capacitors C12-C15 serve as DC blocks and provide the RF with a path to ground. Coax 1 forms a narrowband 1:1 balanced to unbalanced transformer (balun), converting the single needed input from the coax connector to the balanced signal, separated by 180° phase shift. The balanced signal is needed by the transistor for push-pull operation. Coax 2 and coax 3 are used to form a 4:1 balanced to balanced (balbal) transformer, lowering the impedance from 50 ohms to 12.5 ohms. The other sections of the input matching network serve to make the amplifier stable and further match the input to the 1.3 ohm input impedance of the transistor.

The drain bias section includes everything between L2 and $V_{DD}$. The inductor, L2, is an RF choke, supplying the transistor with DC power. Capacitor C33-C38 filter the input power, removing any RF.
The output matching is accomplished by everything shown from the transistor output to the RF Output. The microstrip sections of the PCB are utilized in the tuning of the output, adding inductance. Coax 4 and 5 form a 1:4 Balbal, stepping the impedance up, closer to 50 ohms. Capacitors C25-C32 form a DC block. So many capacitors are used in parallel to lower the ESR and increase the power handling capacity. Coax 6 is used to form a 1:1 Balun.
Figure 5.1: VHF TV broadcast reference design schematic diagram.
Another very important design consideration is the cooling of the transistor, as the junction temperature directly affects the MTTF. To accomplish this task, the device must have the heat removed from the package. Assuming a relatively ideal efficiency of 75% and a worse case duty cycle of 40%, there would be 100 watts of power, in the form of heat. To keep the device from exceeding the junction temperature, this heat must be removed from the device. The method selected for heat extraction is the heat spreader. Another option would be to use liquid cooling, but this proved to be too costly and cumbersome for operation of the radar in the typical environments where CReSIS systems are deployed.

A prototype system was assembled in the laboratory. The amplifier consists of input bandpass filter to remove any out of band emissions from the 8 channel WFG, 50 watt driver amplifier that is transistor-transistor logic (TTL) switched, 1-kW Freescale DVB-T reference amplifier, Renaissance Electronics 2B1NH circulator [44], and Trilithic H9BE195/32-3-KK 30MHz wide bandpass filter centered at 195MHz to the antenna. The receive path consists of the Trilithic bandpass filter, Circulator, Duplexer circuit, and CMOS isolation switch. There are provisions in the mechanical layout for a LNA and low pass filter that are not populated at this time.

Fast switching, high power, pin-diode T/R switches are not always practical for high power designs because of the tradeoff between switching speed and high power. In addition they require high voltages supplies which add complexity to the system. This makes them impractical to implement in this design. The circulator and duplexer take the place of a traditional T/R switch. The circulator alone cannot be used because of the amount of power
reflected from an antenna matched to -10 dB insertion loss during transmit is 100 watts. The Duplexer alone cannot be used due to the power handling issues described in chapter 5.9.2.
Figure 5.2: Prototype power amplifier.
Figure 5.3: System Block Diagram
5.2 Measurements

This chapter will present the measurement setup and data collected during lab tests of the prototype amplifier system.

5.3 Output power

The output power of the entire system is dependent on both the output from the 1-kW output amplifier and the losses in components to the output port. The power was measured using the Agilent U2021x peak power meter, triggered to the pulse repetition interval (PRI) TTL signal from the DDS. This signal is a TTL pulse indicating the start of the radar pulse. The pulse length of the RF chirp used was 10 µs. 50 dB of attenuation was used between the amplifier output and the pulse power meter. When the output of the 1-kW drive amplifier is 60 dBm, the power at the output port is 58.22 dBm. The loss in power is attributed to the loss from the circulator, directional coupler, output bandpass filter and coax.

5.4 Gain Compression and the need for pre-distortion

The gain of each amplifier stage was measured as a function of input power for five discrete frequencies within the band of operation. These frequencies cover the nominal range of operation of the 1-kW amplifier and that of MCoRDS/I. The measurements were accomplished with a vector network analyzer (VNA) that was set to pulse the RF source. The pulse duration was set to 10 µs with a pulse repetition frequency (PRF) of 12 kHz. These are the same parameters that are nominally used with the 10 µs waveform during low-altitude operation. The only difference between this measurement setup and the radar is that the amplitude does not have a window (e.g. Tukey) applied to it. The driver amplifier consists of a
two-stage 50-watt amplifier based on Polyfet devices [15]. The driver amplifier is driven at approximately -8.4 dBm with its gate bias voltage switched from a secondary pulse generated by the VNA. This pulse was 13 µs long and occurred 2 µs before the RF pulse to give sufficient time for the amplifier to completely turn on. Figure 5.4 shows a block diagram of the measurement setup.

Figure 5.4: Driver amplifier gain compression test setup

The output power of the VNA was calibrated using a power meter. For the measurement of the high-power stage, the effect of the driver amplifier was taken into account by performing a separate calibration with the driver using pulse mode. The driver amplifier cannot be operated in continuous wave (CW) mode due to potential heating issues, and the pulse mode represents a more realistic operating condition. The test setup for the gain compression measurement of the high power, 1-kW stage is shown in Figure 5.5.
When the power is pulsed during source calibration, the measurement must be adjusted by a correction factor given by $10\log_{10}(\% \text{ Duty Cycle})$. The correction is required because the power measurement is done in terms of average power, not peak power [45]. Once the source calibration has been completed, the receiver calibration follows to give the gain measurement of the DUT. The measured gain of the driver amplifier for various levels of input power and operating frequencies is shown in Figure 5.6. From this plot, it can be seen that the gain of the amplifier is dependent on both frequency and input power. For all measured frequencies, the device begins to experience gain compression effects for an input power close to 0 dBm. The 1 dB gain compression point occurs when the input power reaches approximately 7 dBm, which is much higher than what is required to reach the desired output power at the high-power stage. Since the driver amplifier will operate far from the compression region, the overall linearity of the system will be dominated by the contribution of the 1-kW stage.
Figure 5.6: Measured Gain Vs. Input Power for the driver Amplifier

The plot of the measured gain of the high-power stage for various levels of input power and a few discrete frequencies is shown in Figure 5.7. The gain profile leading to compression changes much more rapidly than the gain profiles shown in Figure 5.6 for the driver amplifier. It is possible to infer the output power from this plot, since both the gain and input power levels are known for any given frequency. From this plot it can be seen that the amplifier needs to operate in the compression region to accomplish the desired output power of 60 dBm. Moreover, there is a significant variation in the gain as a function of operating frequency. The operation of the radar requires an output waveform with a pre-defined windowed envelope (typically a Tukey function) having 1-kW of peak power across the middle of the band. This can be achieved using digital pre-distortion, as will be discussed in chapter 6.
5.5 Frequency Response

The gain of each amplifier circuit is plotted against frequency for a given, constant, input power of -8.4 dBm. The results of gain measurement for the driver amplifier is shown in Figure 5.8. The gain over frequency for the 1-kW output amplifier is shown in Figure 5.9.
Figure 5.8: Measured gain Vs. frequency of the driver amplifier stage operating in pulse mode for an input drive level of -8.4 dBm.

Figure 5.9: Measured Gain Vs. Frequency of the high-power stage operating in pulse mode for an input drive level of 37 dBm.
5.6 Phase and Time Delay

The phase delay of the amplifier should have a linear rate of change with respect to the change in frequency. This rate of change is known as the group delay[24]. The phase and time delay are critical in a phased antenna array system. If one or more channels do not maintain the same delay as the others, the antenna pattern will become skewed. In the application for MCoRDS/I, this can lead to increased clutter, potentially masking weak bed returns.

The phase and time delays with respect to frequency from the driver and 1-kW amplifiers are shown below.

![10μs Pulsed Driver Amplifier Unwrapped Phase vs. Frequency](image)

**Figure 5.10:** Measured Phase Vs. Frequency for the driver Amplifier for an input power level of -8.4 dBm.
Figure 5.11: Measured Delay Vs. Frequency for the driver amplifier for an input power level of -8.4 dBm.

Figure 5.12: Measured Phase Vs. Frequency for the 1-kW amplifier at 37 dBm drive level.
Figure 5.13: Measured Delay Vs. Frequency for the 1-kW amplifier for an input drive level of 37 dBm.

The phase of the Driver amplifier, in Figure 5.10, decreases linearly as the frequency increases.

The 1-kW amplifier phase measurement, in Figure 5.12, shows that the phase change with frequency is not perfectly linear. The change in group delay with the 1-kW amplifier is not significant enough to require correction in this application.

5.7 Spurious Products

Single tone and two-tone spurious product measurements were conducted on the driver and 1-kW output amplifiers. These two tests determined the linearity of the two amplifiers. The single tone test was conducted with the Agilent 8648D signal generator to generate the pulsed RF, Agilent 33522A arbitrary waveform generator to generate the TTL pulse timing signals, and the Agilent E4407B spectrum analyzer to measure the output of the amplifier.
The two-tone test measures the intermodulation distortion of the amplifier. This measures the amount and strength of mixing between two tones within the amplifier. The more nonlinear the circuit, the more mixing will occur. In this setup, the arbitrary waveform generator is replaced by the vector network analyzer (VNA). The VNA serves as both a second signal source and handles all of the TTL pulse timing.

5.7.1 Harmonic
To assess the spectral purity of the output signal at nominal operating levels, a test tone of 194.9 MHz of -8.4 dBm of power was applied first to the driver alone and then to the combination of driver and high-power stage while the output signal was monitored and recorded on a spectrum analyzer (SA). A high power attenuator was placed between the output of the amplifier under test and the SA to bring the signal to adequate levels. Figure 5.14 shows a block diagram of the experimental setup of the harmonic test with the driver amplifier. The setup for the 1-kW output amplifier is identical, except the 1-kW amplifier follows the driver amplifier in the RF chain.
Figure 5.14: Harmonic distortion test setup

All instruments were synchronized to the 10 MHz reference clock from the arbitrary waveform generator (AWG) so all signals and measurements would be coherent. The SA was set to cover 100 MHz to 2 GHz in 8192 points. The IF bandwidth of the SA was set to 300 kHz with peak detection. These settings resulted in a sweep time of 81.91 ms of the SA. The pulse length was set to 90 ms with a PRF of 2.6 Hz. This maintained the duty cycle of the original 10 µs, 12 kHz PRF waveform while allowing the signal to be present during the entire SA sweep. If the pulse length was kept at 10 µs, used in other measurements, the SA would not have time to sweep the entire measurement bandwidth, resulting in errors.
The measured harmonic power from the driver amplifier is shown in Figure 5.15. From this plot, it can be seen that the second-harmonic is at -45.83 dBC while the third-harmonic is at -37.18 dBC. Higher order harmonics were below the noise floor of the SA. Figure 5.16 shows the harmonic power produced by the high-power amplifier stage. The harmonics generated from the 194.9 MHz tone are much lower than with the driver amplifier. The second-order harmonic is at -60.37 dBC and the third-order harmonic is at -50.89 dBC. This is attributed to the narrow bandwidth of the matching network of the amplifier, as the latter severely attenuates signals outside the band of operation. The spurious signal present at 298.3 MHz is attributed to third-order intermodulation distortion produced by the 194.9 MHz test signal and a 91.5 MHz (IP3 = 2*194-91.5 = 298.3) broadcast signal from nearby radio station.

Figure 5.15: Measured output spectrum for the driver amplifier for an input tone of 194.9 MHz and -8.4 dBm of power.
5.7.2 Intermodulation

The background of intermodulation distortion (IMD) was described in chapter 2.2.5. As mentioned in chapter 3.1, for the case of the narrow-band MCoRDS/I radar in normal operation, only one tone is present at the input at any given time. Linearity characteristics, however, will be critical for adequate performance of future versions of MCoRDS/I that support operation over wider bandwidth.

The IMD characteristics for both the river pre-amplifier and the 1-kW amplifier were evaluated for completeness. Two separate tones at 194 MHz and 197 MHz, at suitable power levels, were applied simultaneously to the amplifier under test using a power combiner, while the output signal was monitored and recorded using a SA. The power of the input tones was -
11.4 dBm, 3 dB lower than the nominal -8.4 dBm, for the driver amplifier and high-power stages.

The two-tone test setup for the driver amplifier is shown in Figure 5.17 below. All instruments use the 10 MHz reference from the vector network analyzer (VNA). This ensures that all signals are coherent and the two tones do not destructively interfere. The VNA is used a second signal generator with the Agilent 8648D signal generator, as a second generator capable of a pulsed signal was not available. The VNA also produces the control signals for the pulse trigger of signal generator and the acquisition trigger of the SA. The VNA also produces the TTL gate bias switching pulse for the driver amplifier.

The SA was set to cover a span from 1 MHz to 600 MHz at 8192 points, and IF bandwidth of 300 kHz. These parameters created a sweep time of 81.91 ms. This sweep rate is much slower than the 10 µs pulse used in other measurements. If 10 µs were used, much of the signal would not be captured by the SA and would result in inaccurate measurements. For this reason, the length of the pulse was increased to 90 ms and the PRF was extended to 2.6 Hz. This maintained the same duty cycle as the 10 µs, 12 kHz PRF pulse, but allowed for the slower sweep time of the SA.

Power output was verified using the U2021 peak power meter. The power acquisition was triggered by the RF Pulse Trigger line, output by the VNA. The power measurement was taken with the meter in peak power mode. The power from the VNA and signal generator was measured, along with the output from the combiner.
Figure 5.17: Driver amplifier two-tone test setup

Figure 5.18 and Figure 5.19 show the output spectrum of the driver amplifier during the intermodulation distortion measurements. Figure 5.19 was sub-banded for greater detail. The amplitude scale is in dB referenced to the carrier (dBc). From these plots, it can be seen that the driver amplifier is fairly linear for the operating conditions used during the measurement, with the largest spurious signal being -26.73 dBc at 3.048 MHz. Within the 180 MHz to 210 MHz of the output filter, the largest spurious emission is at -33.8 dBc. This is important to note, because unlike the 3.048 MHz signal, spurious signals within the pass-band of the filter will not
be filtered out of the transmitted signal, thus causing distortion. IMD products below -20 to -30 dBc are normally acceptable for a linear amplifier[46].

The two-tone test of the 1-kW amplifier was conducted with a setup similar to that of the driver amplifier, with the exception that the driver amplifier was placed at the input of the 1-kW amplifier. The resulting data from this test are shown in Figure 5.18. From this plot, it can be seen that the IMD products measured for the driver amplifier are very different from those measured at the output of the 1-kW. First, the second- and third-order IMD products located outside the nominal operating frequencies of the amplifier (170-230 MHz) are greatly attenuated. The highest value for any IMD product outside of the amplifier’s operating range is -47.75 dBc, more than 10 times lower than the value recorded for driver amplifier. Near the location of the third-order IMD products, within the amplifier’s range of operation, there are many more products than predicted from the calculations presented in chapter 2.2.5. Figure 5.19 shows this in more detail.
Figure 5.18: Output spectrum for the driver amplifier over the 2-600 MHz measured with two tones applied to the input.
Figure 5.19: Subset of driver two-tone spectrum
Figure 5.20 shows the fundamental tones at 194 MHz and 197 MHz with amplitude of 0 dBc and -0.37 dBc respectively. The reason the amplitudes are not the same is because of a slight amplitude imbalance of the input tones. Given the frequency of the two tones used in this test, the second-order products can be calculated to be at 191 MHz and 200 MHz. These products can be identified in Figure 5.21 with amplitudes of -26.94 dBc and -23.59 dBc, which are considered to be two to four times higher than desired [24]. In addition, the other frequency products present in the output spectrum are be attributed to higher order IMD products. For linear amplifiers, only the third-order products are commonly considered when evaluating IMD performance. For highly non-linear devices, such as this amplifier biased at $I_{\text{dq}}=25\text{mA}$, higher order IMD products do affect the output signal and need to be considered. For example, it can be shown, the IMD product at 188 MHz is actually a fifth-order product where $188\text{ MHz} = 3(194\text{ MHz}) – 2(197\text{ MHz})$.

The two-tone test of the 1-kW amplifier was conducted with a setup similar to that of the driver amplifier, with the exception that the driver amplifier was placed at the input of the 1-kW amplifier. The resulting data from this test are shown in Figure 5.20. From this plot, it can be seen that the IMD products measured for the driver amplifier are very different from those measured at the output of the 1-kW. First, the second- and third-order IMD products located outside the nominal operating frequencies of the amplifier (170-230 MHz) are greatly attenuated. The highest value for any IMD product outside of the amplifier’s operating range is -47.75 dBc, more than 10 times lower than the value recorded for driver amplifier. Near the location of the third-order IMD products, within the amplifier’s range of operation, there are
many more products than predicted from the calculations presented in Section 2.2.5. Figure 5.21 shows this in more detail.
Figure 5.20: 1-kW amplifier output spectrum from two-tone test.
Figure 5.21: Subset of 1-kW two-tone spectrum
5.8 Added Noise

Noise coupled from the transmitter into the received radar signal will have negative impact on the quality of the data collected, as interfering signals and noise can potentially mask weak radar echoes. Coherent integration and inter-pulse modulation such as zero-pi [47] are common digital techniques employed to increase signal-to-noise-ratio and reduce coherent noise. Incoherent noise, however, is more difficult to eliminate in post-processing.

We have experienced noise issues from the power supplies biasing the power amplifiers in the past [48].

Proper design practices considering electromagnetic-compatibility issues mitigate noise problems. One of the steps implemented in past versions of the MCoRDS/I power amplifier was to switch the gate bias voltage on the amplifier. The version proposed in this document does not employ the gate switching solution but uses properties of the Class C amplifier to achieve the same result.

5.8.1 Amplifier-generated Noise

The data in Figure 5.23 and Figure 5.24 were collected using the test setup shown in Figure 5.22. Antennas and the anechoic chamber [49] were used to prevent any damage to the equipment in case the output signal was larger than predicted. The amplifiers were turned on without an input signal and the resulting noise was recorded. Two cases were tested, one with the driver amplifier pulsed and the other with it constantly on. To keep the advantages gained from increased transmit power, it was critical that the noise produced during receive did not exceed the levels of the current system.
The results of the pulsed test, in Figure 5.23, show the results at different bias levels compared to the noise produced by the driver, which served as the primary amplifier in the past. The noise of the driver is shown in green in both figures. The bias level of 2.5A to 2A is considered to put the 1-kW device in Class AB linear operation [42, 50]. A bias current of 200mA puts the amplifier into Class C mode of operation [50, 51]. Initial bias points were selected using these values. Both tests show that even the noise produced by a bias current of 0.15A, slightly lower than the suggested bias for Class C, is more than 10 dB higher than the driver. The bias current was decreased until it was close to the noise level of the driver. The bias current of 0.01 A produced the most favorable results, but resulted in the gain being too low. There was a dramatic increase in gain when $I_{dq}=0.05$ A, but also in noise power. The bias point of $I_{dq}=0.025$ A was selected as a tradeoff between gain and amplifier-generated noise.
Figure 5.23: Amplifier Noise Test, Pulsed
5.8.2 Radiated Noise

Noise radiated from the switching power supplies and amplifier circuits was measured using the setup shown in Figure 5.25.

Components contained within the dot-dashed line were all placed on top a foam cube that was approximately 1 m by 1 m by 1 m. This was placed at distance of 7 m from the receive antenna.

Three test cases were considered: the amplifier system running at full output power, the amplifier biased at operating conditions but no drive signal, and everything turned off. The full power condition provides a load on the power supply that is the same during data collection. The noise data were gated, so the data during transmit were not used, as this would not represent the added noise and only show the transmit signal. The second condition, where the amplifiers were biased on, but no RF drive signal was applied, shows the noise contributed by the power supplies while idle and is used for comparison. The final test is used as a baseline for the thermal noise of the chamber and noise generated by the data acquisition system. Figure 5.26 shows the results from these three tests.
There is a 6 dB increase in radiated noise at the peak around 192 MHz from baseline to full output from the amplifier. These data represent the worst case, as none of the components are shielded from the receive antenna. Further reduction in noise can be expected when the components are mounted inside a metal enclosure and are racked inside of aircraft.

5.9 Heating Issues

5.9.1 Heat Spreader Design
The package of the MRFE6VP61K25H transistor, used in this design, is only 1.23 inches by 0.36 inches. This is a very small area to remove a large amount of heat. In order to dissipate the large amount of heat produced by the device into the air, it must be spread over a large surface area. The task of dissipating heat from a small area into the air is accomplished by the
heat spreader. In order to accurately know that the maximum junction temperature of the device is not exceeded, the thermal resistance of the heat spreader system must be calculated. To minimize the thermal resistance, the best thermal connection must be made in the heat spreader system. The contact between the transistor package and copper block is an area that is often overlooked. Large high power transistors, like the MRFE6VP61k25H, are often bolted down with thermal grease between the transistor and the block. For better results, [52] recommends the package be soldered down. This method was used in reducing the thermal resistance. The results of the thermal resistance calculations, which are discussed in chapter 2.2.7, are shown in Table 5.2.

Table 5.2: Thermal resistance of 1-kW amplifier cooling system with 600 LFM air speed over heat spreader.

<table>
<thead>
<tr>
<th></th>
<th>Transistor Case to Tj</th>
<th>Solder</th>
<th>Copper Block</th>
<th>Thermal Conductive Grease</th>
<th>Cool Innovations Heat Spreader</th>
</tr>
</thead>
<tbody>
<tr>
<td>Width [m]</td>
<td>9.1440E-03</td>
<td>9.1440E-03</td>
<td>3.2004E-02</td>
<td>1.2700E-01</td>
<td></td>
</tr>
<tr>
<td>Length [m]</td>
<td>3.1242E-02</td>
<td>3.1242E-02</td>
<td>5.4102E-02</td>
<td>1.2700E-01</td>
<td></td>
</tr>
<tr>
<td>Height [m]</td>
<td>5.0800E-05</td>
<td>1.1430E-02</td>
<td>5.0800E-05</td>
<td>5.0800E-01</td>
<td></td>
</tr>
<tr>
<td>K_th [W/m K]</td>
<td>50 [53]</td>
<td>398 [54]</td>
<td>0.63 [55]</td>
<td></td>
<td></td>
</tr>
<tr>
<td>R_th [°C/W]</td>
<td>1.50E-01 [43]</td>
<td>3.56E-03</td>
<td>1.66E-02</td>
<td>4.66E-02</td>
<td>7.00E-02 [56]</td>
</tr>
<tr>
<td>R_th Total [°C/W]</td>
<td>2.87E-01</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

The Cool Innovations heat spreader [56] was selected for its low thermal resistance and compact size. To produce 600 LFM over the 5 inch by 5 inch area of the heat spreader, a fan capable of 104 CFM is required. The amplifier will be operated well above sea level, meaning the effectiveness of the fan and heat spreader will be reduced. For this reason, the air movement requirement was doubled and a fan capable of 200 CFM was selected for impingement cooling of the heat spreader.
With the thermal resistance known, the junction temperature for a given ambient
temperature and operating conditions can be calculated. Using a worst case 40% duty cycle,
50% amplifier efficiency, the power dissipated by the device at 60 dBm output is 200 watts.
Since the air temperature inside of the aircraft utilized by CReSIS has been found to fluctuate
quite high, an ambient temperature of 32°C was used to find the transistor junction
temperature of 89.34°C. This temperature is much lower than the 225°C maximum [43].
Leaving such a large margin was done for two main reasons, to allow for any errors in
calculations and assumptions, and to allow the amplifier to be used for other applications in the
future.

5.9.2 Thermal Measurements
Using a device designed to produce 1000 watts provides many unique challenges, one of
those being heat management. For a device that comes after the amplifier, if it has as little as 1
dB insertion loss, it is absorbing 251 watts. This power must go somewhere, and is transformed
into heat. Devices used in the system including the power amplifier were checked for heating
issues using a FLIR® i7 camera [57]. All devices under test were painted flat black to achieve the
most accurate results possible. The use of a FLIR® camera was adventitious over an infrared
thermometer because hotspots within a device can be identified instead of an average
temperature over the measurement area.
The driver amplifier, shown in Figure 5.27 is being operated at -8.4 dBm input without switching the gate bias voltage. This is a worst case situation, where switching the gate bias voltage will allow the amplifier to run cooler. It can be seen that the case of the amplifier is reaching 60°C. Other background objects on the bench are seen in Figure 5.27, such as the table top fan at the bottom left.
The image shown in Figure 5.28 shows the thermal image of the 1-kW amplifier while in operation. This image demonstrates the need to use a thermal camera over an infrared thermometer. It can be seen that the hottest parts around the transistor are the inductor that is in box Ar1 and the capacitors that are in box Ar2. The overall average temperature would be measured lower than those individual components. From this image, it was decided to add additional cooling to the top of the amplifier. Identifying individual components that get too hot during operation would be nearly impossible without the use of the FLIR® camera.
Figure 5.29 shows the thermal image of the circulator and load that is used as an isolator. As the image shows, the isolator does not get overly warm and the load is only slightly warmer. The heating in the load can be attributed to the mismatch between the circulator and the duplexer circuit. Keep in mind, a S11 measurement of -10 dB, considered to be an acceptable match, is still 100 watts of power reflected back. Although, pulsed at a 24% duty cycle, that is still a non-trivial amount of power reflected into the load.

The high power coupler is shown in Figure 5.30. The image shows this device does not have much heating from the operation of the power amplifier. This corresponds to its low insertion loss.
Figure 5.30: Thermal image of directional coupler during nominal operation.

Figure 5.31: Thermal image of bandpass filter during nominal operation.

The thermal image of the Trilithic H9BE195/32-3-KK bandpass filter is shown in Figure 5.31. The image shows that a hotspot develops in the middle of the filter, while the ends are
slightly cooler. While this is not critical for this application, as the temperature stays around 40°C, a cooling system could be developed around this measurement.

From the thermal imaging, it is clear that the only component that needs additional cooling is the top of the 1-kW amplifier. The other components show that heating is minimal and the current cooling is sufficient.

The use of thermal imagery was also critical in development of the duplexer, which is discussed in detail in chapter 3 and chapter 4. When the duplexer was implemented as shown in [37] and 60 dBm was applied, the diodes used overheated. This can be seen in Figure 5.32 that the diodes measure 165°C which is close to the 175°C maximum junction temperature of the 1N4148 Diode [39].

![Figure 5.32: Duplexer at 60 dBm under nominal pulse conditions.](image)
Upon closer inspection, in Figure 5.33, the diodes actually exceeded the 175°C junction temperature limit. This caused a topology change, to the one shown in Figure 5.3, where the duplexer is switching the lower reflected power. Nominally, this reflected power should not exceed 50 dBm for an antenna with a return loss of -10 dB.

After the diodes were replaced, the duplexer was then measured at 50 dBm. It was found that some cooling of the diodes was needed, which was implemented with a fan. The result from this test is shown in Figure 5.34. The maximum diode temperature, shown in Figure 5.35, is 45°C. This temperature is well within the limits of the 1N4148 diode.
Figure 5.34: Thermal image of duplexer at 50 dBm under nominal pulse conditions.

Figure 5.35: Close up thermal image of duplexer diodes at 50 dBm under nominal pulse conditions.
6 Digital Pre-Distortion Implementation

An ideal DPD system continuously corrects the waveform in near real-time for amplitude and phase distortions. Due to the limitations of the existing hardware of the MCoRDS/I system, a less than ideal DPD system was implemented. The DPD system for the amplifier does not include phase correction. This means that issues like memory effects cannot be corrected. Since the amplitude variations have been found to be fairly constant during operation, the DPD correction algorithm is not continuously ran.

The DPD system consists of the direct digital synthesis (DDS) signal generator, amplitude correcting MATLAB script and the attenuated output of the amplifier connected to the input of the National Instruments Data Acquisition (DAQ) system. This system allows for a feedback network to be formed where the current input into the amplifier is based on its past outputs. The amplitude correction also relies on a priori knowledge of the amplifier’s output power at 195MHz for a given input power. This allows for the output power to be maintained without the need for calibrated measurements in the feedback system. All corrections are relative to the amplitude of the DDS at 195MHz, allowing for easier setup and measurement during field operation. A flow chart for the DPD algorithm is shown in Figure 5.1.

The first step for the DPD is to run the GUI software that programs the DDS without loading an amplitude shape. The DDS GUI is initially loaded with the desired frequency and duration settings and from this, it calculates the RAM size required for the waveform\(^2\). When this value is entered, the software generates the initial, ideal, amplitude shape for the radar

\(^2\) The amplitude values are stored in a RAM as 1024 discrete values.
chirp. The amplitude is shaped by a 20% Tukey window, but it could be changed to an arbitrary window. After the initial waveform is created with the correct number of points for the RAM size, the DDS is programmed. The attenuated output of the amplifier is recorded using the DAQ GUI. From this point, waveform correction software is executed again, and the previous correction and recorded amplifier output is used to form a new DPD signal. This process is iterated until the output signal presents the desired amplitude profile.

Results from the DPD correction process are shown in Sections 6.1 and 6.2. The results for the driver amplifier are shown separately from those of the entire chain. This helps to show the distortion that the signal experiences at each stage. The MATLAB code used to process and extract the desired envelope profile is shown in the Appendix.
Figure 6.1: Waveform correction flowchart.
6.1 Driver Amplifier Correction

The uncorrected waveform and resulting envelope for the driver amplifier can be seen Figure 6.26. From this plot, it can be seen that here is a significant, frequency dependent, drop in gain. To correct this, the amplitude of the chirp must be adjusted for various frequency. This adjustment can be seen in Figure 6.3.

The recorded data can be seen crossing the reference envelope in the middle of the chirp. This occurs because the amplitude of the data is scaled so that the amplitude at 195 MHz, the middle of the chirp, is the same as a known value. The amplifier’s maximum power of 60 dBm was measured, for a 195 MHz tone, when the input to the Driver pre-amplifier was -8.4 dBm. Since an ideal amplifier should produce a signal that only differs in amplitude at the output, we can scale the recorded data to match the DDS waveform amplitude.

After the first iteration, the corrected, or output, envelope is almost an exact inverse of the recorded data envelope. However, these envelopes are not exact inverse. The error function is defined in Equation (6.1)

\[
\text{error} = \frac{\text{reference envelope} + \varepsilon}{\text{data envelope} + \varepsilon}
\]

(6.1)

The value of \(\varepsilon\) is determined experimentally so that the correction does not overshoot and cause damage by overdriving the amplifier.
Figure 6.26: Uncorrected Driver Amplifier Waveform and Envelope

Figure 6.3: Reference Envelope Compared to Uncorrected Data and Output Envelopes
Figure 6.46: Corrected Driver Amplifier Waveform and Envelope

Figure 6.5: Reference Envelope Compared to Corrected Data and Output Envelopes
The final results, after three iterations, are shown in Figure 6.46 and Figure 6.5. While some noise is seen on the envelope of the recorded data, it fits the reference envelope much closer than the uncorrected case.

### 6.2 1-kW Amplifier Correction

Continuing with the correction from chapter 6.1, the leveled Driver amplifier was used to drive the Freescale DVB-T amplifier. By using the corrected driver, it is possible to see the amplitude distortion caused by the 1-kW amplifier alone. The signal and envelope from the uncorrected 1 kW amplifier is shown in Figure 6.6.
Figure 6.7: Uncorrected Freescale Amplifier

Figure 6.8: Corrected Freescale Amplifier Waveform and Envelope
After four iterations when the Driver amplitude was level, the Freescale amplifier amplitude leveled out. The results of the fourth iteration are shown in Figure 6.8 and Figure 6.9.

6.3 System Correction

Both the driver pre-amplifier and the 1-kW final amplifier were corrected at the same time for this test. The amplifier system output before correction is shown in Figure 6.10. The first iteration corrected input compared to the data envelope and reference envelope is shown in Figure 6.11. Figure 6.12 and Figure 6.13 show the resulting waveform and input power after 5 iterations.
Figure 6.10: Uncorrected System Waveform and Envelope

Figure 6.11: System Uncorrected Data, Reference and DDS Envelopes
Figure 6.12: Corrected System Waveform and Envelope

Figure 6.13: System Corrected Data, Reference and DDS Envelopes
6.4 System Power output verification

The waveform correction process relies on relative measurements and corrections. There is nothing, other than a priori knowledge, to set the output power. For this reason, the waveform correction process needs to be verified so that the output power remains at 60 dBm, as measured at 195 MHz. To test the power, the output of the final amplifier was passed through a 49.9 dB attenuator to an Agilent U2021xa peak power meter [58]. Once the power was recorded, the output from the final amplifier was connected to the NI System and the amplitude was corrected as described above. This process was repeated for each iteration.

The power of the uncorrected pulse is shown in Figure 6.14 and Figure 6.15. It can be seen that the power actually exceeds 60 dBm from 1.5 µs to 6.75 µs. After 6.75 µs, the power quickly drops by 4 dB until the taper of the Tukey window effects the pulse around 10 µs. After five iterations, the pulse becomes fairly flat and ideal. The power profile for the corrected pulse can be seen in Figure 6.16 and Figure 6.17. From these plots, it is easy to see that the power has been leveled out. Power fluctuations across the pulse are less than 1 dB.
Figure 6.14: Iteration 0 Output Power 20dBm to 65dBm

Figure 6.15: Iteration 0 Output Power 55dBm to 65dBm
Figure 6.16: Iteration 5 Output Power 20dBm to 65dBm

Figure 6.17: Iteration 0 Output Power 55dBm to 65dBm
The input power to the amplifier was also recorded for the uncorrected and corrected cases. The output from the DDS was filtered and connected to the peak power meter. From Figure 6.18, it is possible to see that there is some variation in power of the input signal. This can be attributed to the filter used and in the output of the DDS. The amplitude correction algorithm is able to compensate this along with the other amplitude distortions in the system.

![Uncorrected Input Power](image)

**Figure 6.18: Uncorrected Input Power**

The input power from the fifth iteration is shown in Figure 6.19. Comparing this result plotted on a linear scale in Figure 6.20 with the corrected envelope in Figure 6.13, they can be seen to closely match, as expected. The input power ranges from -6.3 dBm to -11.78 dBm, a difference of 5.48 dB, or almost four times.
Figure 6.19: Corrected Input Power

Figure 6.20: Corrected Input Power, Linear Scale
7 Conclusions and Future Work

7.1 Conclusion

A power amplifier system for the MCoRDS/I radar depth sounder was developed and implemented. The unit weighs 23.4 kg for a single channel and can be extended to multiple channels. This system was implemented using a COTS amplifier system, originally designed for linear television broadcast transmission, was modified to operate in class C. By operating in class C, the amplifier was able to meet the noise specifications set by previous amplification systems while obtaining higher output power.

DPD allowed the amplifier to move away from linear schemes used in the past while maintaining the ability for the radar to utilize amplitude shaping. The DPD technique was used to correct amplitude variations as a function of frequency and the input power in the amplifier was successfully corrected using digital techniques, resulting in the capability to produce 60 dBm +/- 1 dB across the 180-210 MHz frequency range of operation. The amplification system also included a duplexer derived from NMR systems to facilitate the high power and fast switching requirements of the MCoRDS/I radar.

7.2 Future work

The narrowband duplexer system, described in chapter 3.1.1, needs to be integrated with the system. This will eliminate the need for the ferrite circulator, reducing weight and loss, resulting in an increase of output power. The current DPD system requires manual intervention from the operator. Future implementations should include an automated real-time system for DPD error correction.
References


Department of Electrical Engineering and Computer Science, University of Kansas, Lawrence, 2010.


%% Correct the MCoRDS/I Pulsed Chirp Waveform
%
% This program corrects the frequency dependent amplitude distortion caused
% by the Polyfet driver and Freescale 1KW DVB-T amplifiers.
% The function relies on data collected from the NI System to correct the
% waveform.
%-------------------------------------------------------------------------
%% Correction Steps:
%-----------------
% 1) Start MCoRDS/I DAQ GUI
% 2) Start DDS_GUI_amp
% 3) Load config for Amplitude Correction.
% All settings, except for presums, should be the same as what
% you're planning on running for data collection. Presums should
% be set 1 and only one waveform should be used.
% 4) Select 'time enable' and click 'Program'
% There will be several warnings/errors, this is normal for this
% setup. Keep clicking 'continue' until they're cleared.
% 5) Deselect 'time enable' and click 'Program'
% There will be several warnings/errors, this is normal for this
% setup. Keep clicking 'continue' until they're cleared.
% 6) Turn on the main power to the PA (top switch).
% 7) Wait 10 seconds after main power switch is turned on, then turn on
% PA Bias (bottom switch).
% 8) Enter the value from the 'ram size' box in the DDS_GUI_amp window
% into the parameter value 'ramPoints' in the WF_Correct.m MATLAB
% program and check that other parameters are correct as well.
% 9) Set 'firstRun' flag to 1 and run WF_Correct.
% 10) In the DDS_GUI_amp program, click the file open icon next to the
% 'amp file' text box. Select 'DDS_Amp_Corr.bin' and click 'OK'
% 11) Click 'time enable' and then click 'Program'
% After this step you should see the uncorrected output from the
% amplifier on the A-Scope.
% 12) Record 3 files of data with the amplifier running.
% 13) In WF_Correct, change the 'firstRun' flag to 0. Run the program.
% A window will popup, select the 2nd file (or any file that's
% not the first or last) that was recorded and click OK. The
% program will now correct the waveform. It may take a few
% iterations to get it fairly level. The amount of "gain" the
% correction has is controlled by 'eps,' the larger the number,
the slower the corrections will be. Do not go much lower than 20000, otherwise there will be a lot of overshoot.

14) Repeat steps 10 through 12 until you reach an acceptable result. This usually takes 3 - 5 times.

clc; clear all;
close all

firstRun = 1; % 1 indicates this is the first time the function is being ran.
% 0 indicates this is an iteration of the correction

%% Parameters
pulseLen = 10e-6; % Pulse length in seconds
Fs = 1e9/9; % Sampling frequency [Hz]
startF = 180e6; % Chirp start frequency [Hz]
stopF = 210e6; % Chirp stop frequency [Hz]
debug = 1; % Debugging Flag. Generates several plots
savePlot = 0; % The number of points required for the ram
ramPoints = 222; % The DDS value to get the desired output at 195MHz
MaxDDS = 28350; % Prevent correction from overshooting.
eps = 3000;

%% Constants
fn_out = 'DDS AMP_Corr.bin'; % DDS Amplitude shape filename
fn_fulcor = 'LastCorr.mat';
whichBits = 0; % Number of LSBs to drop
presums = 1; % Number of presums
tukeyWinPer = 0.2; % Tukey windowing [%]
MCoRDS/I = 0; % Flag to indicate if the code is being used on the MCoRDS/I system or the single channel test system

%% Generate the ideal amplitude w/ no correction for the first iteration
if firstRun == 1
    WF = struct('pulseLen', pulseLen, 'Fs', Fs, 'startF', startF, 'stopF',
                 'ramPoints', ramPoints, 'MaxDDS', MaxDDS, 'tukeyWinPer',
                 'fn_out', fn_out, 'fn_fulcor', fn_fulcor);

    WF_First_Run(WF);

    return;
else
    % After the first run, load recorded data and correct
    load(fn_fulcor);

%% Load desired data file
[filename, pathname] = uigetfile('*.bin');
fn=sprintf('%s%s',pathname,filename);
% fn = 'C:\kuband\kuband_01_20130409_141014_0043.bin';

param  = struct('clk',Fs);
param.wfs   = [0];
param.rec   = [1 1];
if MCoRDS/I == 0
    [hdr, data] = basic_load_fmcw2(fn,param);
else
    [hdr, data] = basic_load_MCoRDS/I2(fn,param);
end

data = data';

% Remove any DC offset
DCoffset    = mean(data(1:101));
data       = data - DCoffset;
if ((debug == 1) || (savePlot == 1))
    h=figure;
    plot((data), 'k')
    set(gca, 'YTickLabel',num2str(get(gca, 'YTick').'))
    title('Recorded Waveform')
    xlabel('Sample Number')
    ylabel('ADC Word')
    if savePlot == 1
        saveTightFigure(h,sprintf('%sWaveform.jpg',pathname));
    end
end

%% Shift Data start to 0
% Run pulse_compress from the CReSIS-Toolbox
clear pc_param;
pc_param.f0 = startF;
pc_param.f1 = stopF;
pc_param.Tpd = pulseLen;
pc_param.tukey = tukeyWinPer;
pc_param.rx_gain = 1;

Nt = hdr.wfs.num_sam;
if MCoRDS/I == 0
    t0 = hdr.wfs.Tadc;
else
    t0 = hdr.wfs.t0;
end
dt = 1/Fs;
BW = pc_param.f1-pc_param.f0;
alpha = BW/pc_param.Tpd;
pc_param.time = t0 + (0:dt:(Nt-1)*dt).';

signal = data';
signal(pc_param.time<0 | pc_param.time>pc_param.Tpd) = 0;
[pc_signal,pc_time] = pulse_compress(signal,pc_param);

if debug == 1
  figure;
  %Plot pulse compressed signal
  plot(pc_time*1e6, lp(pc_signal,2));
  xlabel('Time (us)');
  ylabel('Relative power (dB)');
end

% Find start point at corresponding index to data
idx=find(pc_param.time<=pc_time(find(abs(pc_signal)==max(abs(pc_signal)),1,'first')),...
  ,1,'last');

% Calculate the hilbert of the data
if ((debug == 1)||(savePlot == 1))
  h=figure; plot(data); hold on
end
data = abs(hilbert(data));

if ((debug == 1)||(savePlot == 1))
  plot(data,'r','LineWidth', 2)
  hold on
  set(gca,'YTickLabel',num2str(get(gca,'YTick').'))
  title('Recorded Waveform and Envelope')
  ylabel('ADC Word')
  xlabel('Sample Number')
  legend('Waveform','Envelope','Location','Best')
  if savePlot == 1
    saveTightFigure(h,sprintf('%sWave&Env.jpg',pathname));
  end
end

% Lowpass filter to smooth the data
firFiltCoeff=1000;
fir6dBcutoff=50e6;
d=fdesign.lowpass('N,Fc',firFiltCoeff,fir6dBcutoff,Fs);
Hd=design(d);
data = filter(Hd,data);

% Shift data back to orig pos
data = [data(1,(firFiltCoeff/2):end) data(1,1:((firFiltCoeff/2)-1))]
if debug == 1
  figure;plot(data,'g')
end
% Shift the start of the pulse to 0 and truncate
data = data(idx:(idx+ceil(pulseLen/dt))-1);

% Scale the amplitude at 195MHz to MaxDDS
% Find the sample number for the 195MHz point in the chirp
sampleFor195 = findFrequency(195e6,startF,stopF,length(data));
% Make sure the value of MaxDDS is no bigger than the maximum value the DDS can produce: 65535
MaxDDS(MaxDDS>65535)=65535;

% Scale the data so the value at the 195MHz point is = to MaxDDS
scaleFac = MaxDDS/data(1,sampleFor195);
data = scaleFac*data;
refAmp = MaxDDS;

%% Generate Ref Chirp
t   = 0:1/Fs:pulseLen;
theChirp = MaxDDS*(chirp(t,startF,max(t),stopF));
win = tukeywin(length(theChirp),tukeyWinPer);

% Apply Tukey Window to Chirp
theChirp = (theChirp.*win');

if debug ==1
    figure;
    plot(theChirp)
end

%% Hilbert transform to get envelope
theChirp = abs(hilbert(theChirp));
L = length(theChirp);
theChirp = [theChirp zeros(1,(firFiltCoeff))];
theChirp = filter(Hd, theChirp);
theChirp = [theChirp(1,(firFiltCoeff/2):end) theChirp(1,1:((firFiltCoeff/2)-1))];
theChirp = theChirp(1,(1:L));
% Scale Ref Back Up
scaleFac = MaxDDS/theChirp(1,sampleFor195);

%% Find error between ideal and actual. Create amplitude correction.
error = ((theChirp+eps)./(data+eps));
corrLin = lastCorr.*error;
corrLin(1,1) = 0;
corrLin(1,end) = 0;

if ((debug ==1)||(savePlot == 1))
h=figure;
plot(data)
hold on
plot(theChirp,'r')
hold on
plot(corrLin, 'g')
set(gca, 'YTickLabel',num2str(get(gca,'YTick'))
set(gca,'YTickLabel','num2str(get(gca,'YTick'))
title('Amplitude Envelopes')
ylabel('ADC Word')
xlabel('Sample Number')
legend('Data Envelope','Reference Envelope','Corrected Envelope','Location','Best')
if savePlot == 1
    saveTightFigure(h,sprintf('%sDataRefCorr.jpg',pathname));
end
end

% Set current corrected value to the lastCorr variable
lastCorr = corrLin;
% Write lastCorr to file. This is used for the next iteration.
save(fn_fulcor,'lastCorr')
if debug == 1
    figure;
    plot(corrLin)
    hold on
    plot(theChirp,'r')
end

%% Convert to 16-Bit Unsigned Int and write to file
% Make sure corrLin is limited to 65535
corrLin(corrLin>65535)=65535;

% Convert to 16-Bit unsigned integer
ddsAmpFile = uint16(corrLin);
% Determine the new sample rate for the number of rampoints and decimate
step = (floor(length(ddsAmpFile)/ramPoints));
ddsAmpFile = ddsAmpFile(1:step:(length(ddsAmpFile)-step));

% Pin the first and last value to 0
ddsAmpFile(1,1)=0;
ddsAmpFile(1,end)=0;

if ((debug==1)||(savePlot == 1))
    h=figure;
    plot(ddsAmpFile,'k','Linewidth',2)
    set(gca,'YTickLabel',num2str(get(gca,'YTick')))'
    title('DDS Amplitude')
    xlabel('Sample Number')
    ylabel('DDS Word')
    if savePlot == 1
        saveTightFigure(h,sprintf('%sDDSWaveform.jpg',pathname));
    end
end

% Reverse the order for the correction as the DDS reads the envelope in
% backwards
ddsAmpFile=fliplr(ddsAmpFile);
if debug == 1
    max(ddsAmpFile)
end

% Write the amplitude envelope to file
fid = fopen(fn_out,'w');
fwrite(fid, ddsAmpFile,'uint16','b');
fclose(fid);
if ((savePlot == 1)&&(debug ~= 1))
% close all
pathname
end
return;
Appendix B  findFrequency MATLAB Function

```matlab
function data=findFrequency(findFreq,startF,stopF,samples)

% Calculate the frequency step size
freqPerSamp = (stopF-startF)/samples;

distanceFromStart = findFreq-startF;

data = distanceFromStart/freqPerSamp;

return
```
function output = WF_First_Run(WF)
% Generate full length window function
  t = 0:1/WF.Fs:WF.pulseLen;
  lastCorr = [WF.MaxDDS*(chirp(t,WF.startF,max(t),WF.stopF))];
  win = tukeywin(length(lastCorr),WF.tukeyWinPer);
  lastCorr = lastCorr.*win';
  lastCorr = abs(hilbert(lastCorr));
  save(WF.fn_fulcor,'lastCorr');

% Generate Window function for RAM
  win = tukeywin(WF.ramPoints,WF.tukeyWinPer);
  ramWin = win.*WF.MaxDDS;
  lastCorr = ramWin;
  ddsAmpFile = uint16(ramWin);
  fid = fopen(WF.fn_out,'w');
  fwrite(fid, ddsAmpFile,'uint16','b');
  fclose(fid);
return;
**Appendix D**

**saveTightFigure MATLAB Function**

```matlab
function saveTightFigure(h,outfilename)
% SAVETIGHTFIGURE(H,OUTFILENAME) Saves figure H in file OUTFILENAME without
% the white space around it.
% % by `a grad student"
% % http://tipstrickshowtost.blogspot.com/2010/08/how-to-get-rid-of-white-
% margin-in.html

% get the current axes
ax = get(h, 'CurrentAxes');

% make it tight
ti = get(ax,'TightInset');
set(ax, 'Position', [ti(1) ti(2) 1-ti(3) ti(1) 1-ti(4)-ti(2)]);

% adjust the papersize
set(ax, 'units', 'centimeters');
pos = get(ax, 'Position');
ti = get(ax,'TightInset');
set(h, 'PaperUnits', 'centimeters');
set(h, 'PageSize', [pos(3)+ti(1)+ti(3) pos(4)+ti(2)+ti(4)]);
set(h, 'PaperPositionMode', 'manual');
set(h, 'PaperPosition', [0 0 pos(3)+ti(1)+ti(3) pos(4)+ti(2)+ti(4)]);

% save it
saveas(h,outfilename);
```